

**DISTRIBUTING  
MULTILOOP RESULTS VIA UFO**

JUST AN IDEA

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# UNIVERSAL FEYNRULES OUTPUT

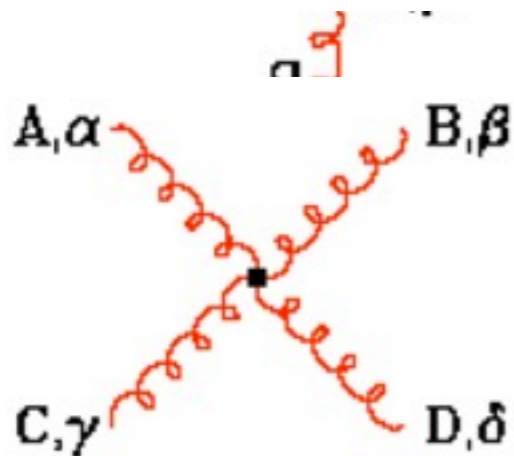
REMINDER

[arXiv:1108.2040]

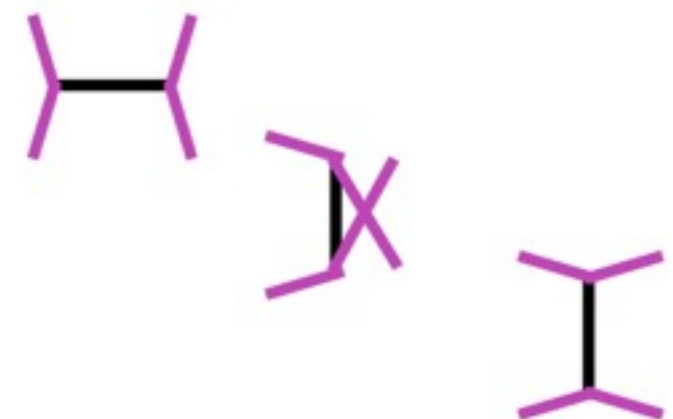
- Python module to specify a model for MC generators

`vertices.py`   `couplings.py`   `parameters.py`   `lorentz.py`

```
V_37 = Vertex(name = 'V_37',
               particles = [ P.g, P.g, P.g, P.g ],
               color = [ 'f(-1,1,2)*f(3,4,-1)',
                        'f(-1,1,3)*f(2,4,-1)',
                        'f(-1,1,4)*f(2,3,-1)' ],
               lorentz = [ L.VVVV1, L.VVVV3, L.VVVV4 ],
               couplings = {(1,1):C.GC_12,
                            (0,0):C.GC_12,
                            (2,2):C.GC_12})
```



$$\begin{aligned} -ig^2 f^{XAC} f^{XBD} & [g^{\alpha\beta} g^{\gamma\delta} - g^{\alpha\delta} g^{\beta\gamma}] \\ -ig^2 f^{XAD} f^{XBC} & [g^{\alpha\beta} g^{\gamma\delta} - g^{\alpha\gamma} g^{\beta\delta}] \\ -ig^2 f^{XAB} f^{XCD} & [g^{\alpha\gamma} g^{\beta\delta} - g^{\alpha\delta} g^{\beta\gamma}] \end{aligned}$$



# UNIVERSAL FEYNRULES OUTPUT

[arXiv:1108.2040]

vertices.py    **couplings.py**    parameters.py    lorentz.py

```
GC_12 = Coupling(name = 'GC_12',  
                 value = 'complex(0,1)*G**2',  
                 order = {'QCD':2})
```



**coupling\_orders.py**

```
QCD = CouplingOrder(name = 'QCD',  
                    expansion_order = 99,  
                    hierarchy = 1)  
  
QED = CouplingOrder(name = 'QED',  
                    expansion_order = 99,  
                    hierarchy = 2)
```

# UNIVERSAL FEYNRULES OUTPUT

[arXiv:1108.2040]

vertices.py    couplings.py    **parameters.py**    lorentz.py

```
G = Parameter(name = 'G',
              nature = 'internal',
              type = 'real',
              value = '2*cmath.sqrt(aS)*cmath.sqrt(cmath.pi)',
              texname = 'G')
```

```
aS = Parameter(name = 'aS',
              nature = 'external',
              type = 'real',
              value = 0.118,
              texname = '\\alpha_s',
              lhablock = 'SMINPUTS',
              lhacode = [ 3 ])
```

# UNIVERSAL FEYNRULES OUTPUT

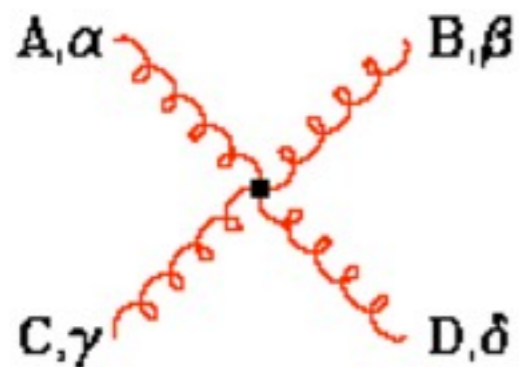
[arXiv:1108.2040]

vertices.py    couplings.py    parameters.py    **lorentz.py**

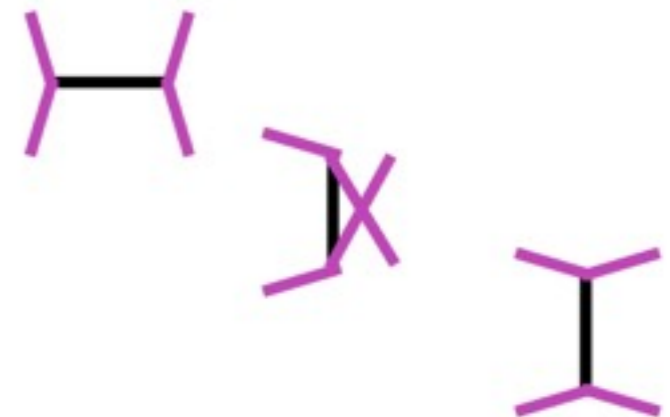
```
VVVV1 = Lorentz(name = 'VVVV1',  
               spins = [ 3, 3, 3, 3 ],  
               structure = 'Metric(1,4)*Metric(2,3) - Metric(1,3)*Metric(2,4)')
```

```
VVVV3 = Lorentz(name = 'VVVV3',  
               spins = [ 3, 3, 3, 3 ],  
               structure = 'Metric(1,4)*Metric(2,3) - Metric(1,2)*Metric(3,4)')
```

```
VVVV4 = Lorentz(name = 'VVVV4',  
               spins = [ 3, 3, 3, 3 ],  
               structure = 'Metric(1,3)*Metric(2,4) - Metric(1,2)*Metric(3,4)')
```



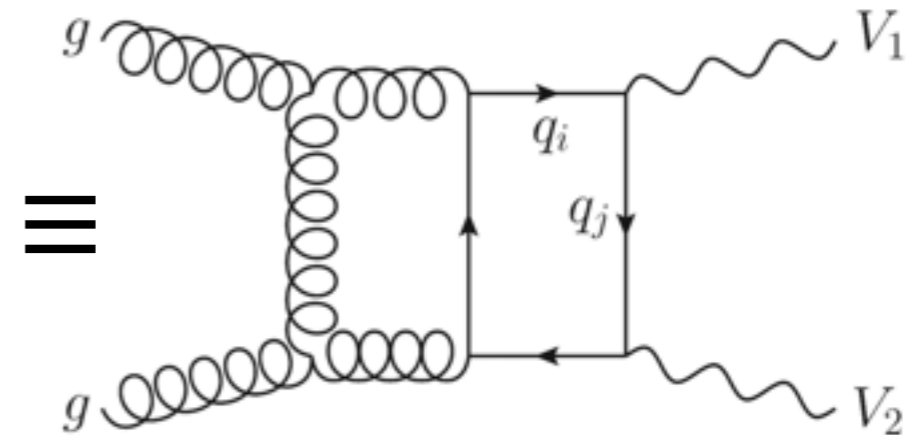
$$\begin{aligned} & -ig^2 f^{XAC} f^{XBD} \begin{bmatrix} g^{\alpha\beta} g^{\gamma\delta} & -g^{\alpha\delta} g^{\beta\gamma} \end{bmatrix} \\ & -ig^2 f^{XAD} f^{XBC} \begin{bmatrix} g^{\alpha\beta} g^{\gamma\delta} & -g^{\alpha\gamma} g^{\beta\delta} \end{bmatrix} \\ & -ig^2 f^{XAB} f^{XCD} \begin{bmatrix} g^{\alpha\gamma} g^{\beta\delta} & -g^{\alpha\delta} g^{\beta\gamma} \end{bmatrix} \end{aligned}$$



# MULTILOOP FORM FACTORS

- IDEA: use a similar format for distributing multi-loop form-factors:

$$\begin{aligned}
 S^{\mu\nu\rho\sigma}(p_1, p_2, p_3) &= a_1 g^{\mu\nu} g^{\rho\sigma} + a_2 g^{\mu\rho} g^{\nu\sigma} + a_3 g^{\mu\sigma} g^{\nu\rho} \\
 &+ \sum_{j_1, j_2=1}^3 \left( b_{j_1 j_2}^{(1)} g^{\mu\nu} p_{j_1}^\rho p_{j_2}^\sigma + b_{j_1 j_2}^{(2)} g^{\mu\rho} p_{j_1}^\nu p_{j_2}^\sigma + b_{j_1 j_2}^{(3)} g^{\mu\sigma} p_{j_1}^\nu p_{j_2}^\rho \right. \\
 &\quad \left. + b_{j_1 j_2}^{(4)} g^{\nu\rho} p_{j_1}^\mu p_{j_2}^\sigma + b_{j_1 j_2}^{(5)} g^{\nu\sigma} p_{j_1}^\mu p_{j_2}^\rho + b_{j_1 j_2}^{(6)} g^{\rho\sigma} p_{j_1}^\mu p_{j_2}^\nu \right) \\
 &+ \sum_{j_1, j_2, j_3, j_4=1}^3 c_{j_1 j_2 j_3 j_4} p_{j_1}^\mu p_{j_2}^\nu p_{j_3}^\rho p_{j_4}^\sigma,
 \end{aligned}$$



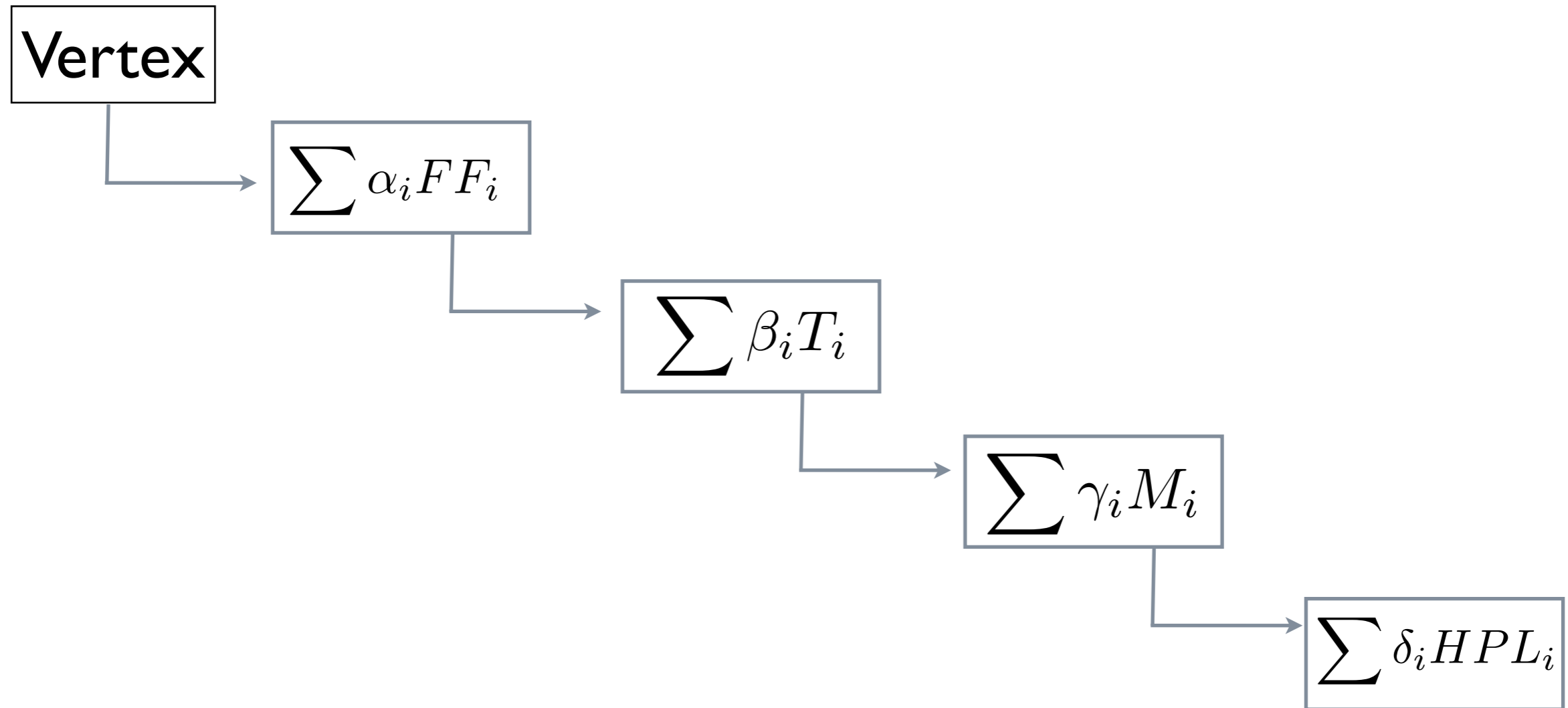
```

GGAA = Vertex(name = 'GGAA',
  particles = [ P.G, P.G, P.A, P.A ],
  color = [ 'Identity(1,2)' ],
  lorentz = [ L.A, L.B, L.C, L.D, L.E,
              L.F, L.G, L.H, L.I, L.J,
              L.K, L.L, L.M, L.N, L.O,
              L.P, L.Q, L.R, L.S, L.T
            ],
  couplings = {(0,0):C.GGAA_C1, (0,1):C.GGAA_C2, (0,2):C.GGAA_C3, (0,3):C.GGAA_C4, (0,4):C.GGAA_C5,
               (0,5):C.GGAA_C6, (0,6):C.GGAA_C7, (0,7):C.GGAA_C8, (0,8):C.GGAA_C9, (0,9):C.GGAA_C10,
               (0,10):C.GGAA_C11, (0,11):C.GGAA_C12, (0,12):C.GGAA_C13, (0,13):C.GGAA_C14, (0,14):C.GGAA_C15,
               (0,15):C.GGAA_C16, (0,16):C.GGAA_C17, (0,17):C.GGAA_C18, (0,18):C.GGAA_C19, (0,19):C.GGAA_C20
             })
  
```

- Allows a tool like MG5\_aMC to generate arbitrary 2-loop amplitudes containing this loop (with any decay or vector quantum numbers, but with still onshell gluons)

# BEYOND FORM FACTORS

- Push the idea further: extend the UFO format so as to further break-down the form factor into Topologies and scalar masters.



- UFO extension to accommodate the above?