

# scale setting for single jet and dijet inclusive cross sections

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# Single jet inclusive cross section

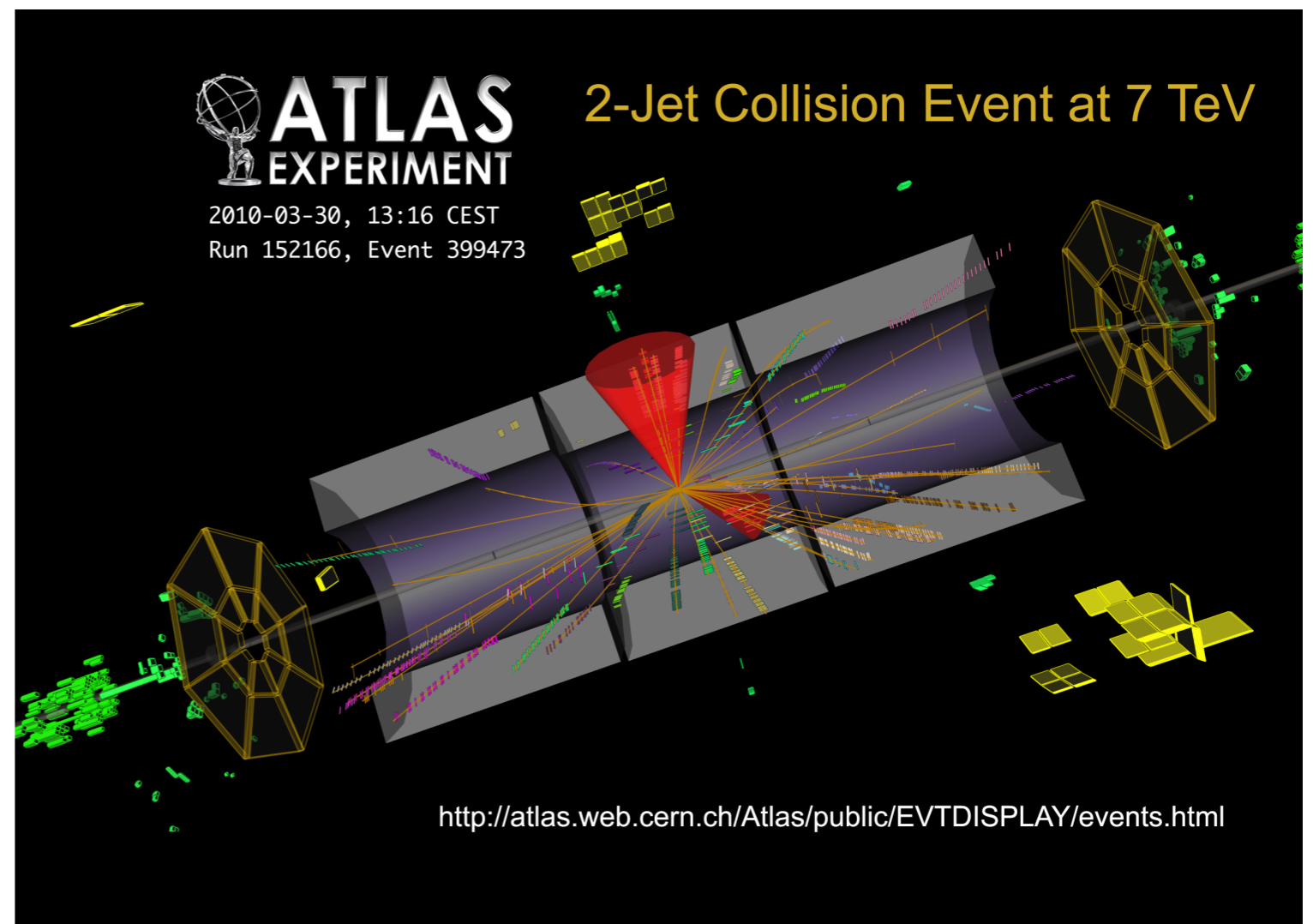
# ATLAS jets

## Theory setup

- NNPDF3.0\_nnlo
- anti- $k_T$  jet algorithm
- $p_{T\min} > 100 \text{ GeV}$  ;  $|y| < 3.0$
- $\mu_R = \mu_F = \{p_{T1}, p_T\}$
- vary scales by factors of 2 and 1/2

## Comparison to data

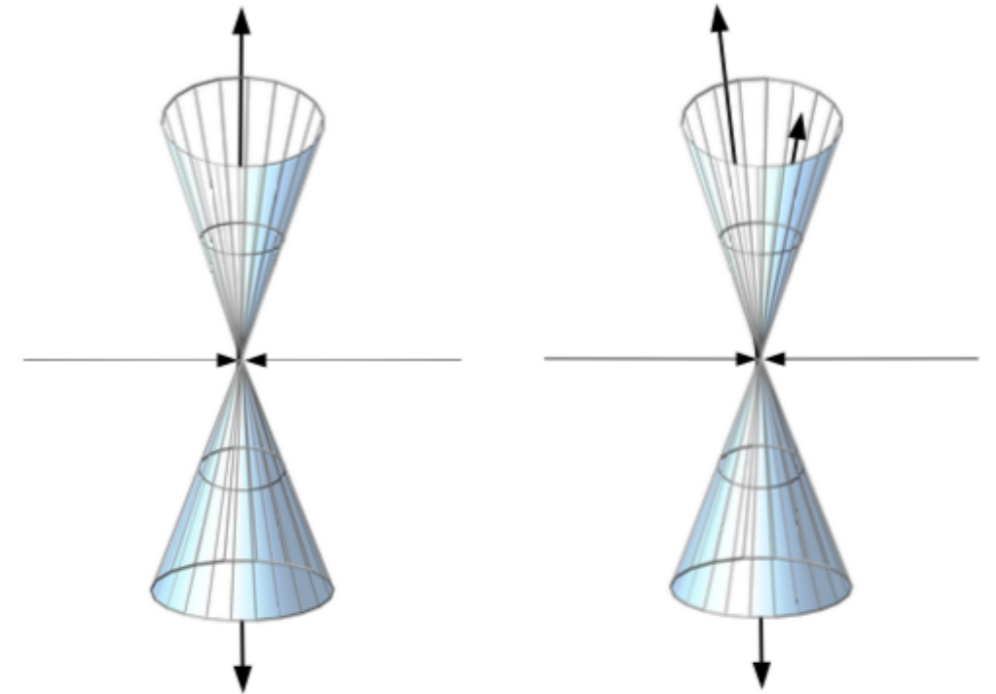
- ATLAS 7 TeV  $4.5 \text{ fb}^{-1}$
- $R=0.4$



# Single jet inclusive scale choice

two widely used scale choices:

- $\mu_R = \mu_F = \{p_{T1}, p_T\}$ 
  - leading jet  $p_T$  in the event  $p_{T1}$
  - individual jet  $p_T$
- high  $p_T$  jets are back to back  $\Rightarrow p_T \rightarrow p_{T1}$



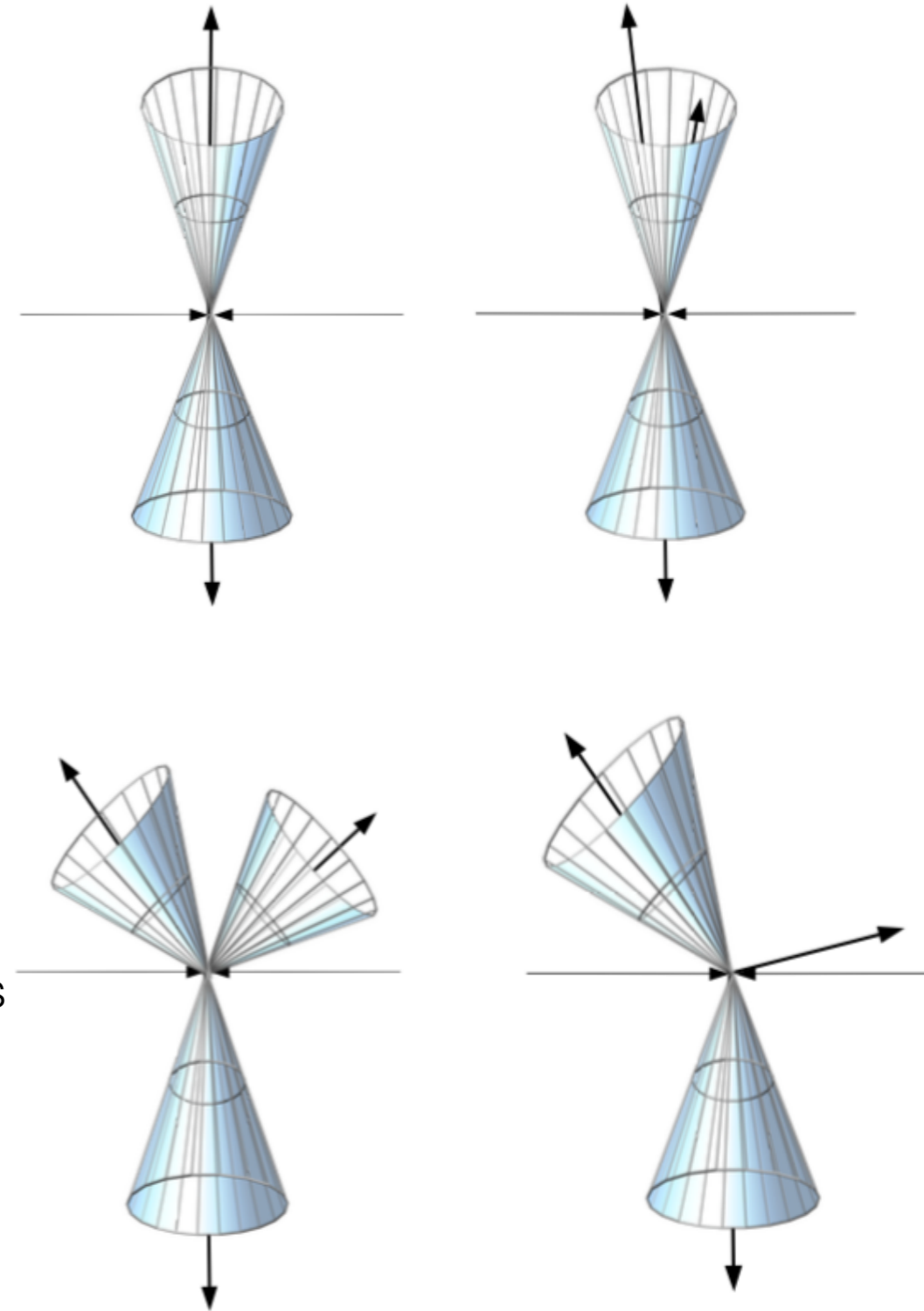
# Single jet inclusive scale choice

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  - leading jet  $p_T$  in the event  $p_{T1}$
  - individual jet  $p_T$
- high  $p_T$  jets are back to back  $\Rightarrow p_T \rightarrow p_{T1}$
- $p_T \neq p_{T1}$  for:
  - 3jet events
  - 3rd jet outside fiducial jet cuts

$\Rightarrow$  with  $p_T$  choice the real emission event with different  $R$  gives rise to a different scale  $\Rightarrow$  larger  $R \Rightarrow$  harder scale  $\Rightarrow p_T \rightarrow p_{T1}$ ; value of the scale depends on  $R$

- at NLO the  $p_{T1}$  scale choice generates the same hard scale for the event independent of the value of  $R$
- at NNLO for the first time  $p_{T1}$  scale depends on the value of  $R$

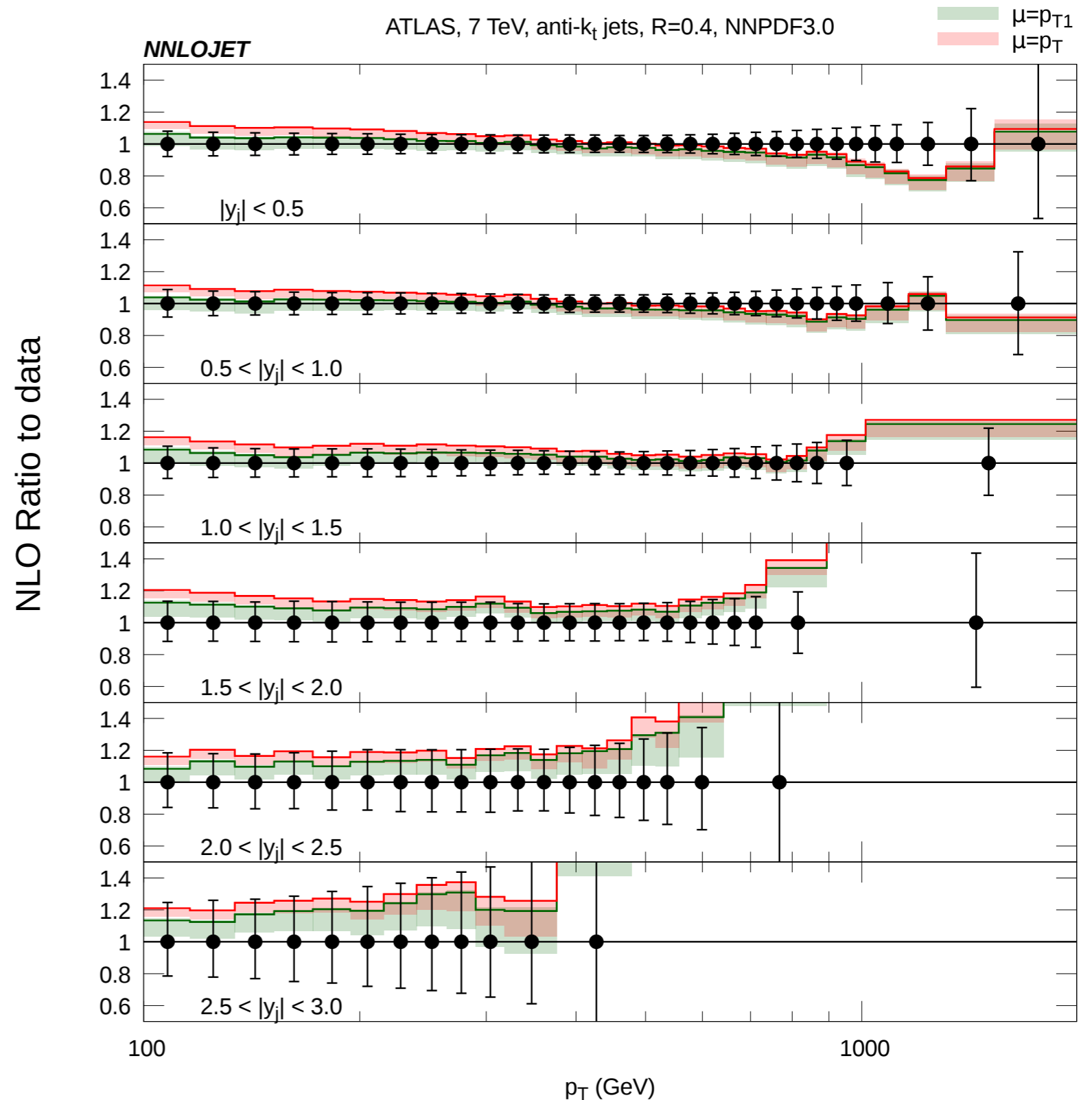


## Ratio to NLO

- asymmetric scale band variation
- underestimated at small  $p_T$  due to turn over of the NLO coefficient
- 20% uncertainty for central high  $p_T$  jets rising to 40% for forward jets

## Comparison to data

- non perturbative effects  $< 2\%$  effect [JHEP 1509, 141 (2015)]
- data favours the  $p_{T1}$  scale choice at NLO

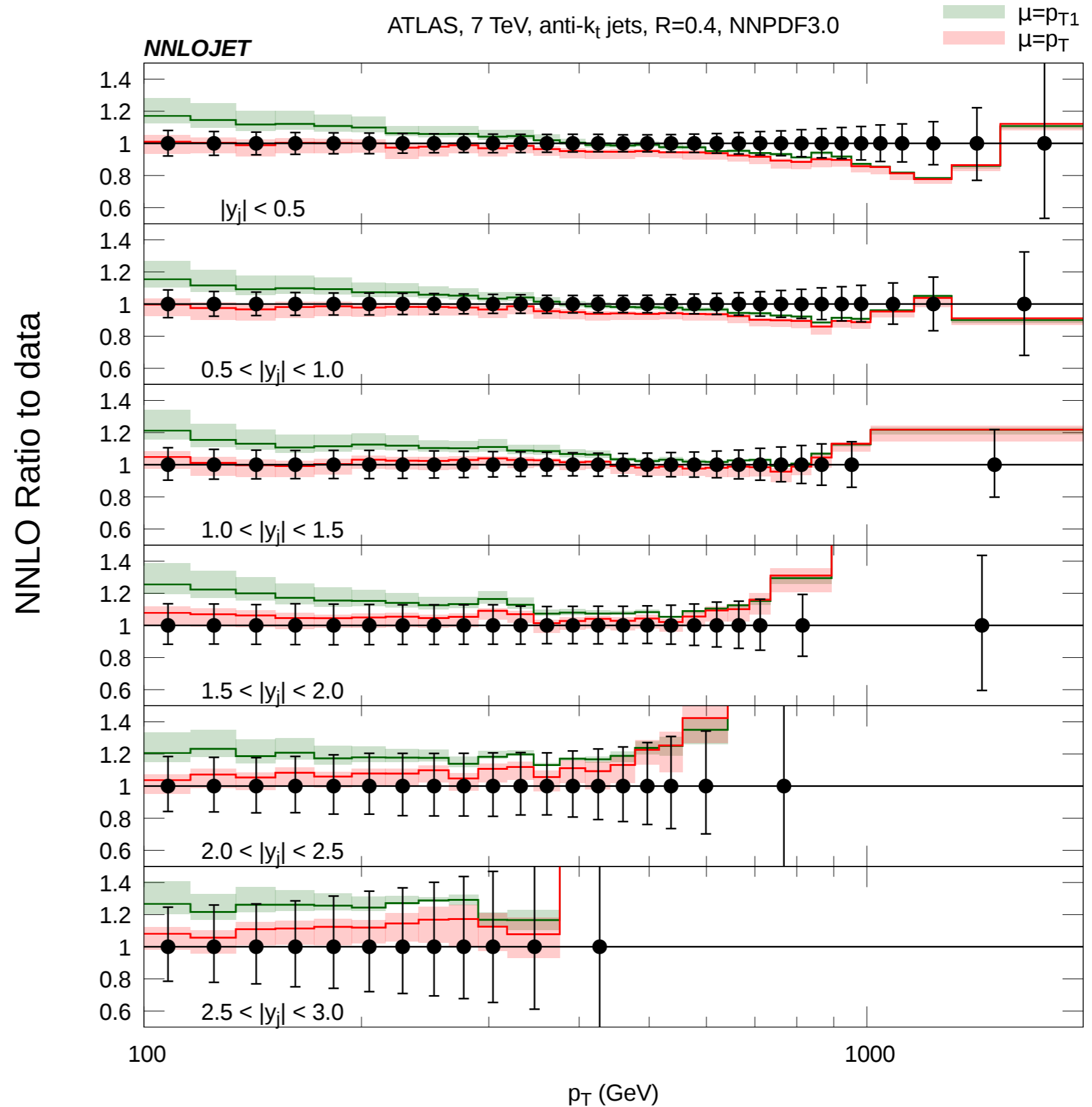


## Ratio to NNLO

- symmetric scale band variation
- $p_{T1} \neq p_T$  effects enlarged at NNLO
- 10% scale uncertainty at low  $p_T$  and percent level scale uncertainty at high  $p_T$

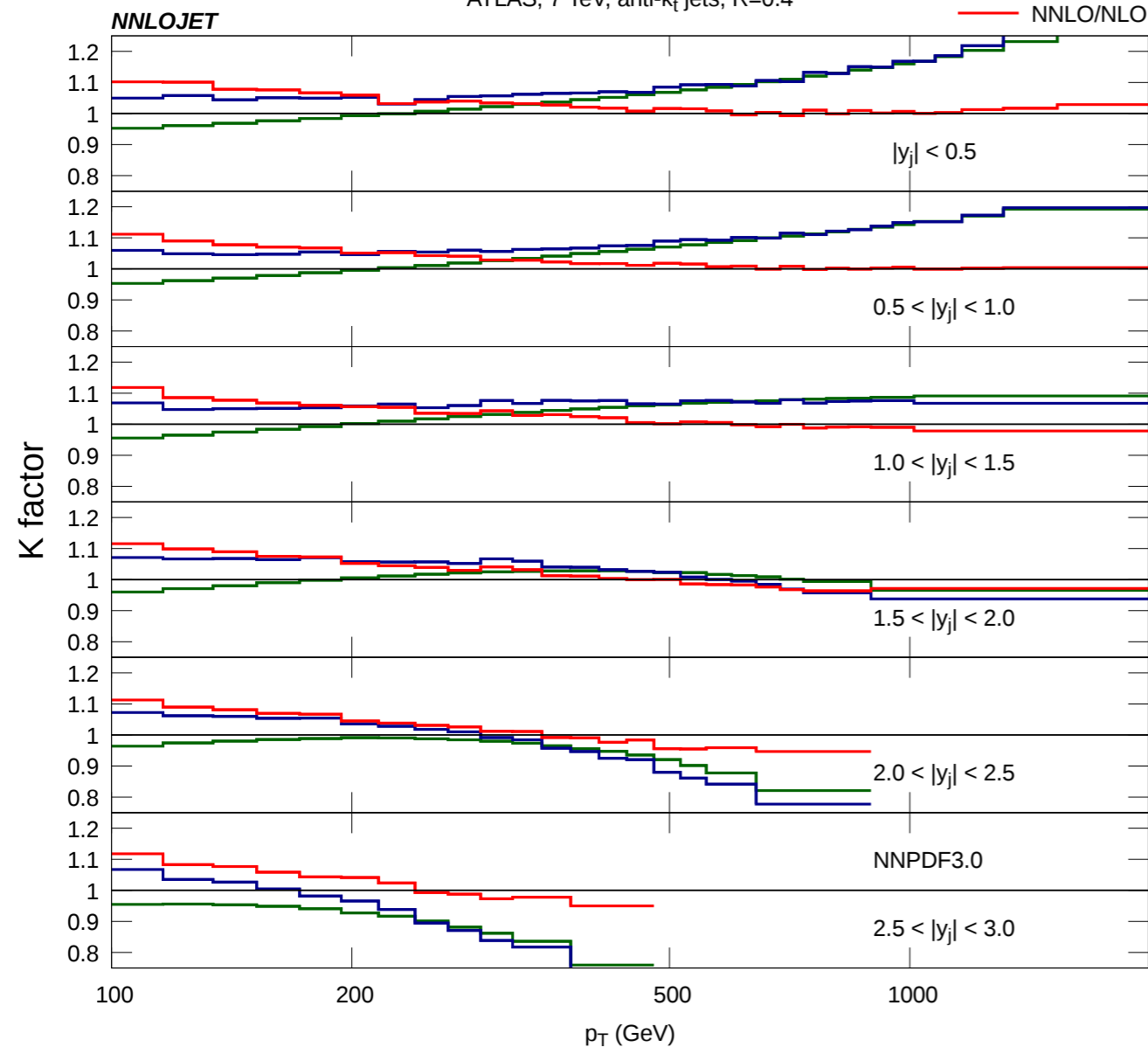
## Comparison to data

- data favours the  $p_T$  scale choice at NNLO



ATLAS, 7 TeV, anti- $k_t$  jets, R=0.4

NLO/LO  
 NNLO/LO  
 NNLO/NLO

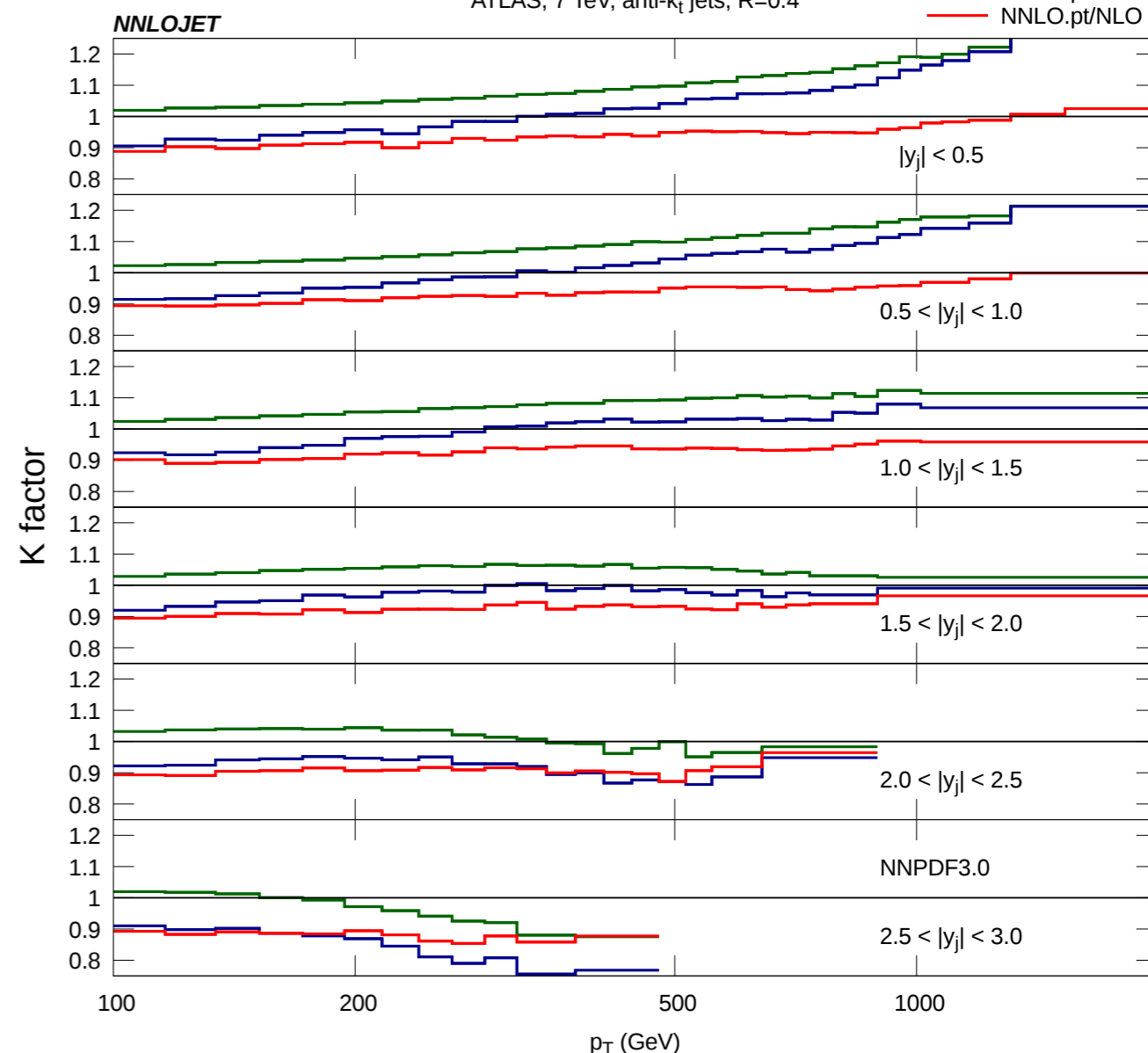


$$\mu_R = \mu_F = p_{T1}$$

- NNLO effects around +10% at low  $p_T$  and small at high  $p_T$
- Shape of NNLO/NLO k-factor is getting steeper going to the forward rapidity slices
- Scale choice has a potential interplay with consistent fit of jet data in PDF's for all rapidity slices
- two commonly used scale choices show no evident instability in the respective perturbative expansion

ATLAS, 7 TeV, anti- $k_t$  jets, R=0.4

NLO.pt/LO  
 NNLO.pt/LO  
 NNLO.pt/NLO

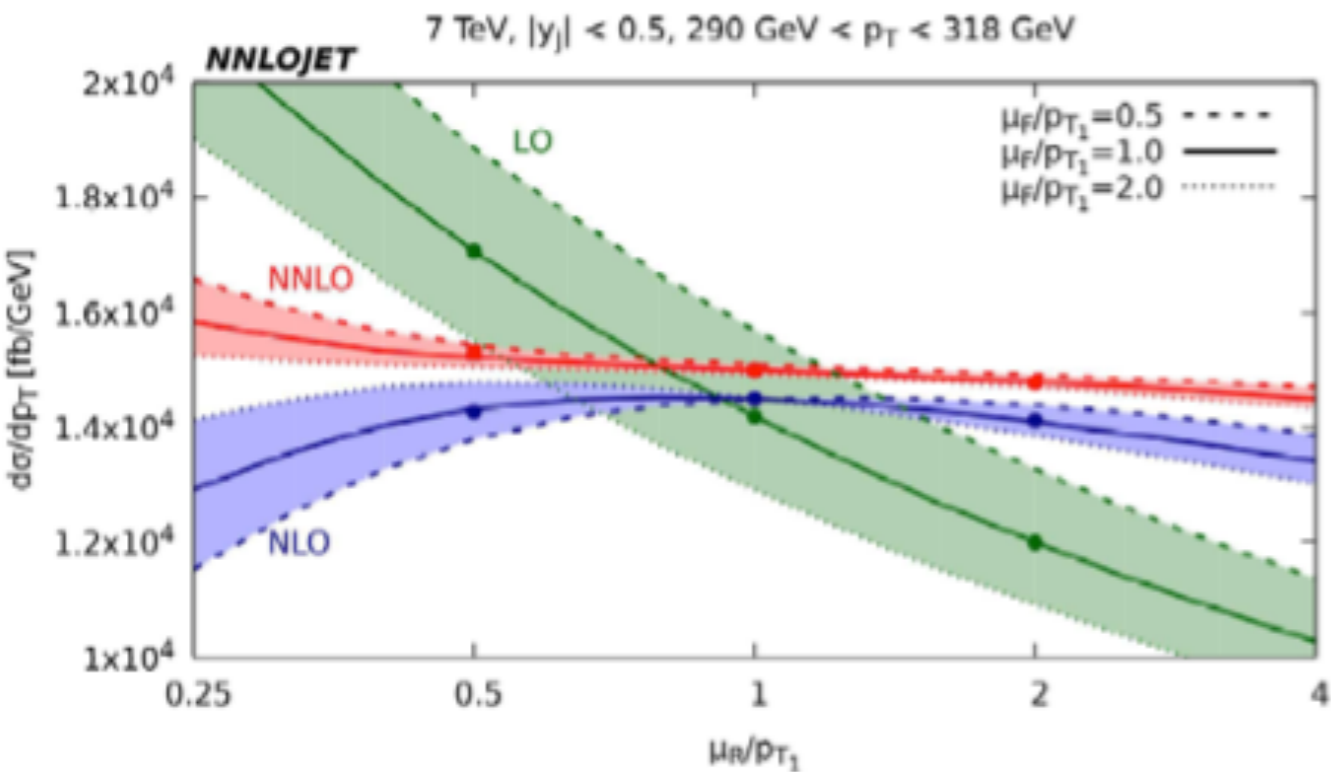


$$\mu_R = \mu_F = p_T$$

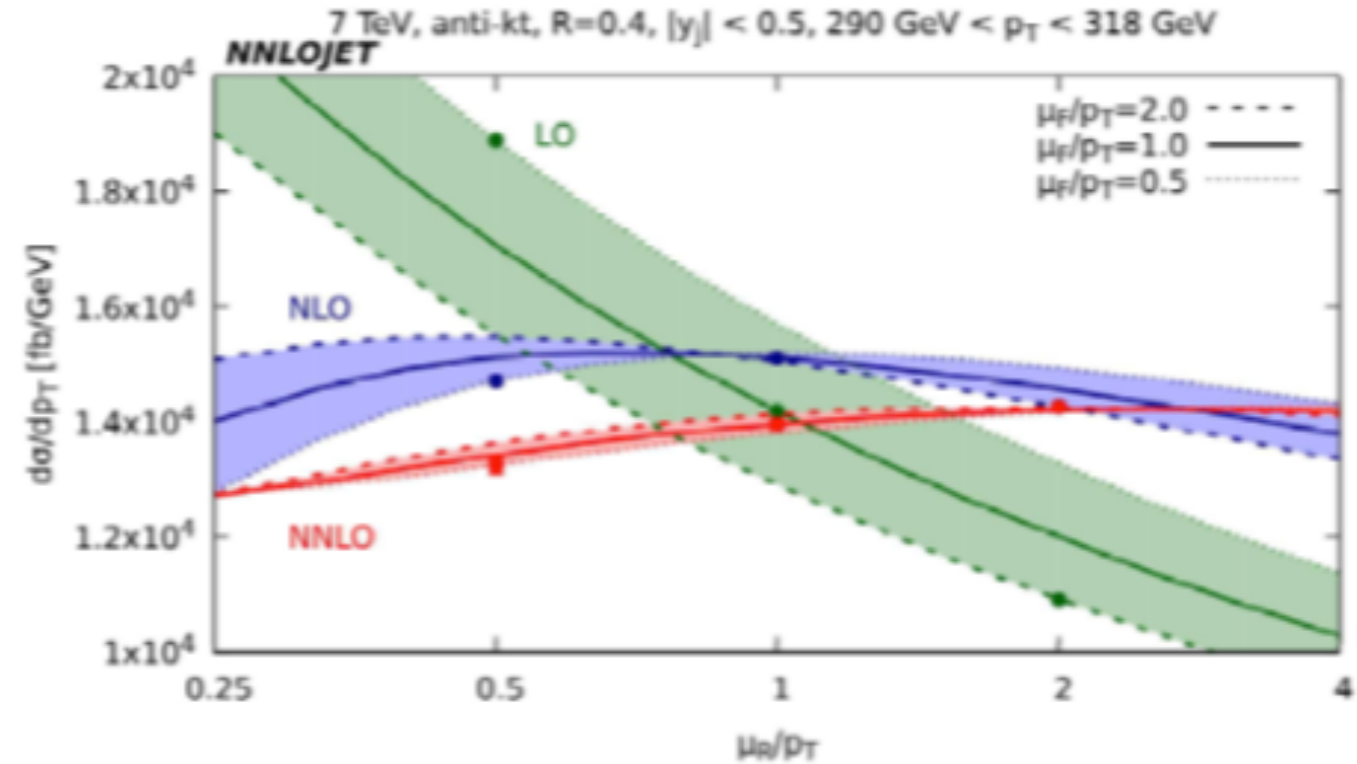
- NNLO effects around -10% at low  $p_T$  and small at high  $p_T$
- Shape of NNLO/NLO k-factor is getting flatter going to the forward rapidity slices



# Scale variation



$$\mu_R = \mu_F = p_{T1}$$



$$\mu_R = \mu_F = p_T$$

- Different behaviour in the NNLO scale variation
- Scale uncertainty much smaller than the difference between the two scale choices
- Difference in the prediction with either scale choice is beyond the scale variation uncertainty
- Lack of a theoretically well motivated preference motivates further study of this issue

## K-factor plot

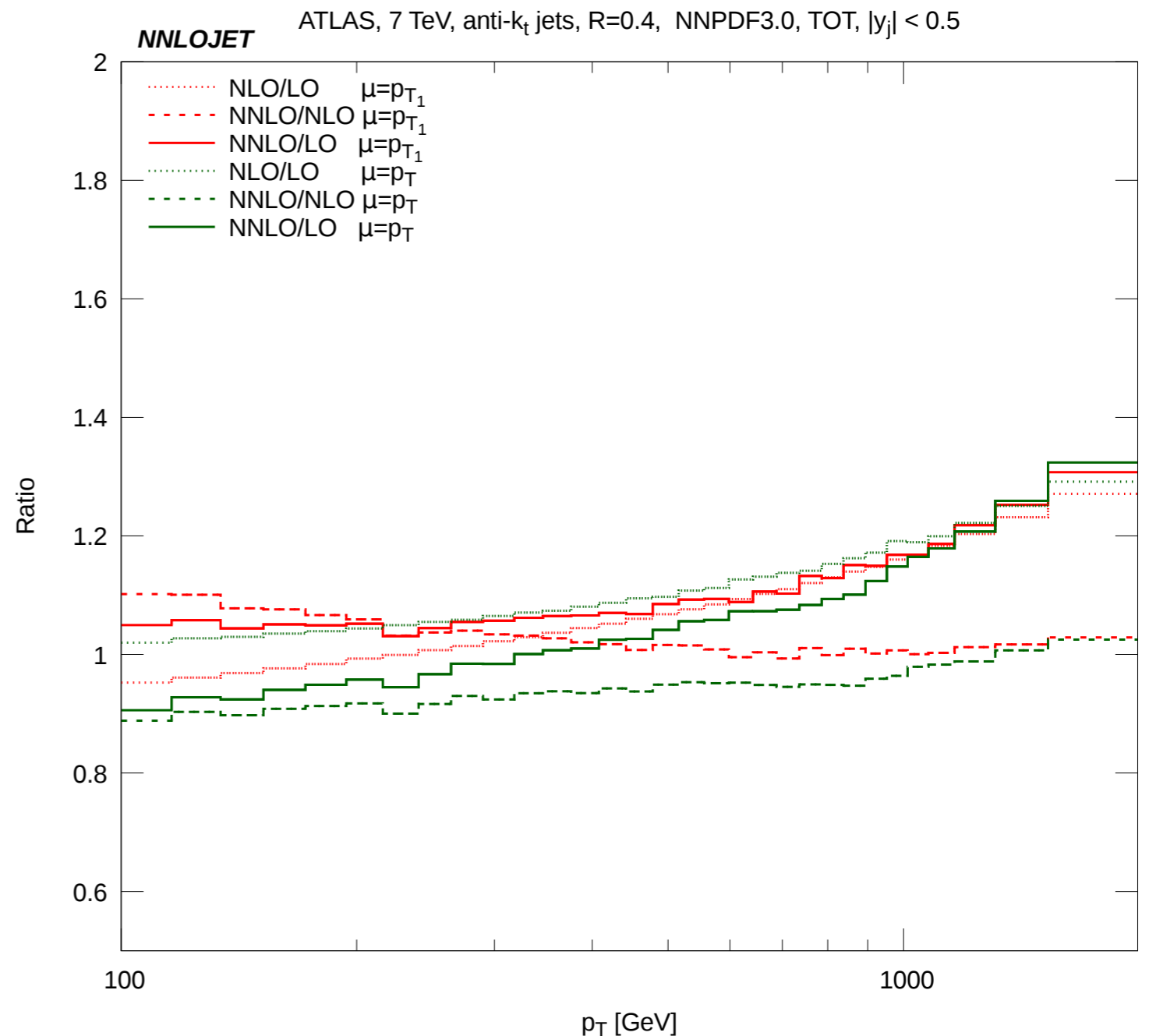
- $p_{T1} \neq p_T$  effects enlarged at NNLO at low  $p_T$ 
  - decrease for larger  $R$  values

Sensible criteria for scale choice for single jet inclusive production

- perturbative stability
- data driven scale choice

## Future steps

- compare with CMS jet data; change  $R$  value ; change  $\sqrt{s}$
- Obtain consistent description of jet data at NNLO for all jet data sets at low and high  $p_T$  in the central and forward regions for multiple  $R$  values

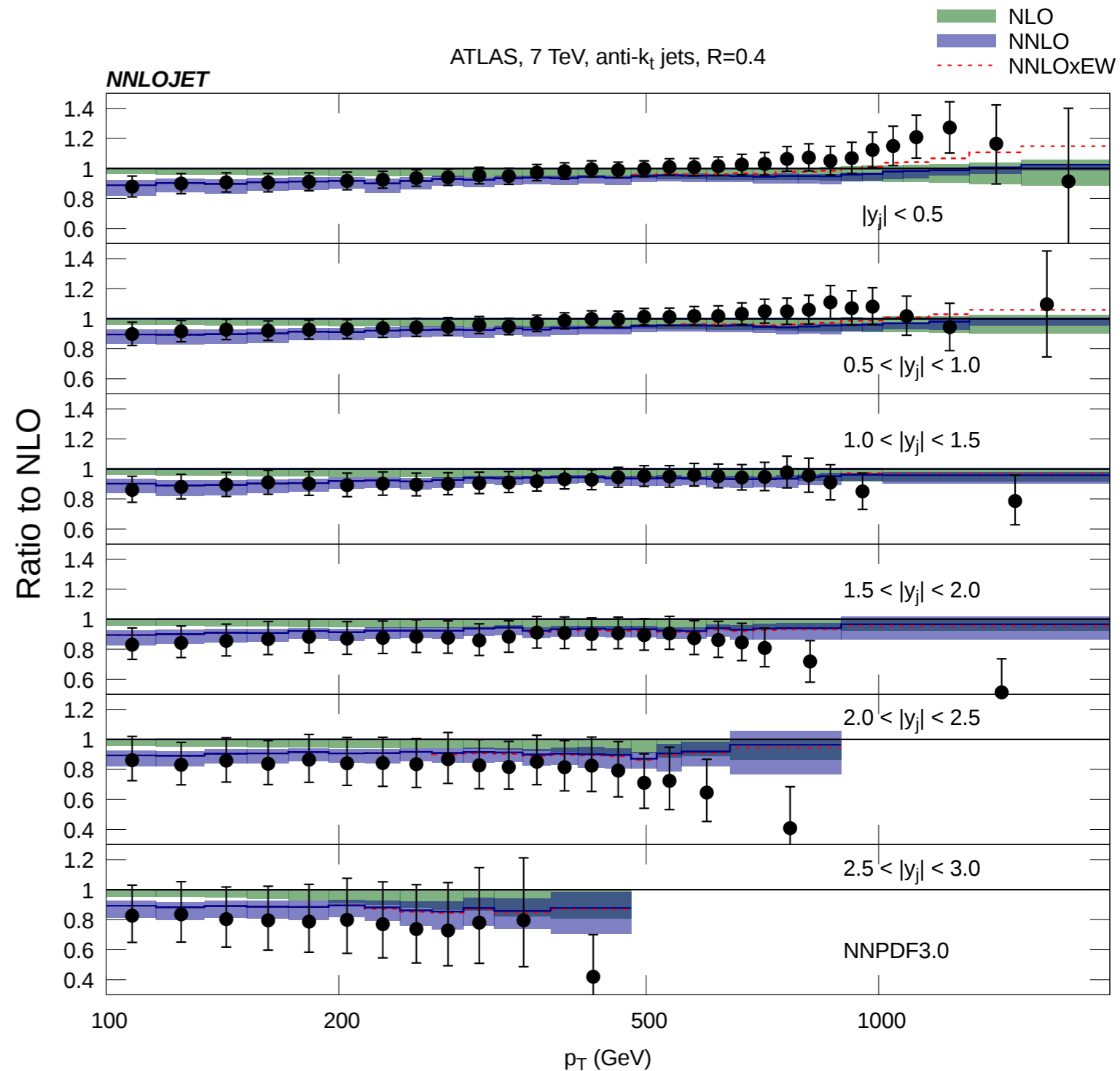


## K-factor plot

- $p_{T1} \neq p_T$  effects enlarged at NNLO at low  $p_T$
  - decrease for larger R values
- Sensible criteria for scale choice for single jet inclusive production
- perturbative stability
  - data driven scale choice

## Future steps

- compare with CMS jet data; change R value ; change  $\sqrt{s}$
- For ATLAS 7 TeV R=0.4 data NNLO QCD + NLO EW prediction with  $p_T$  scale choice gives the best description of the jet data



Dijet inclusive cross section

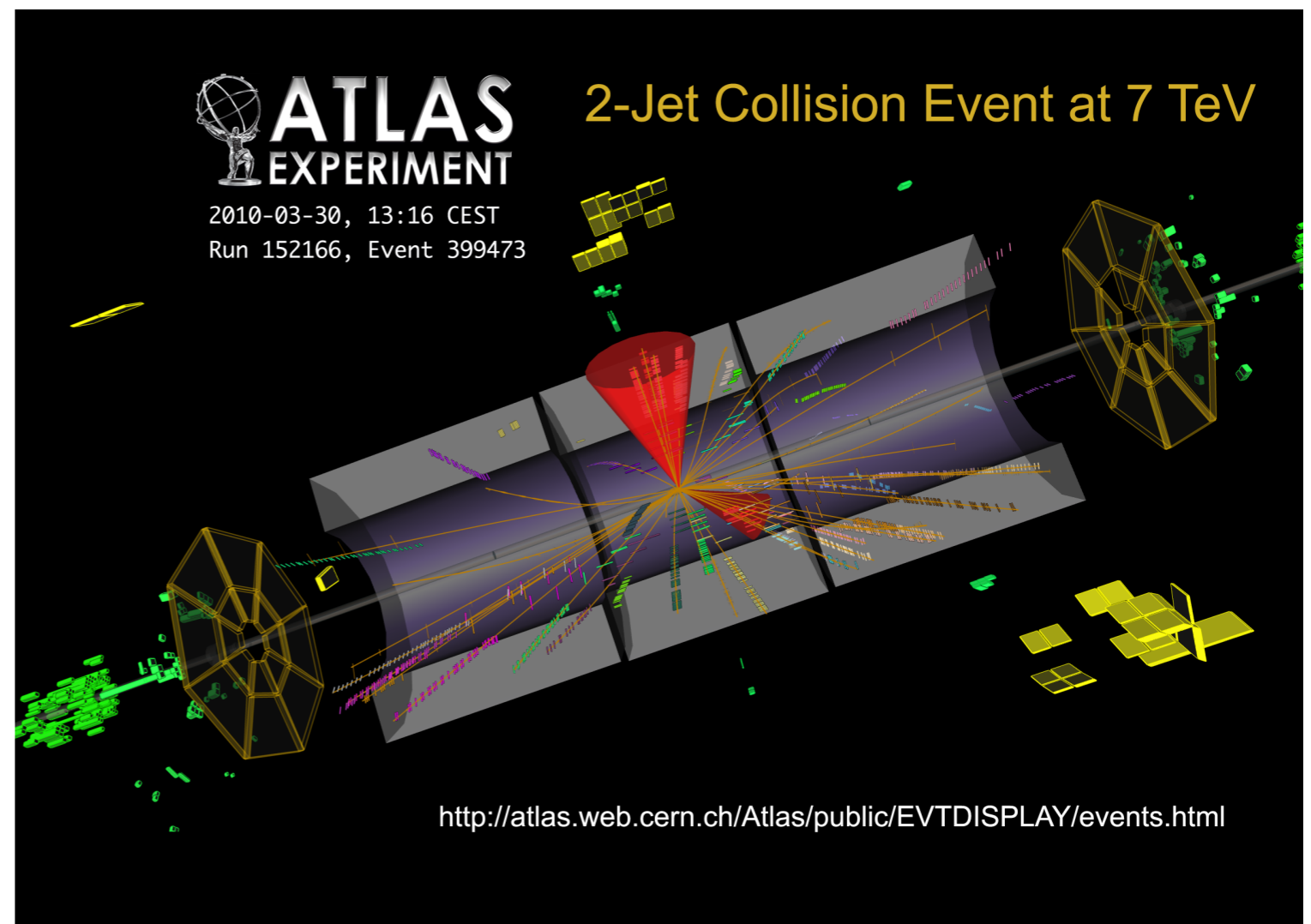
# ATLAS jets

## Theory setup

- MMHT2014 nnlo
- anti- $k_T$  jet algorithm
- $p_{T1} > 100$  GeV;  $p_{T2} > 50$  GeV;
- $|y_{j1}|, |y_{j2}| < 3.0$
- $\mu_R = \mu_F = \{m_{jj}, \langle p_T \rangle\}$
- vary scales by factors of 2 and 1/2

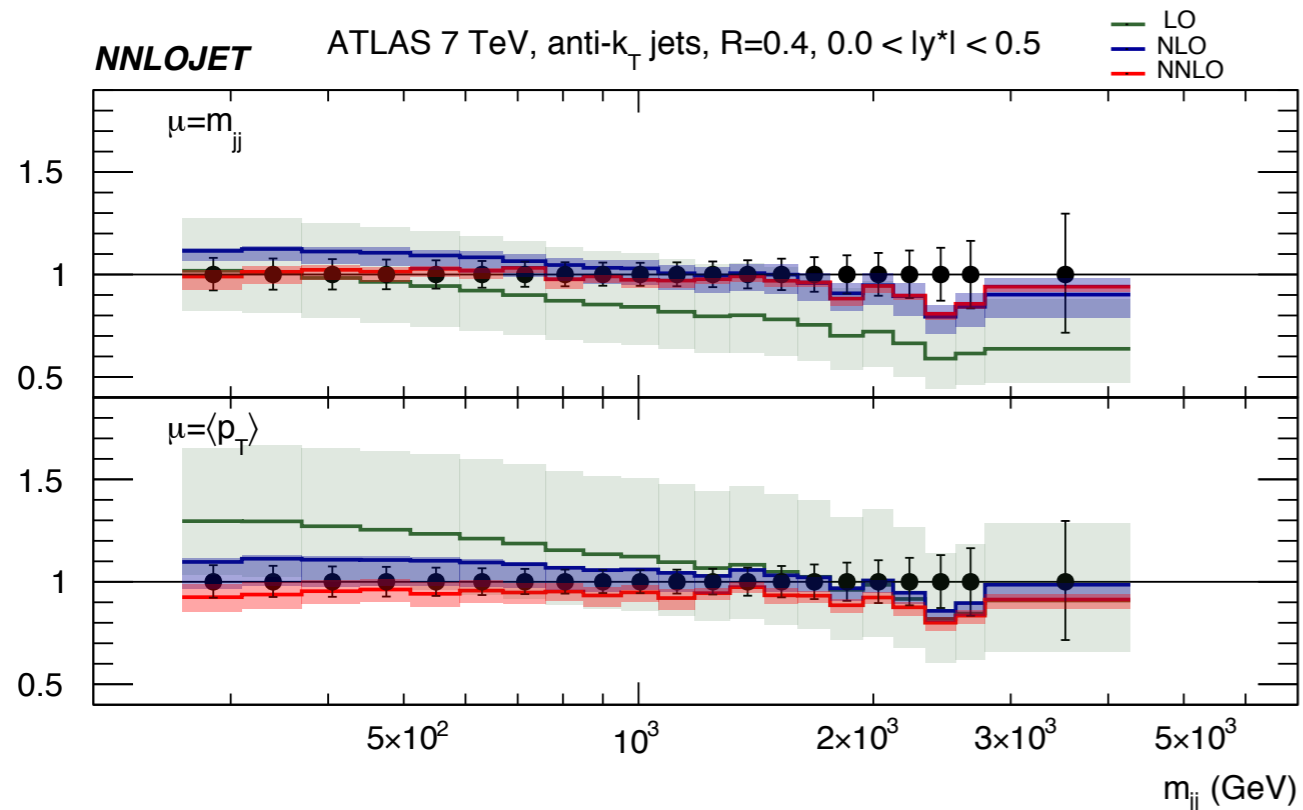
## Comparison to data

- ATLAS 7 TeV  $4.5 \text{ fb}^{-1}$
- $R=0.4$

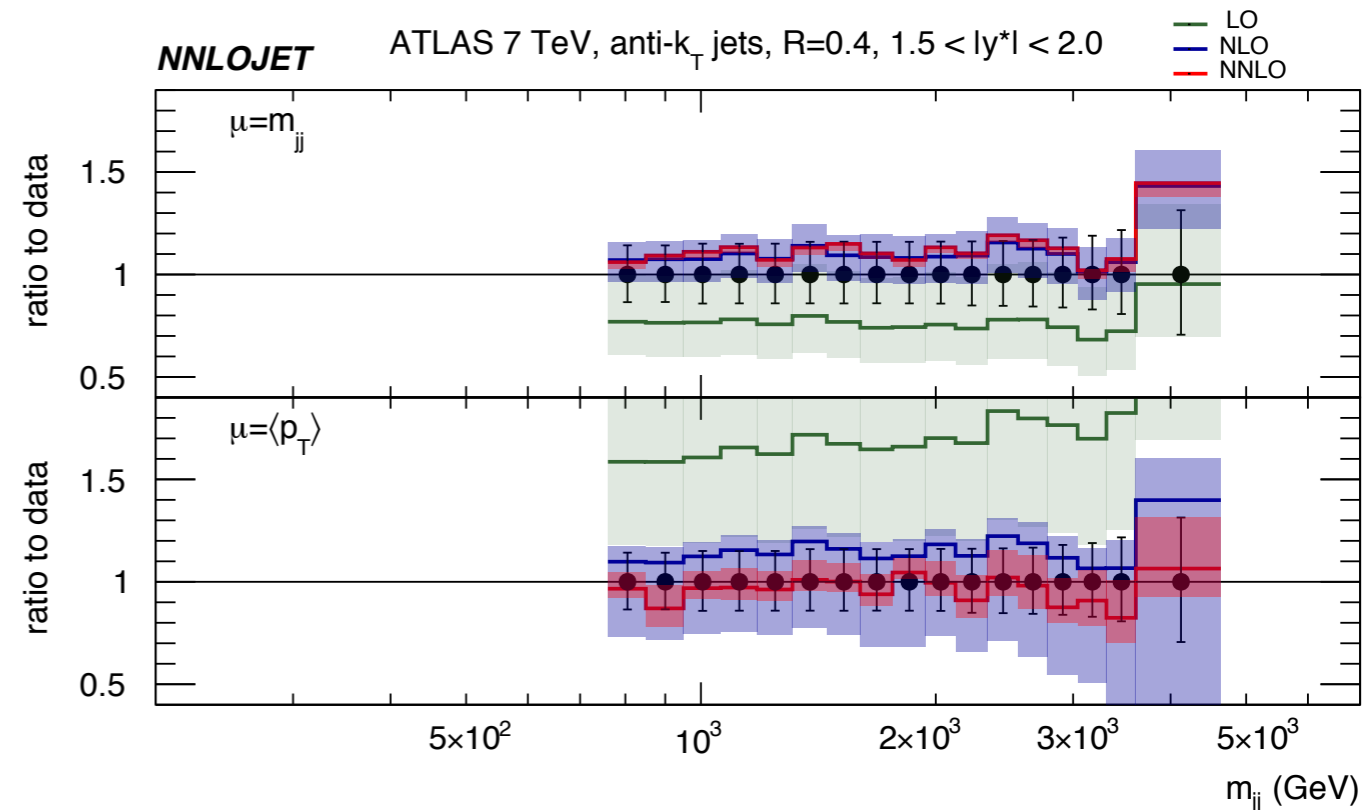


$$m_{jj}^2 = (p_{j1} + p_{j2})^2$$

$$y^* = \frac{1}{2}(y_{j1} - y_{j2})$$

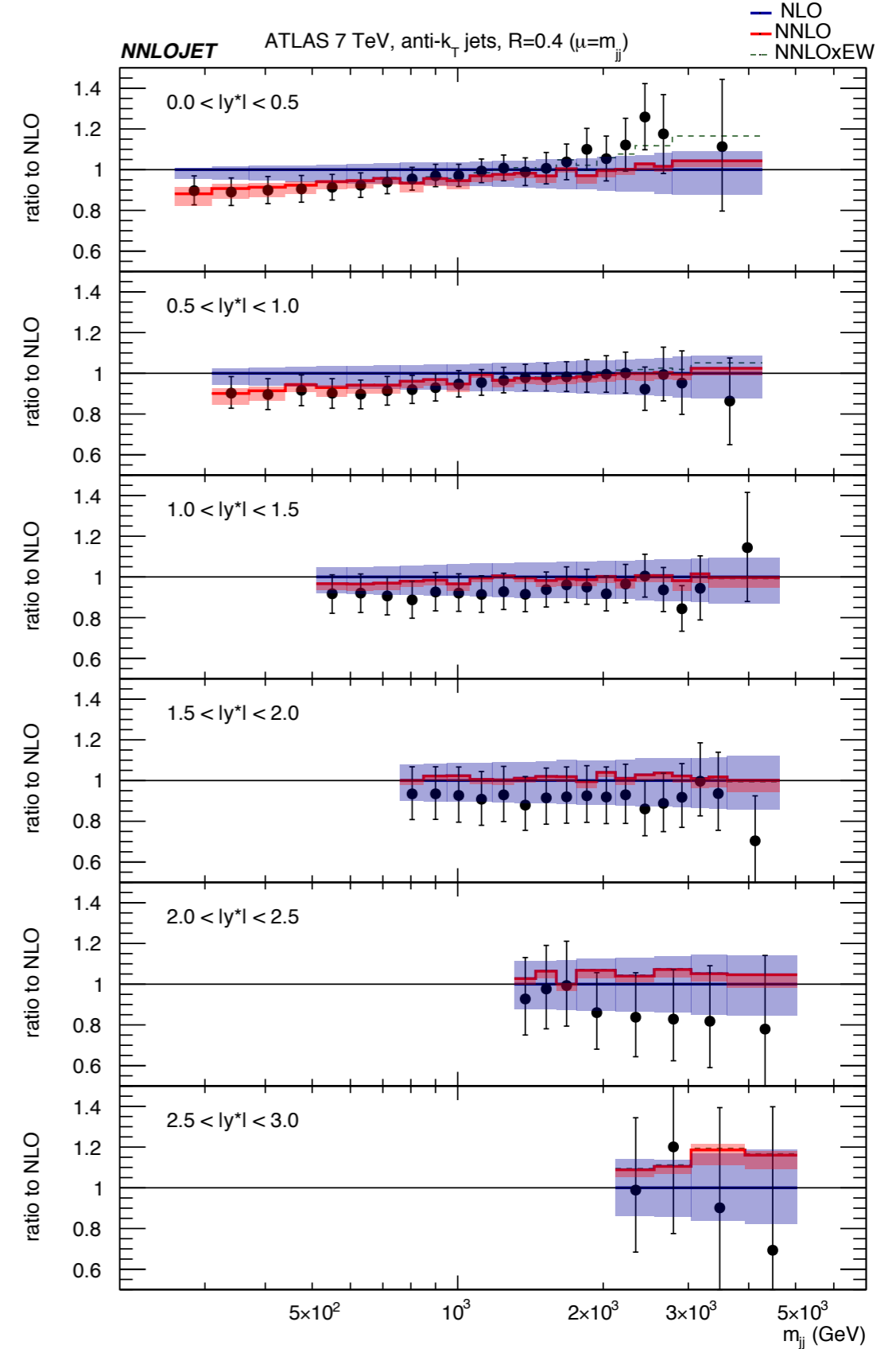
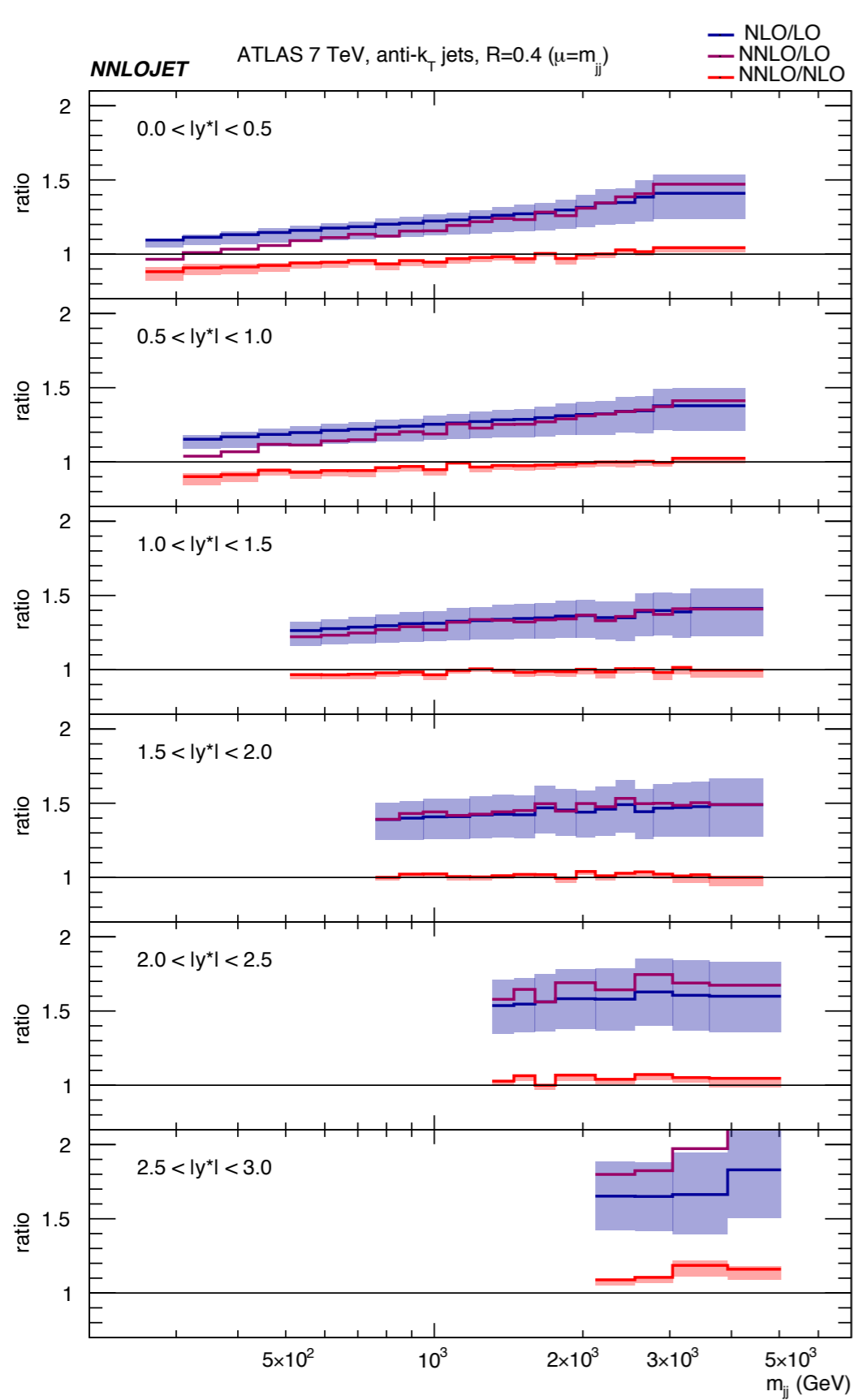


$$0.0 < |y^*| < 0.5$$



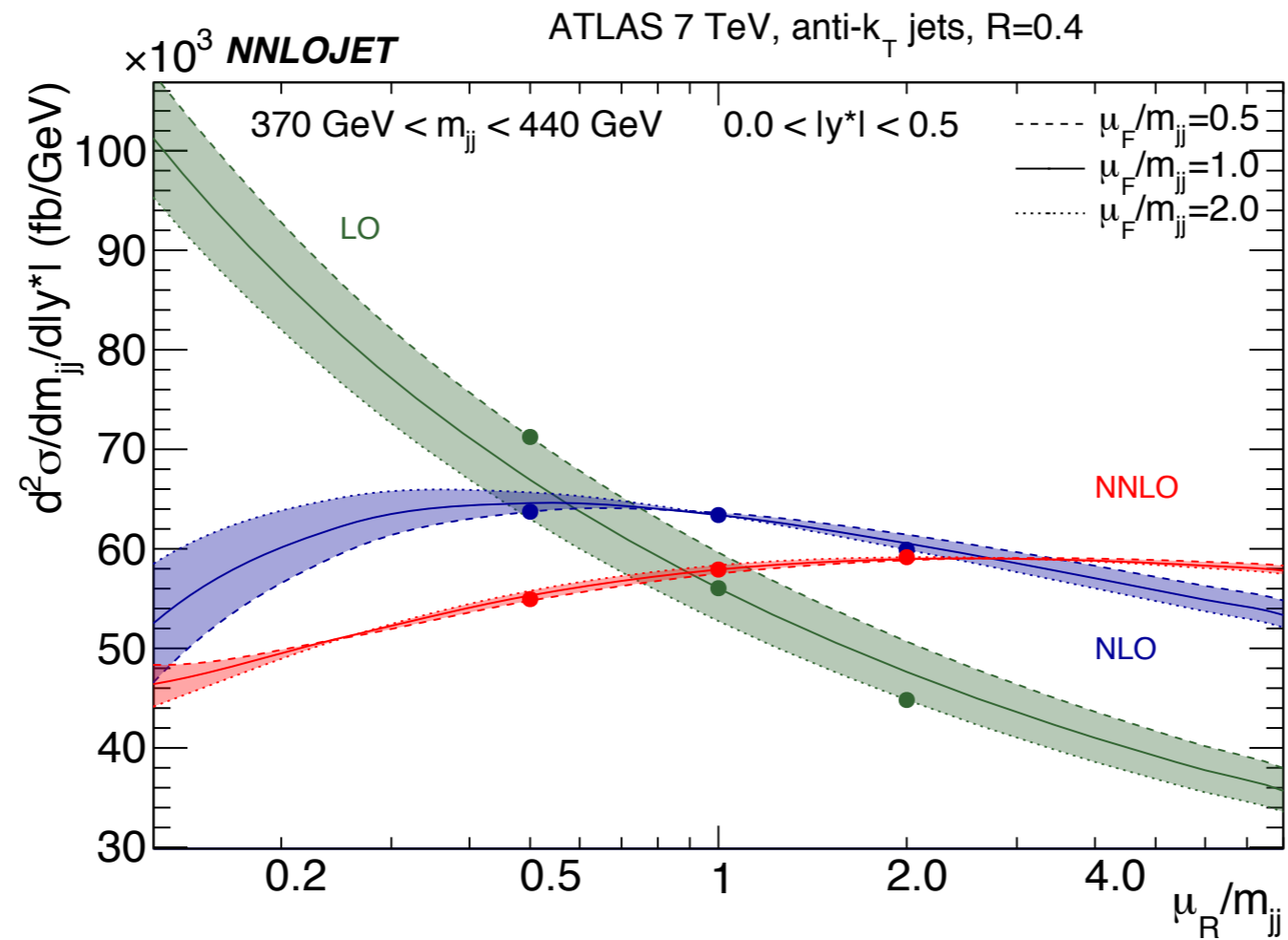
$$1.5 < |y^*| < 2.0$$

- Largely overlapping scale bands at small  $y^*$  with either scale choice
- At large  $y^*$  we observe with  $\mu = \langle P_T \rangle$  large negative NLO corrections, non-overlapping scale bands and residual NLO, NNLO scale uncertainty of  $\sim 100\%$ ,  $\sim 20\%$
- Good theoretical motivation to use  $\mu = m_{jj}$  as central scale choice



- Excellent convergence of the perturbative expansion; NNLO/NLO < 10% and flat
- Improved description of the dijet data at NNLO

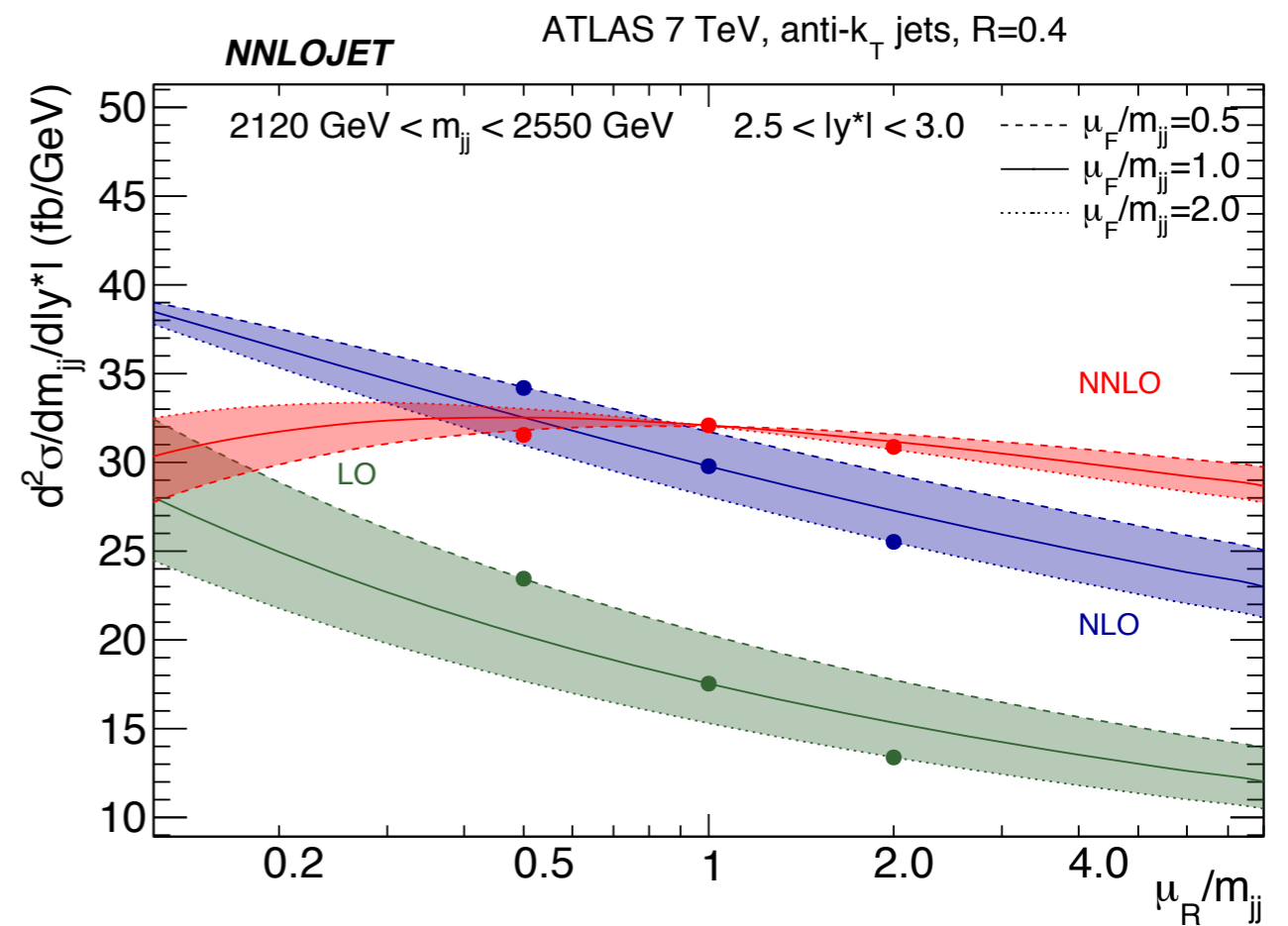
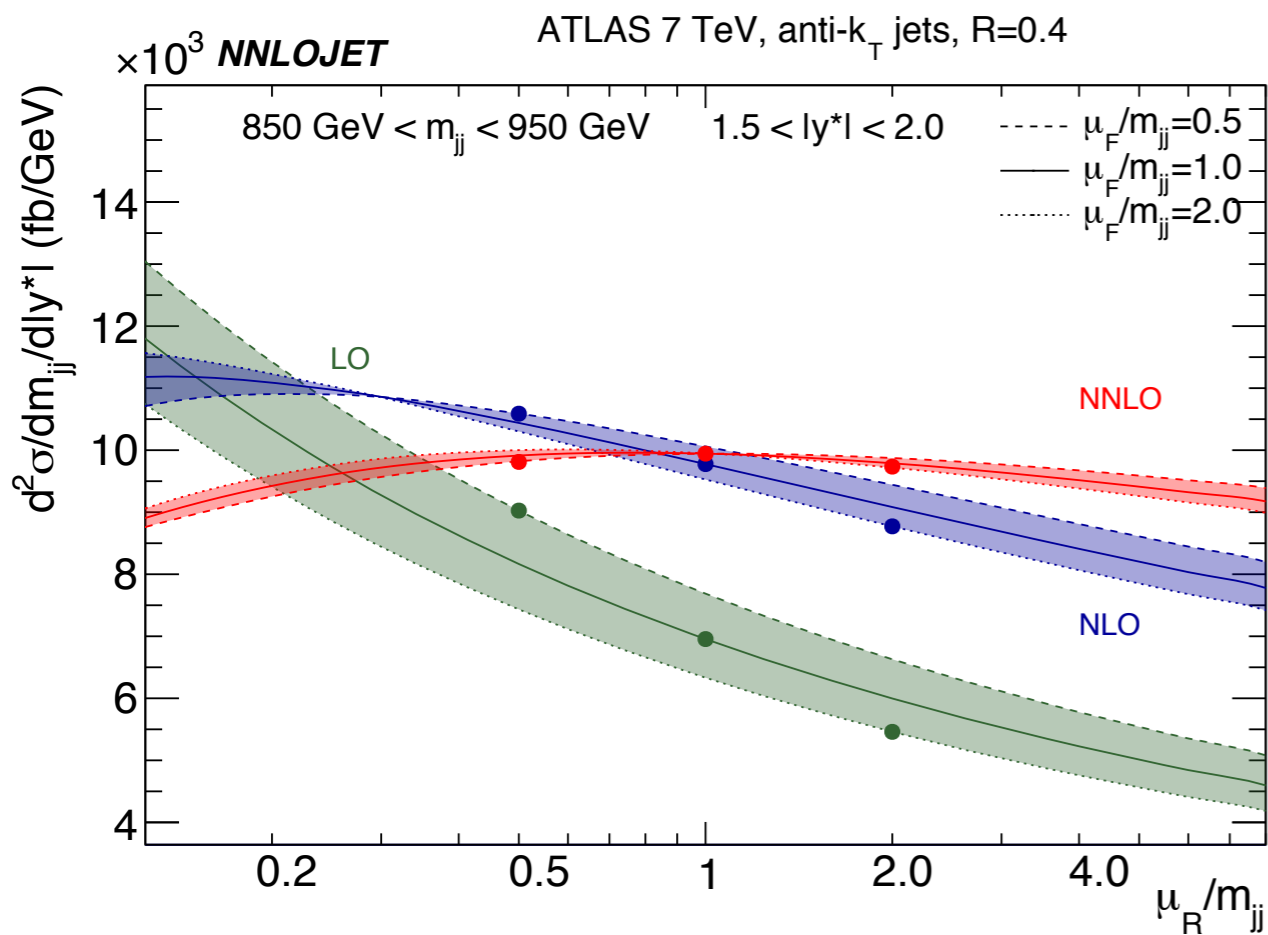
# Scale variation



- at low  $m_{jj}$  and  $|y^*|$  NNLO band of similar size as the NLO band
- central scale choice  $\mu=m_{jj}$  lies close to extremum of the NLO curve
- variation in  $\mu_R$ ,  $\mu_F$  accidentally minimised
- NLO band underestimates the missing higher order uncertainty



# Scale variation



- More reliable NLO scale variation and overlapping NLO and NNLO scale bands
- Significant reduction in scale dependence of the prediction at NNLO
- Residual scale uncertainty <5% smaller than experimental uncertainty on the observable

# Conclusions

## Single jet inclusive cross section

- two commonly used scale choices ( $p_T, p_{T1}$ ) show no evident instability in the respective perturbative expansion or significant differences in the residual scale dependence
- central value of the cross section at low  $p_T$  is significantly different at NNLO (outside the NNLO scale band variation) between the two scale choices, difference increased with respect to NLO
- at large  $p_T$  scale choices converge to the same result as expected

## Dijet inclusive invariant mass cross section

- central value of the NNLO cross section using  $p_{T\_AVG}$  or  $m_{jj}$  is similar
- $p_{T\_AVG}$  scale choice shows non-overlapping LO and NLO scale bands, slower convergence of the perturbative expansion and fairly large residual scale variation at large  $|y^*|$  the opposite of the  $m_{jj}$  scale choice
- Good theoretical motivation to use  $\mu = m_{jj}$  as central scale choice