

# Higgs TH Tools

Daniel de Florian  
Universidad de Buenos Aires - Argentina

**Les Houches 2013**



# *Outline*

- ① The shortest introduction about Higgs Boson Physics

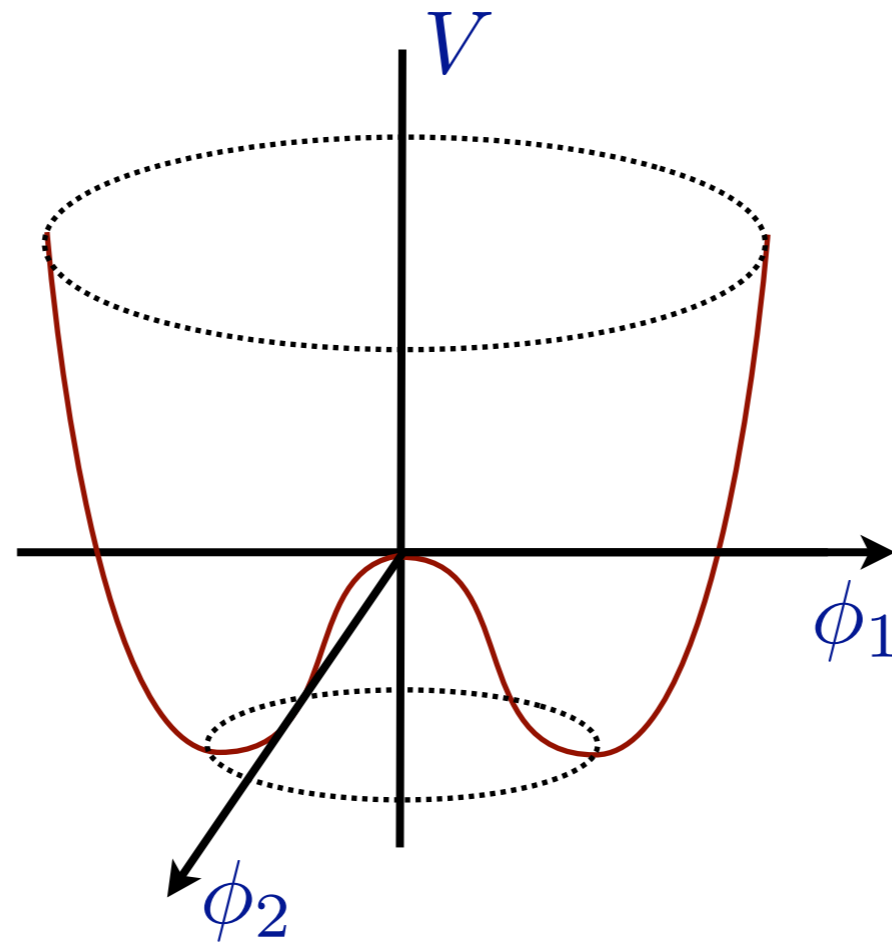
- ② Summary of production cross-sections

where is room/possibility/need for improvements

- ③ Decay and Interferences

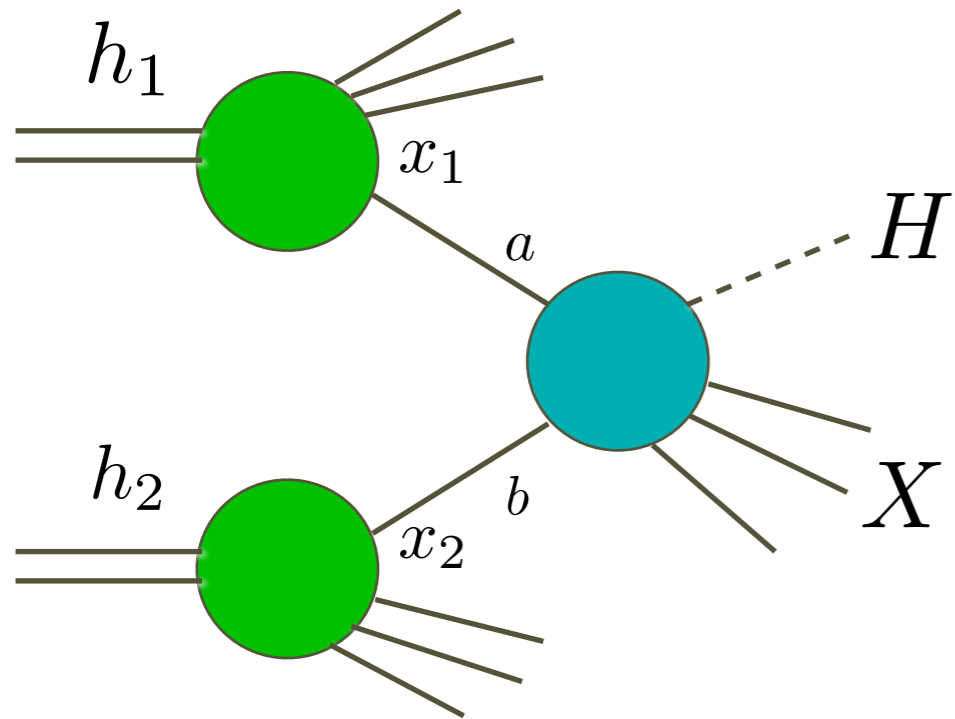
● The shortest introduction about Higgs Boson Physics

The SM Higgs boson is responsible for EW symmetry breaking



End of introduction

# Higgs at Hadronic Colliders



non-perturbative parton distributions

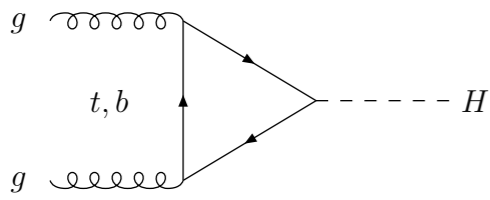
$$d\sigma = \sum_{ab} \int dx_a \int dx_b f_a(x_a, \mu_F^2) f_b(x_b, \mu_F^2) \times d\hat{\sigma}_{ab}(x_a, x_b, Q^2, \alpha_s(\mu_R^2))$$

perturbative partonic cross-section

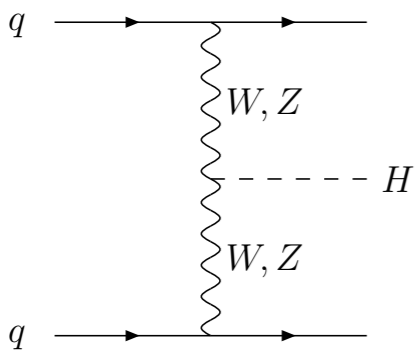
Partonic cross-section: expansion in  $\alpha_s(\mu_R^2) \ll 1$   $d\hat{\sigma} = \alpha_s^n d\hat{\sigma}^{(0)} + \alpha_s^{n+1} d\hat{\sigma}^{(1)} + \dots$

● Need precision for both PDFs and partonic cross sections

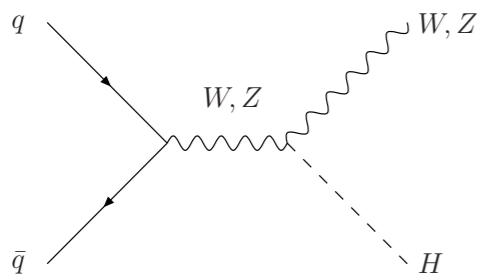
# Production Channels at the LHC



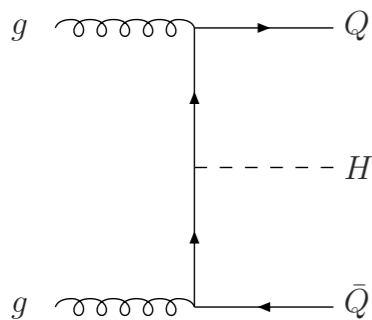
**gg fusion**



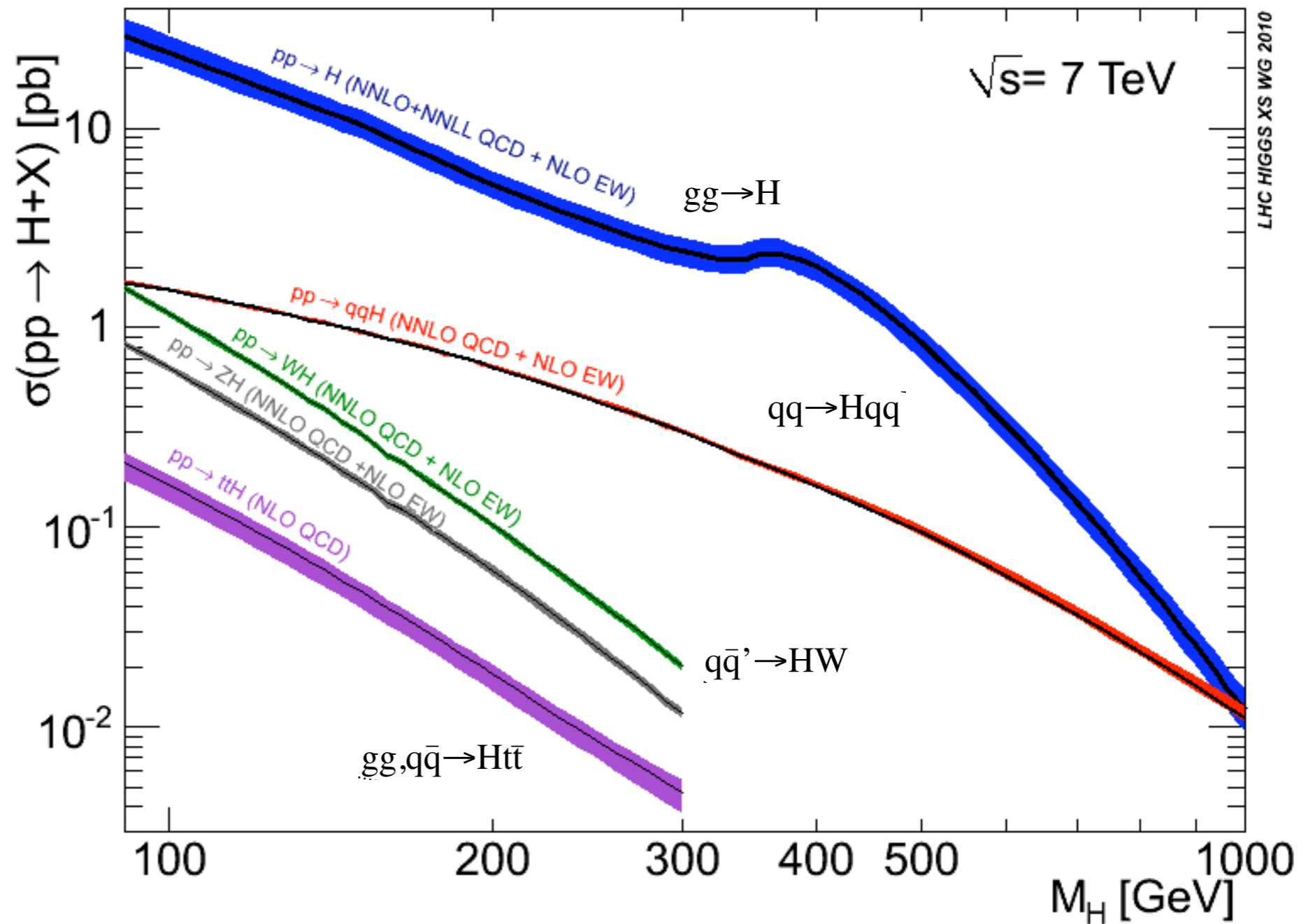
**vector boson fusion**



**associated production with W,Z**

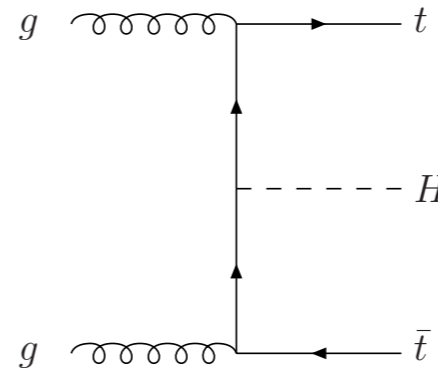
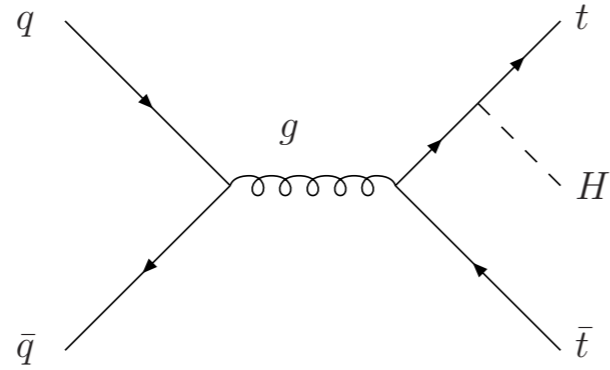


**associated production with heavy quarks**



● Gluon-gluon fusion dominates due to large gluon luminosity

# Heavy Quark Associated production



$t\bar{t}H$   
Yukawa  
coupling

- It was considered an important discovery channel in low mass region
- Not an easy channel because of background and signature



boosted analysis

Plehn, Salam, Spannowsky (2009)

LO known for a long time

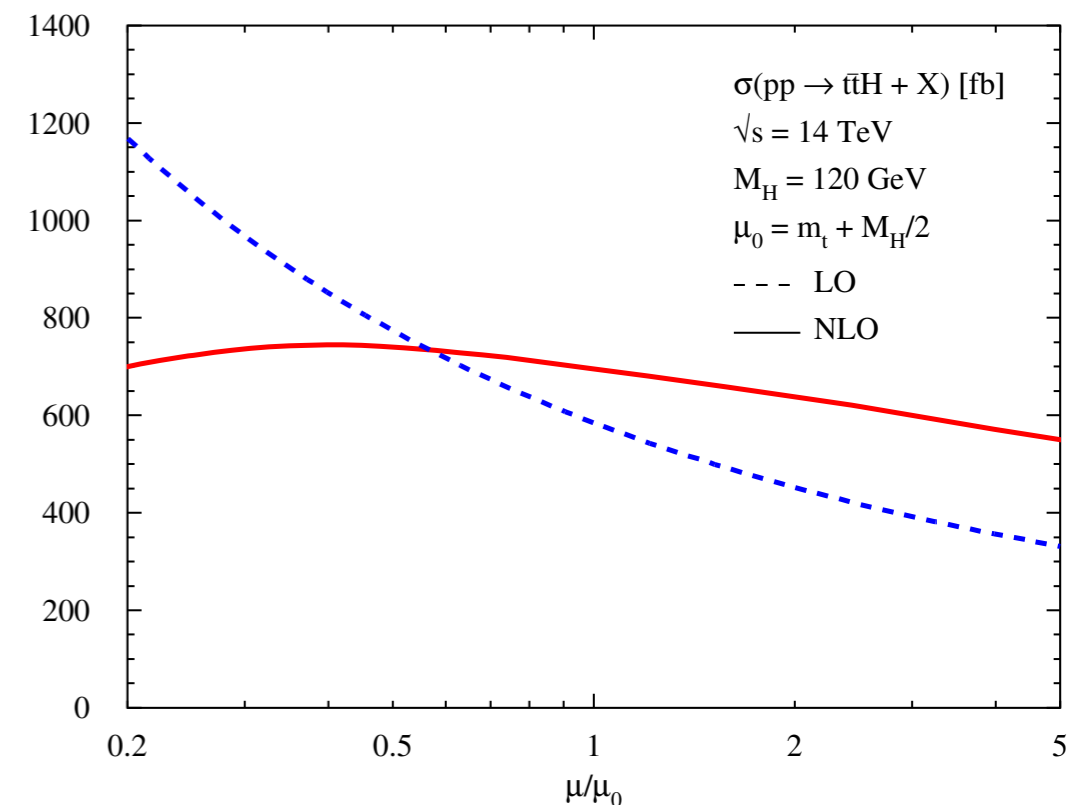
Kunszt (1984); Gunion (1991), Marciano, Paige (1991)

NLO provides more stable results (~10% scale) and 20% increase

Beenakker et al (2002), Dawson, Reina (2001),

Wackerroth et al (2003)

Recent work includes spin correlations in top decay, exclusive distributions



# Associated VH production

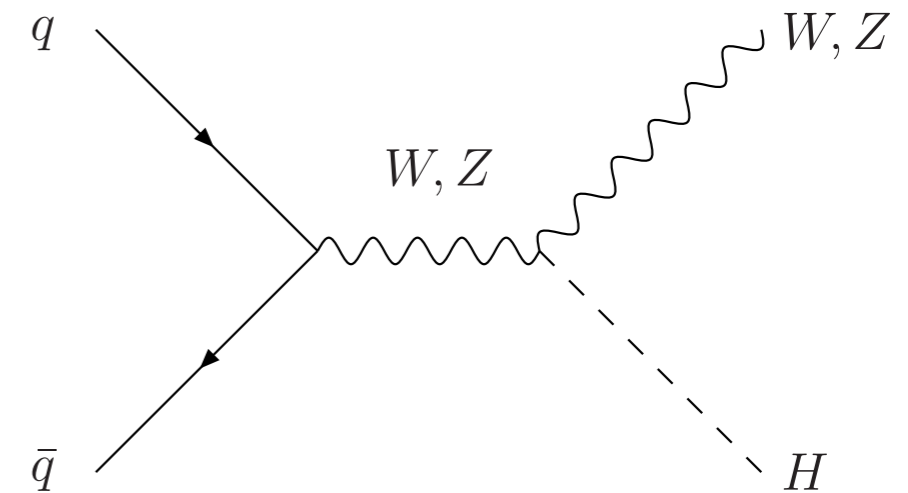
● Main channel for low mass at Tevatron

Possible at the LHC with boosted analysis



bb decay

Butterworth et al (2007)



● From QCD point of view very similar to Drell-Yan (NNLO) van Neerven et al (1991)

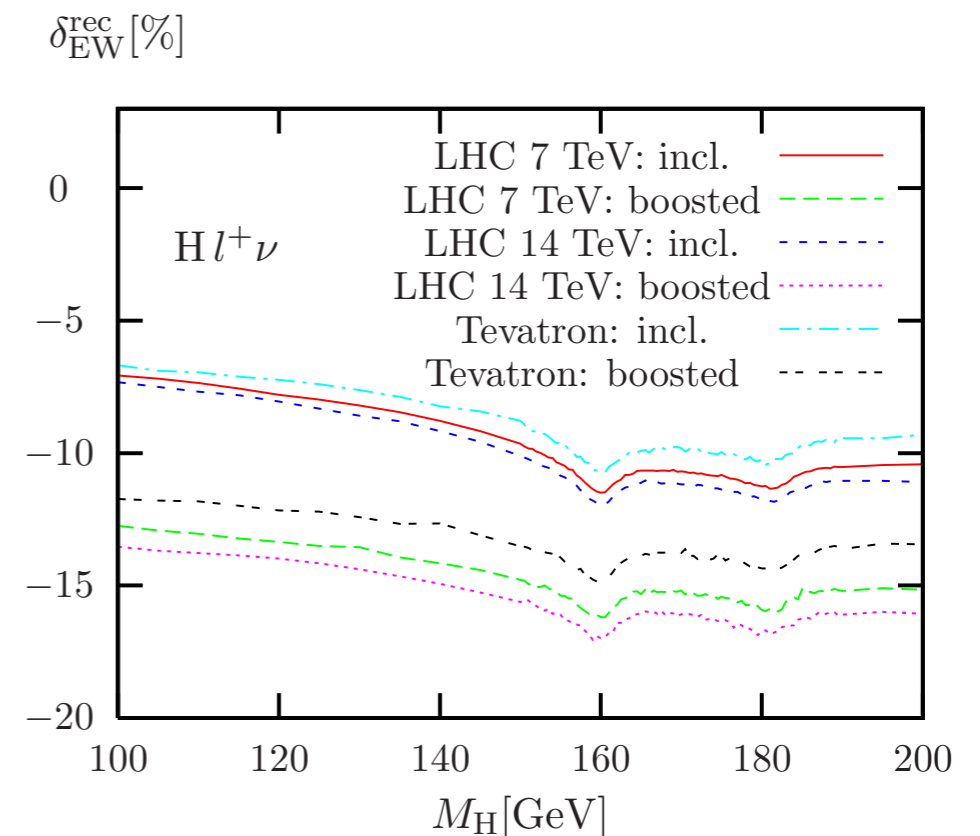
● @ NLO exactly DY : ~30% corrections

Han, Willenbrock (1990)

● EW corrections known : -(5/10) %  
more in distributions

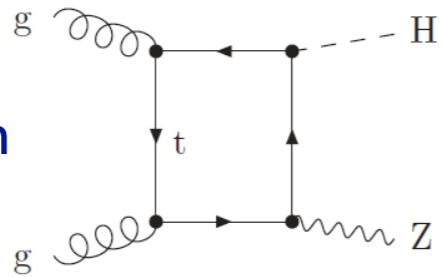
Ciccolini, Dittmaier, Kramer (2003)

HAWK: Denner, Dittmaier, Kallweit, Mück (2011)



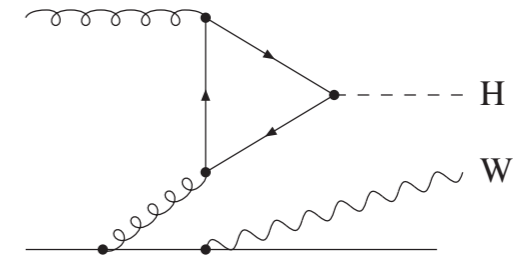
# ⊙ @ NNLO extra contributions involving a heavy quark loop

~2-6% contribution



Brein, Harlander, Djouadi (2003)

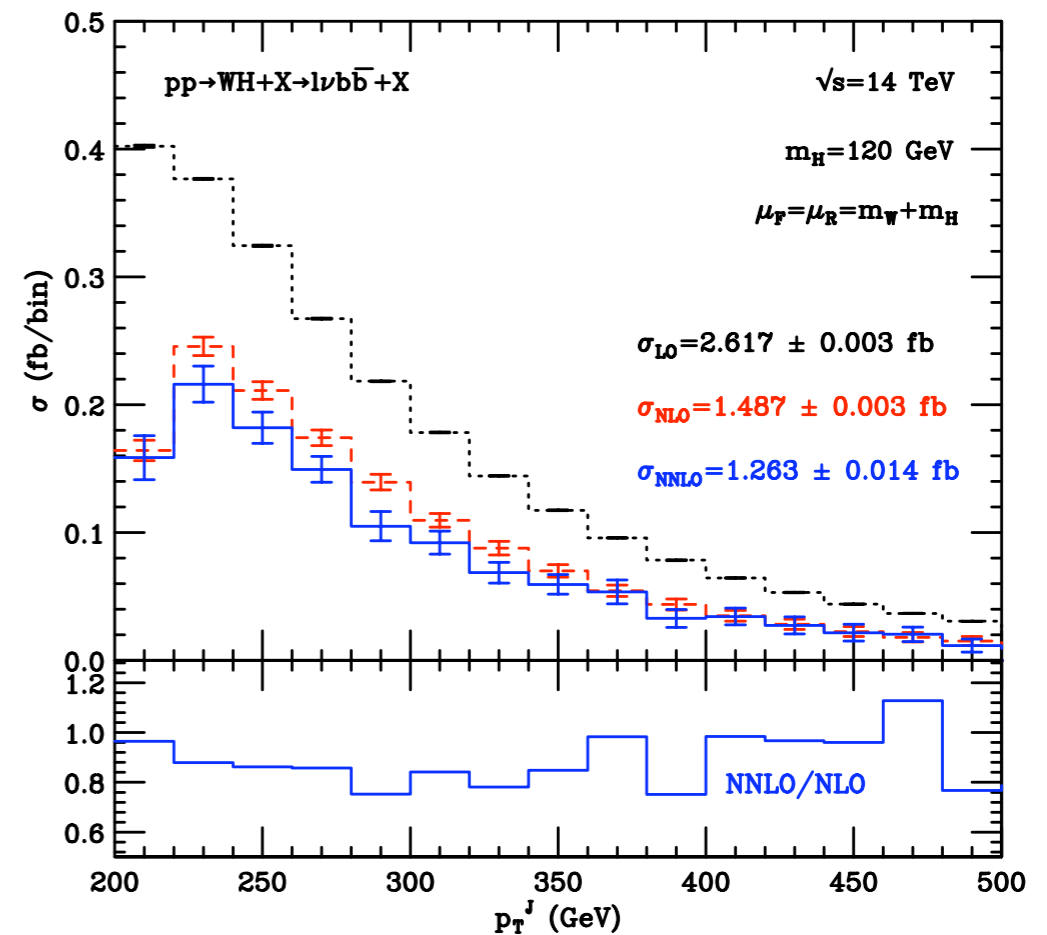
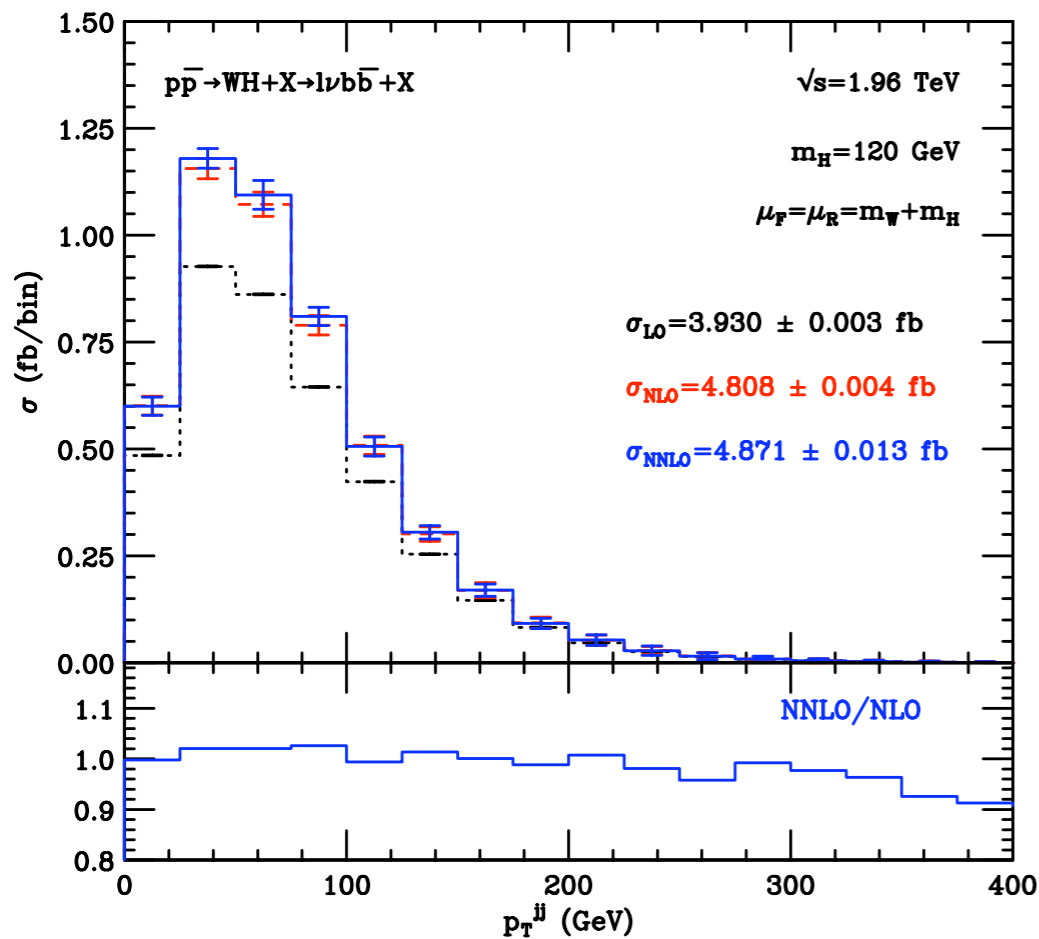
~1% contribution



Brein, Wieseemann, Harlander, Zirke (2011)

QCD corrections (N3LO) Altenkamp et al (2012)

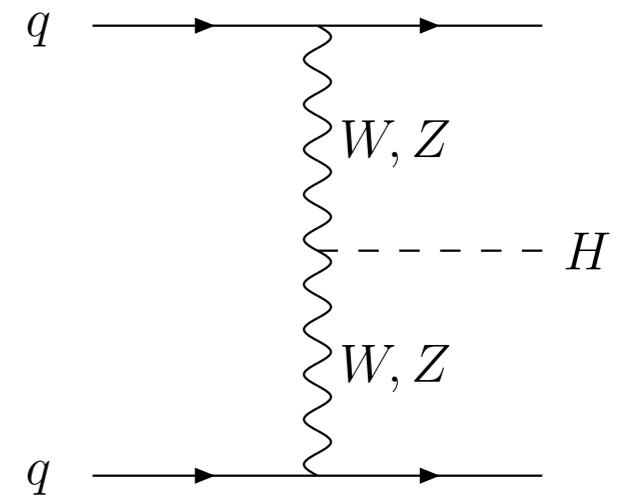
# ⊙ DY approach : fully exclusive NNLO calculation Ferrera, Grazzini, Tramontano (2011)



- Very stable results at Tevatron
- Fixed order challenged at LHC (boosted analysis with jet veto)



# Vector Boson Fusion



- Almost one order of magnitude smaller than gg fusion but still very interesting

Signature : 2 highly energetic jets without hadronic activity in a large rapidity interval

- Moderate NLO corrections ~5-10%
  - Total rate: Han, Willenbrock(1991)
  - Distributions: Figy, Oleari, Zeppenfeld (2003)
  - J.Campbel, K.Ellis (2003)

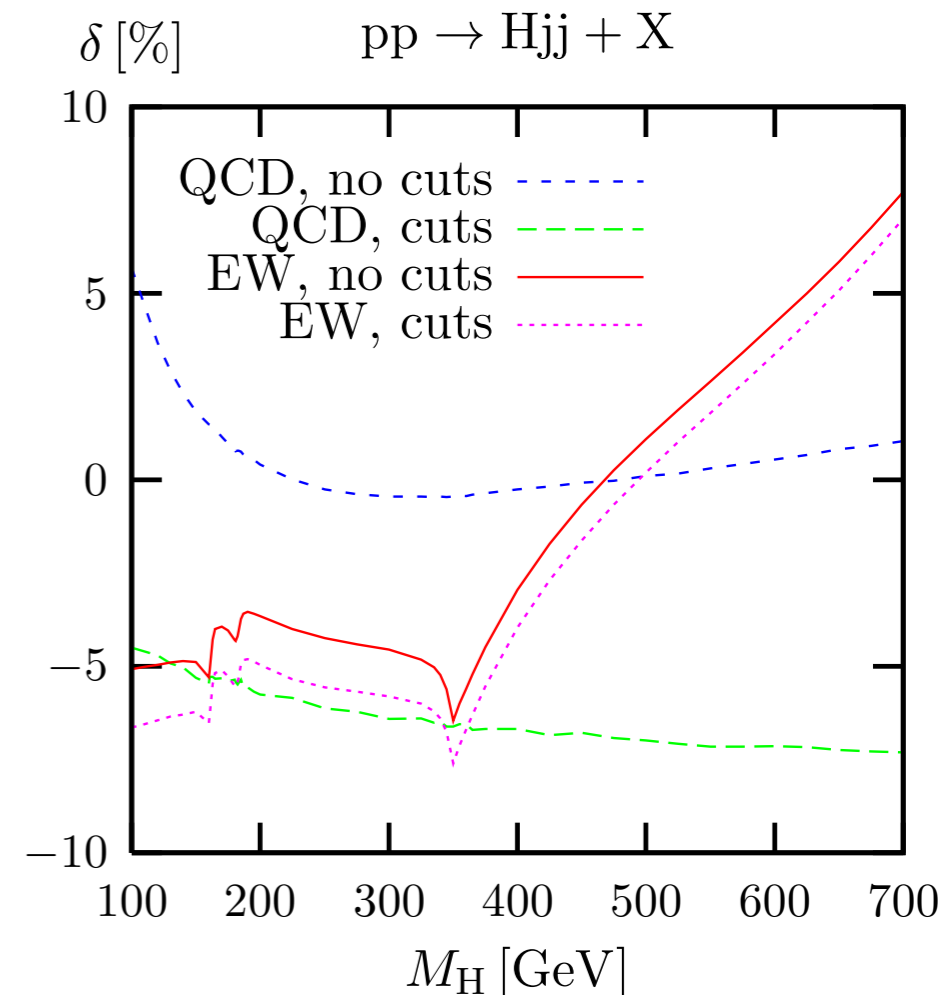
- EW+QCD corrections computed

Ciccolini, Denner, Dittmaier (2008) **HAWK**

- QCD NNLO within structure function approach

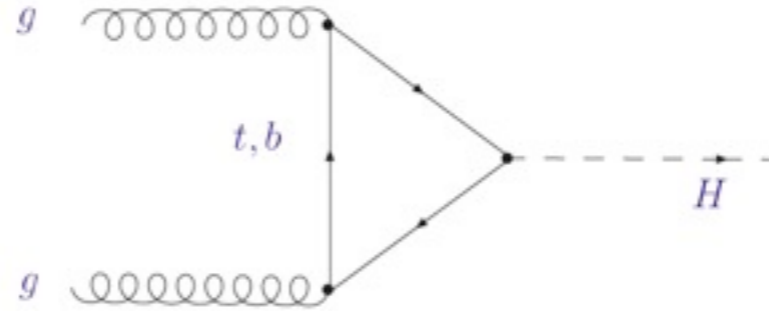
Bolzoni, Maltoni, Moch, Zaro (2011)

Good Theoretical accuracy (2% scale dependence)



# gg fusion

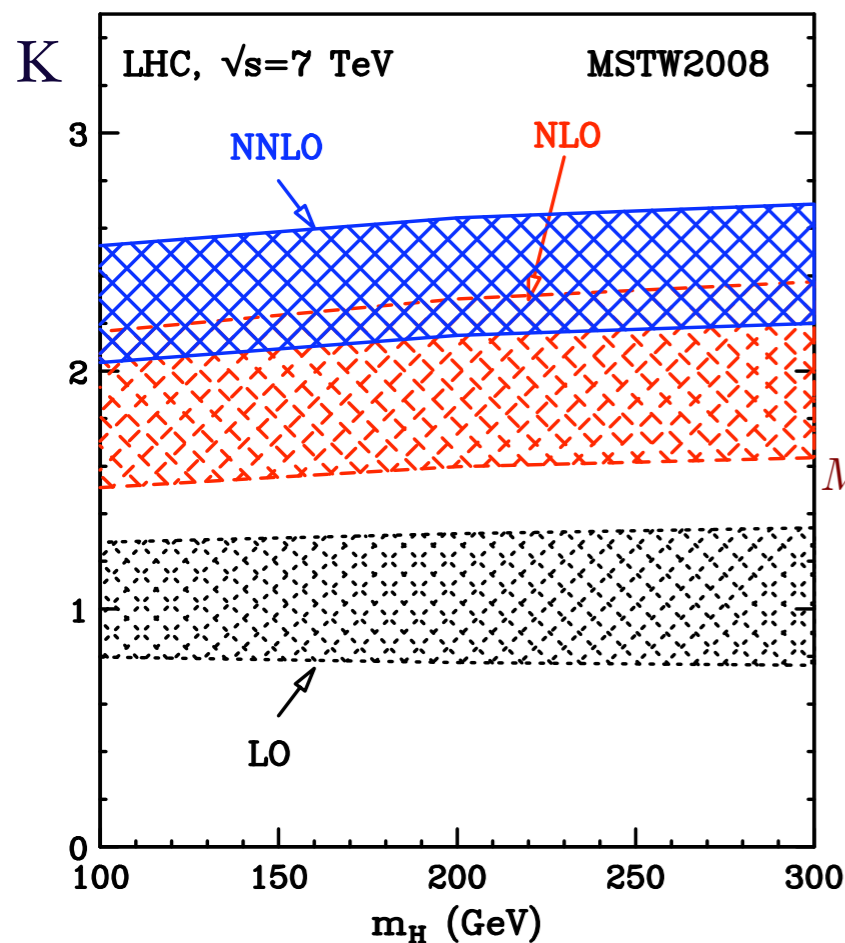
- Top quark dominates



- Higher order corrections very large:  $\mathcal{O}(100\%)$  at NLO

Large top mass limit Dawson (1991); Djouadi, Spira, Zerwas (1991)  
 exact Graudenz, Spira, Zerwas (1993)

- Still sizable at NNLO: +25% at LHC and +30% at Tevatron



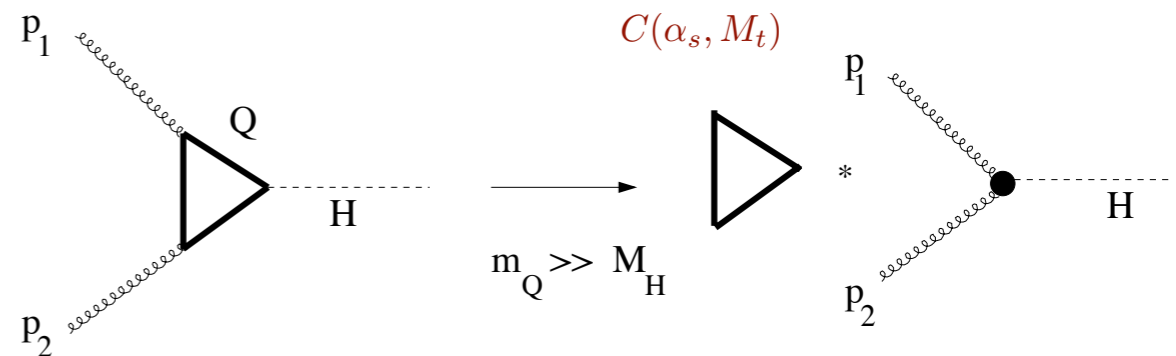
Within large  $M_t$  limit

Harlander, Kilgore (2002)  
 Anastasiou, Melnikov (2002)  
 Ravindran, Smith, van Neerven (2003)

Scale band

$$M_H/2 < \mu_F, \mu_R < 2 M_H$$

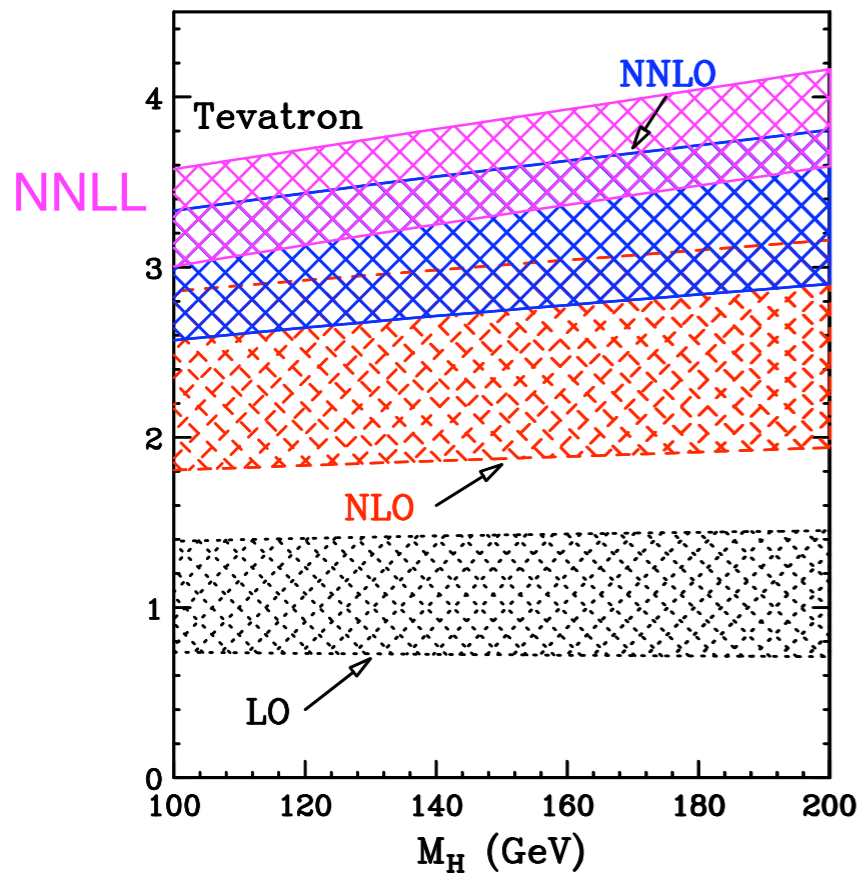
$$1/2 < \mu_F/\mu_R < 2$$



Start to observe some overlap at NNLO/NLO

# Improvements over NNLO

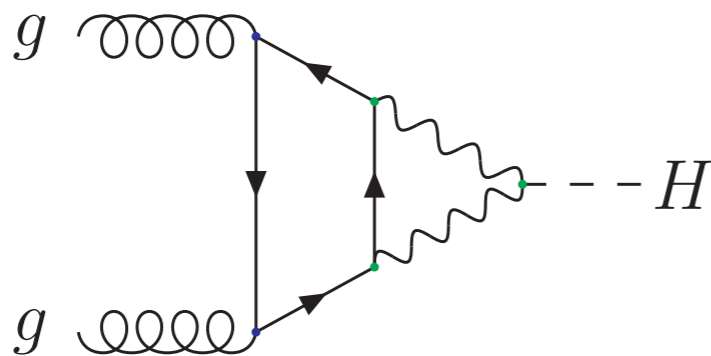
- QCD corrections completely dominated by soft and virtual gluon radiation



Threshold NNLL (+NNLO) Resummation  
**9% at 7 TeV, 13% at Tevatron**

Catani, deF, Grazzini, Nason (2003)

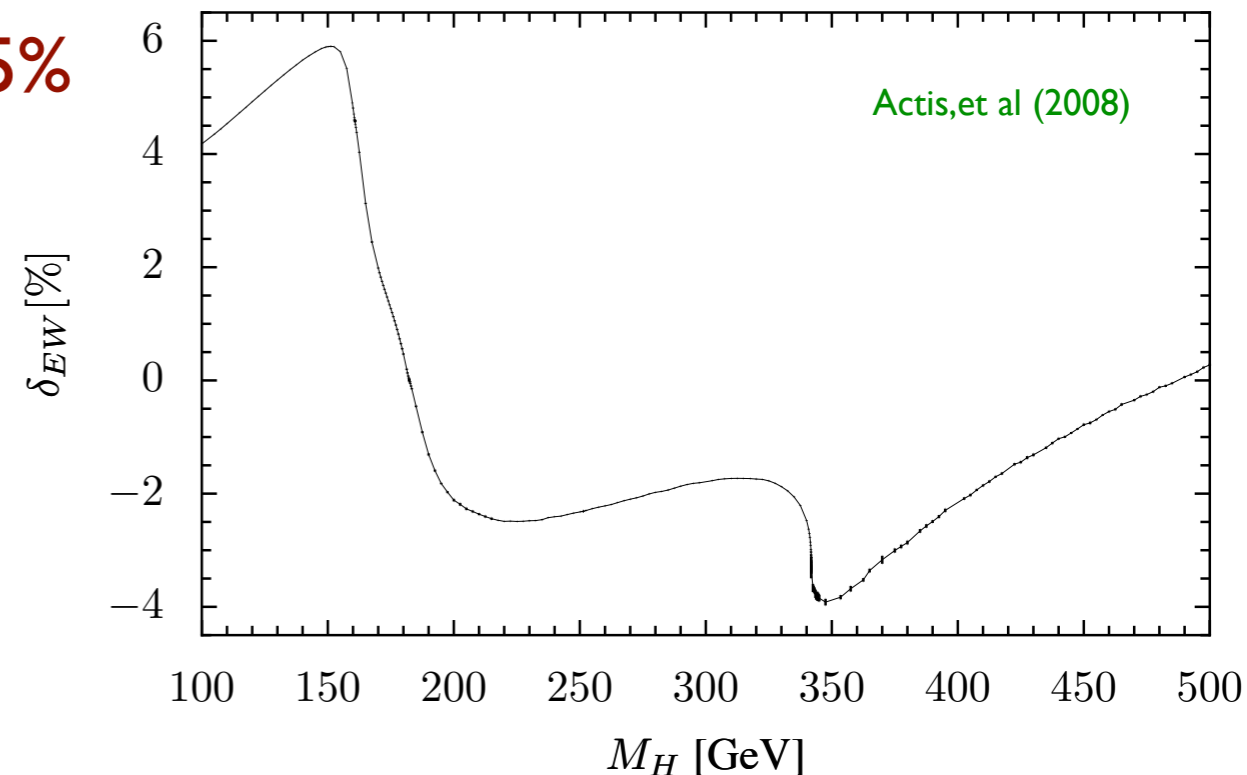
- Two loop EW corrections not negligible  $\sim 5\%$



Aglietti, Bonciani, Degrassi, Vicini (2004)

Degrassi, Maltoni (2004)

Actis, Passarino, Sturm, Uccirati (2008)



- Mixed EW-QCD effects evaluated in EFT approach

Anastasiou et al (2008)



supports “complete factorization” of EW effects

- EW effects from real radiation < 1%

Keung, Petriello(2009); Brein (2010)  
Anastasiou et al (2011)

- Higgs Line-shape

$$\sigma_{H \rightarrow X}(m_H) = \int dQ^2 \frac{Q \Gamma_{H \rightarrow X}(Q)}{\pi} \frac{\sigma_H(Q)}{(Q^2 - m_H^2)^2 + m_H^2 \Gamma_H^2}$$

complex pole

Goria, Passarino, Rosco (2011)

- Better understanding of (loop) mass effects

Schreck, Steinhauser (2007);  
Marzani et al (2008);  
Harlander et al (2009,2010)

## Improved Higgs Cross-section @ LHC

• dFG: deF, Grazzini

- Use full result at NLL+NLO and effective Lagrangian for **top** quark contribution (normalized to Born) for NNLL+NNLO

$$\sigma^{QCD} = \sigma_{top}^{NNLL+NNLO} + \sigma_{bottom}^{NLO}$$


- Include EW effects assuming complete factorization

$$\sigma^{best} = (1 + \delta_{EW}) \sigma^{QCD}$$

Actis, Passarino, Sturm, Uccirati (2008)

# Other calculations

- Baglio, Djouadi, Ferrag, Godbole (2011)
- more conservative estimate of uncertainties

- SCET resummation Ahrens, Becher, Neubert, Yang (2010)
- Exponentiates  $\pi^2$  terms (concern about consistency)
- ✓ Central value agrees with others
- Scale dependence 3% or less  underestimates TH uncertainty

- iHixs Anastasiou, Buehler, Herzog, Lazopoulos (2012)
- Based on ABPS + Breit-Wigner line-shape + EW effects from real radiation

Agreement within uncertainties with LHC-HXS numbers for light Higgs

Fully Exclusive: FEHIP Anastasiou, Melnikov, Petriello (2005)

FEHIPRO Anastasiou, Lazopoulos, Stoeckli

HNNLO Catani, Grazzini (2007)  
Grazzini (2008)

'now' including HQ mass  
dependence exactly up to NLO

scale pdf +  $\alpha_s$

$$\sigma(m_H = 125 \text{ GeV}) = 19.52^{+7.2\%}_{-7.8\%} \begin{matrix} +7.5\% \\ -6.9\% \end{matrix} \text{ pb}$$

## Uncertainties in inclusive cross-sections

Dittmaier and Schumacher (2012)

$M_H$ [GeV]	LHC @ $\sqrt{s} = 7 \text{ TeV}$				LHC @ $\sqrt{s} = 14 \text{ TeV}$			
	uncertainties		corrections		uncertainties		corrections	
	THU	PU	QCD	EW	THU	PU	QCD	EW
ggF < 500	6–10%	8–10%	$\gtrsim 100\%$	5%	6–14%	7%	$\gtrsim 100\%$	5%
VBF < 500	1%	2–7%	5%	5%	1%	3–4%	5%	5%
HW < 200	1%	3–4%	30%	5–10%	1%	3–4%	30%	5–10%
HZ < 200	1–2%	3–4%	40%	5%	2–4%	3–4%	45%	5%
ttH < 200	10%	9%	5%	?	10%	9%	15–20%	?

## PDF4LHC recommendation for Higgs

- Compute uncertainties using **global** MSTW & CT & NNPDF
- Obtain the envelope of all 68% c.l. bands : uncertainty

supplemented with  $\Delta\alpha_s(M_Z) = \pm 0.0012 (\pm 0.002)$  at 68% (90%) c.l.

## Even Higher orders $N^3LO$

- Towards  $N^3LO$  and  $N^3LL$

$$g^{(4)} \rightarrow \alpha_s^2 (\alpha_s \ln N)^n$$

Soft corrections at  $N^3LO$

Moch, Vermaseren, Vogt (2005)

combination of small  $x$  and threshold to estimate  $N^3LO$

Ball et al (2013)

Possible to reach Soft+Virtual approximation (and even beyond that) in near future

- 3 loop form factor

Baikov et al (2009)

Gehrmann et al (2010)

Lee, Smirnov, Smirnov (2010)

- Triple real emission: expansion in  $(1-z)$

Anastasiou, Duhr, Dulat, Mistlberger (2013)

- 2 loop + single emission : SV approximation

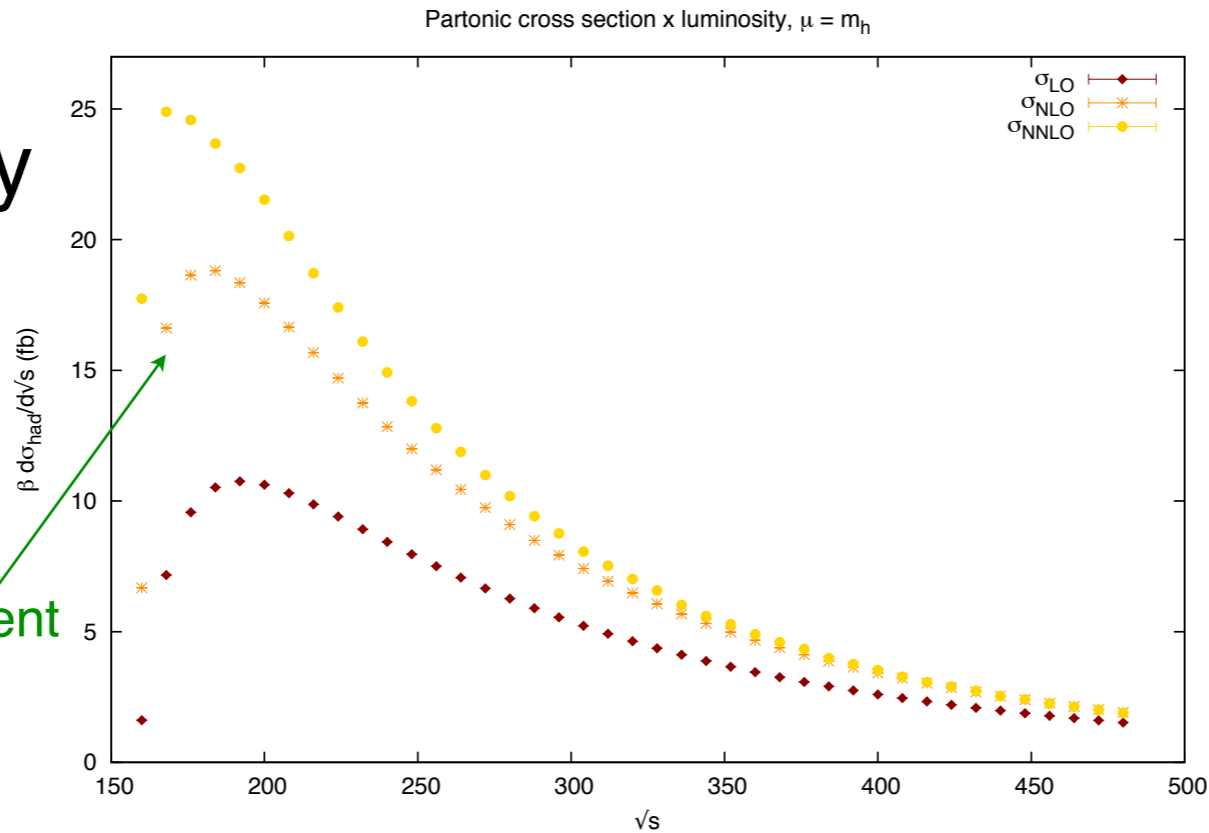
- 1 loop + double emission : needs soft current for SV approximation or explicit calculation (expansion in  $(1-z)$  )

# H+jet at NNLO

R.Boughezal, F.Caola, K.Melnikov, F.Petriello, M.Schulze (2013)

pure gluon only

Threshold enhancement



$$p_T^{jet} > 30\text{GeV}$$

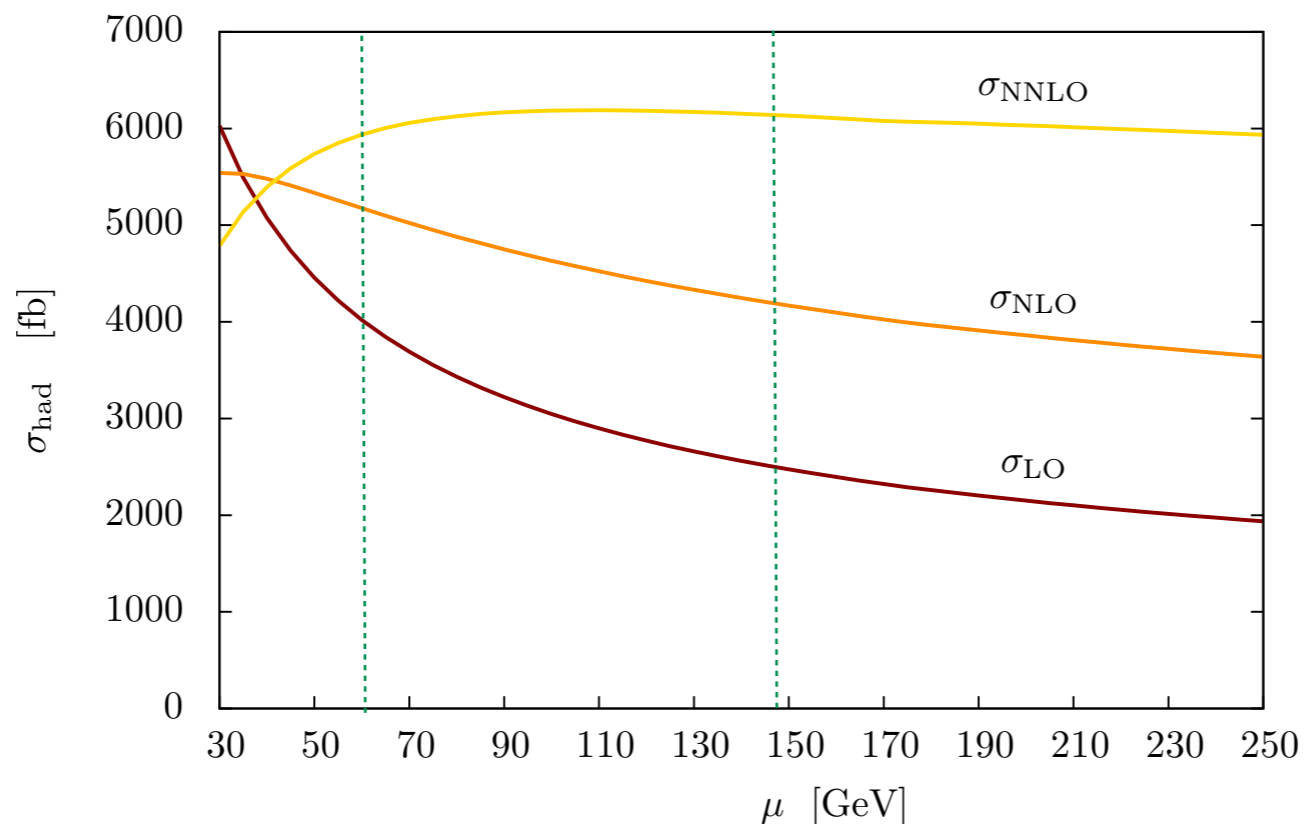
$$\sigma_{\text{LO}}(pp \rightarrow H j) = 2713_{-776}^{+1216} \text{ fb},$$

$$\sigma_{\text{NLO}}(pp \rightarrow H j) = 4377_{-738}^{+760} \text{ fb},$$

$$\sigma_{\text{NNLO}}(pp \rightarrow H j) = 6177_{+242}^{-204} \text{ fb}.$$

**+60% NLO**  
**+40% NNLO**

more stable results for  
 $\mu = M_H/2$





# Double Higgs production

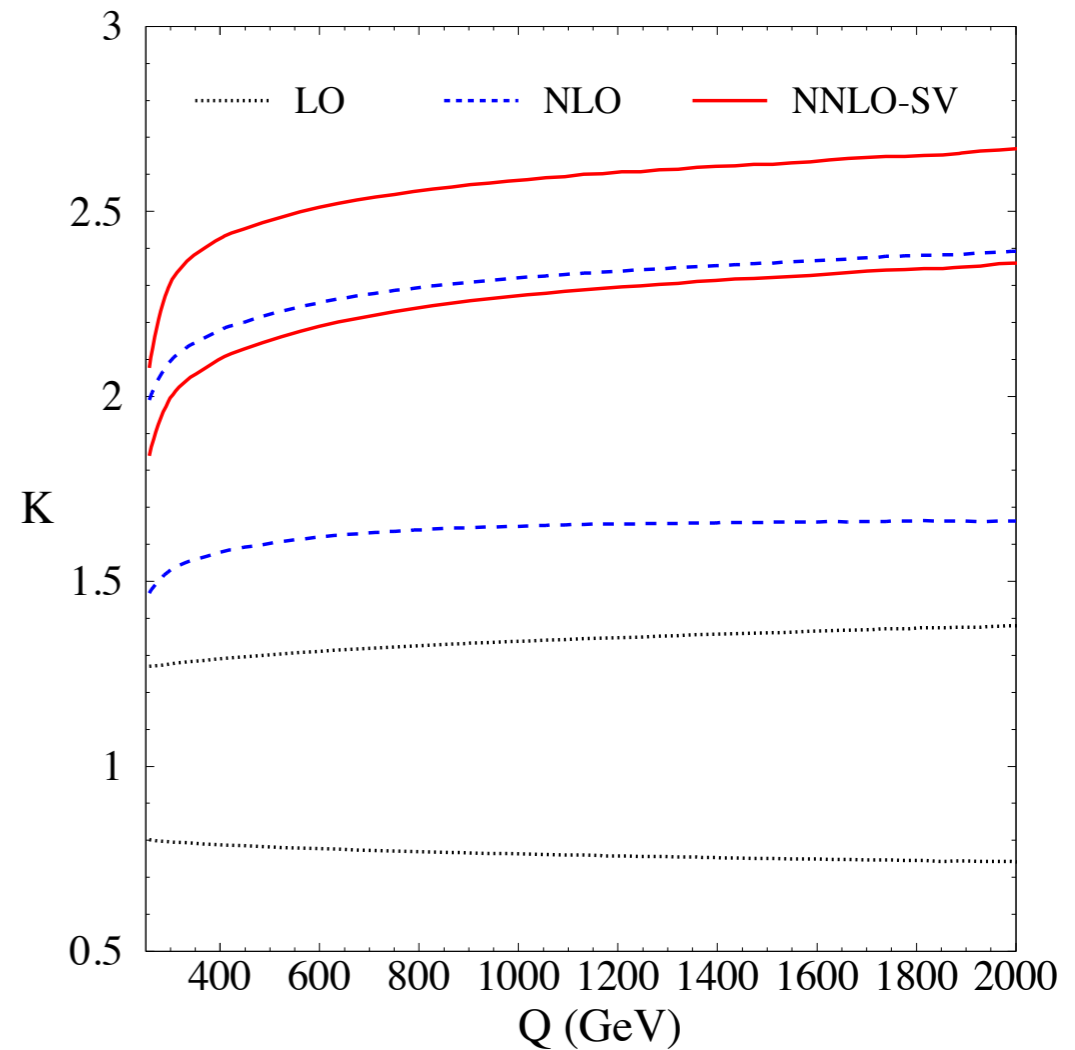
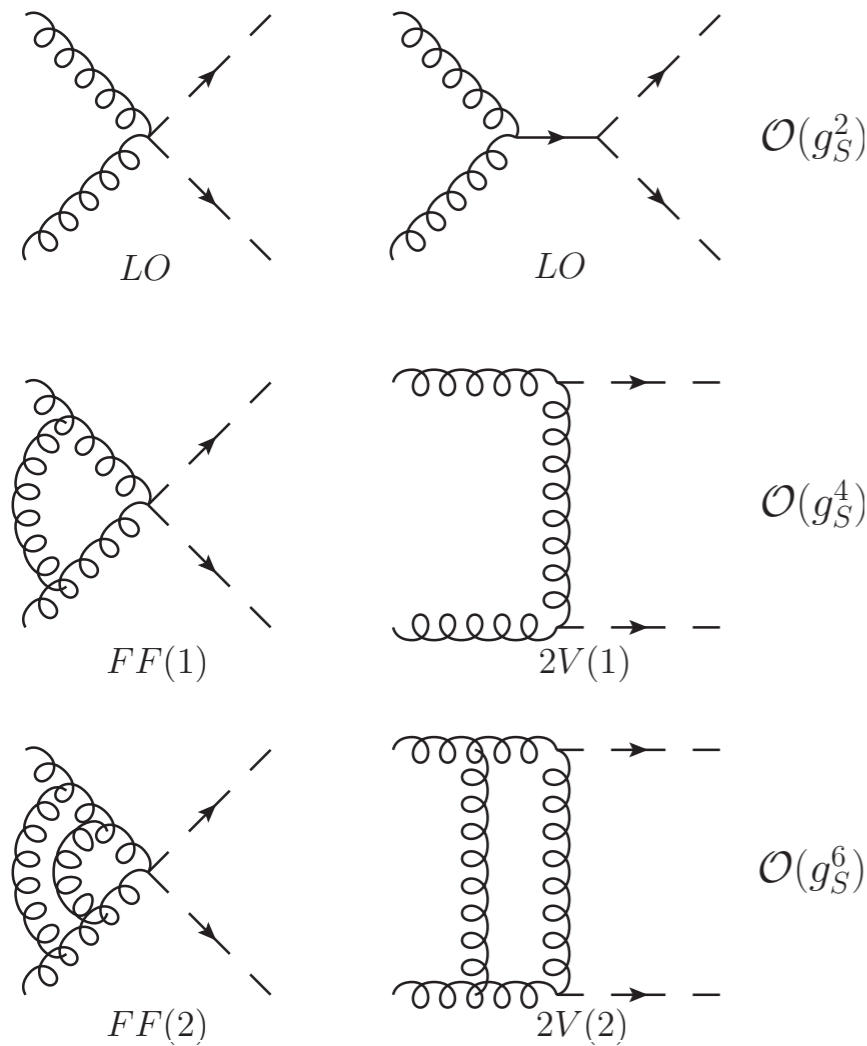
## Direct access to Higgs self-coupling

in SM

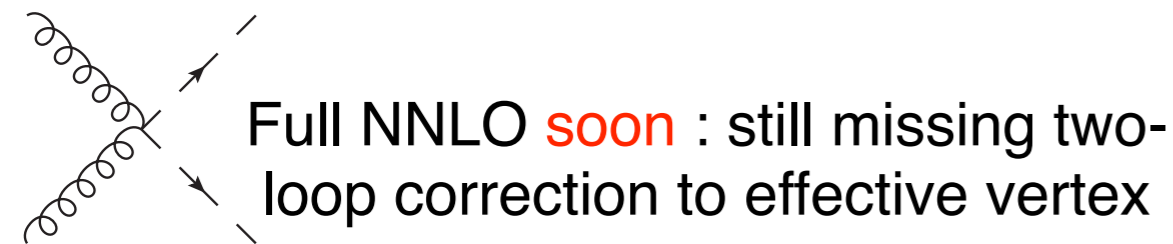
$$V(H) = \frac{1}{2} M_H^2 H^2 + \lambda v H^3 + \frac{1}{4} \lambda' H^4 \quad \lambda = \lambda' = M_H^2 / (2v^2)$$

NLO computed within effective Lagrangian (large K)

Dawson, Dittmaier, Spira (1998)



**New** : two-loop corrections and NNLO-SV approximation deF, Mazzitelli (2013)

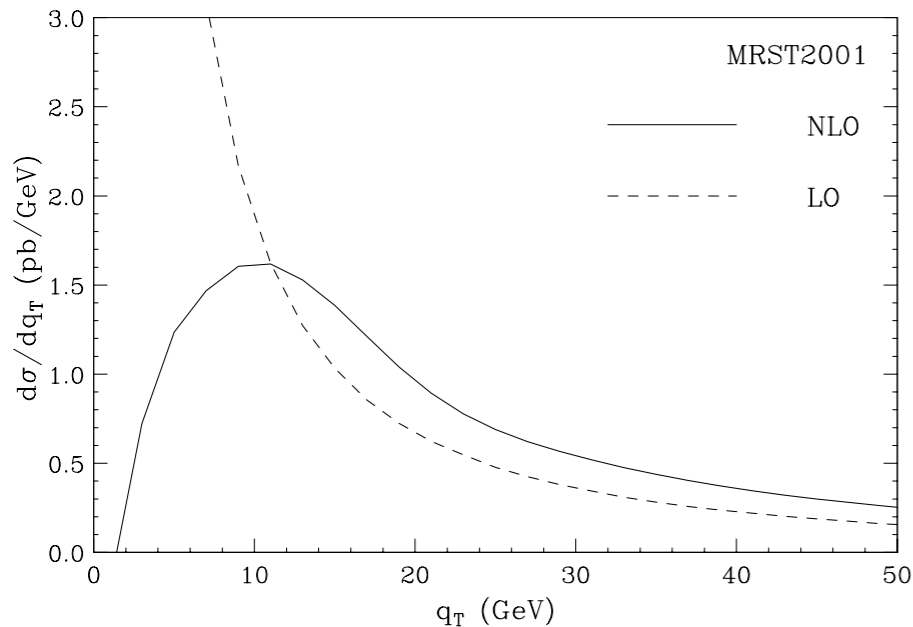


Full NNLO soon : still missing two-loop correction to effective vertex

$$C_{HH} = -\frac{1}{3} \frac{\alpha_S}{\pi} \left\{ 1 + \frac{11}{4} \frac{\alpha_S}{\pi} + \left( \frac{\alpha_S}{\pi} \right)^2 C_{HH}^{(2)} + \mathcal{O}(\alpha_S^3) \right\}$$

# Higgs Transverse momentum distribution

Fixed order not reliable at small transverse momentum

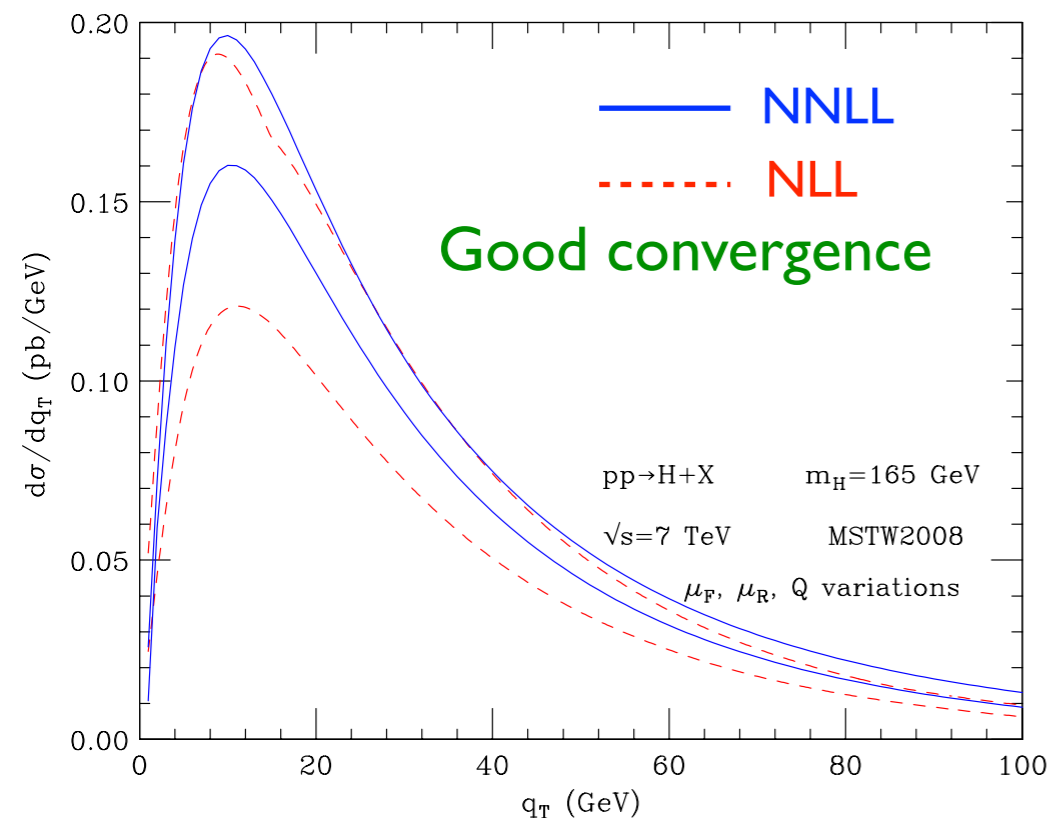


● Convergence spoiled when two scales are very different (small  $q_T$ )

$$\alpha_s^n C_n \sim \frac{\alpha_s^n}{q_T^2} \log^{2n-1} \frac{M_H^2}{q_T^2}$$

Logs originated by soft and collinear gluon radiation

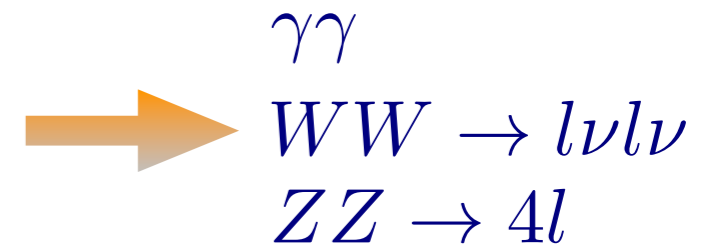
● Large logs need to be resummed! : analytical calculations allow to reach NNLL



**HqT 2.0** deF, Ferrera, Grazzini, Tommasini (2011)

**HRes** deF, Ferrera, Grazzini, Tommasini (2012)

Include full description of Higgs decay products

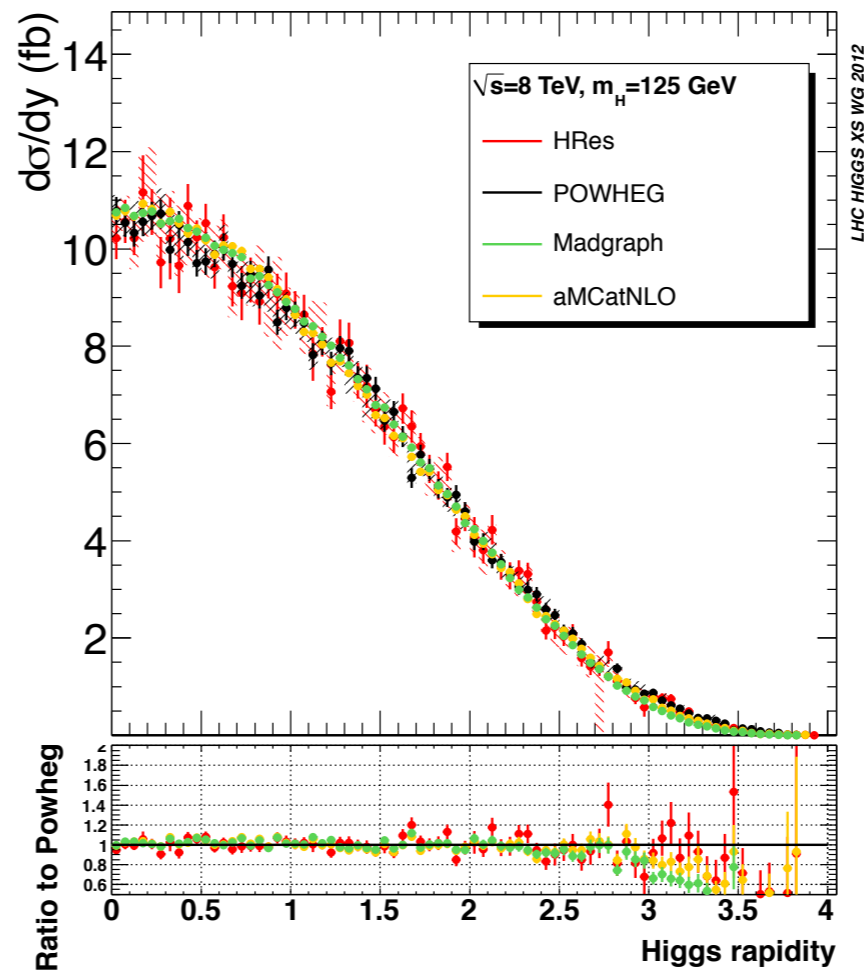
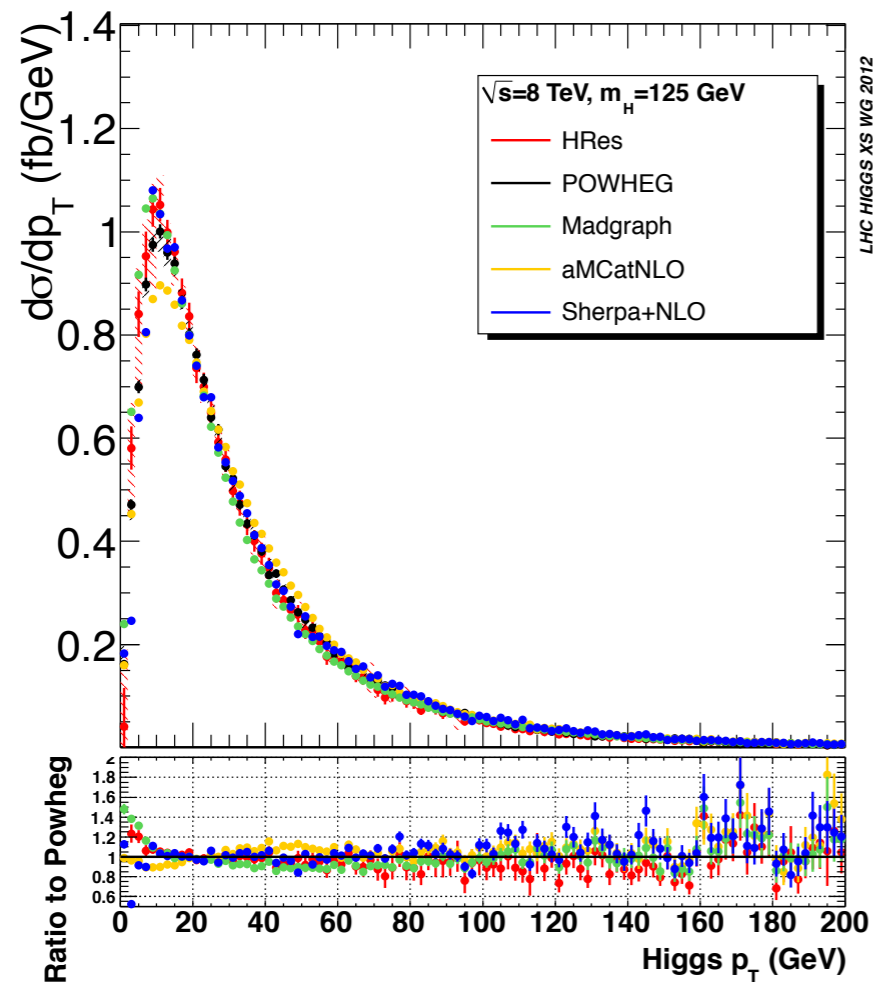


Effect from Higgs small transverse momentum propagates into more exclusive distributions

But analytical calculations are too inclusive (final state partons are integrated)

## Merging NLO with Parton Showers

- ▶ Resummation to NLL accuracy + realistic final states
- ▶ Allow to carry NLO precision to all aspects of experimental analysis
- ▶ (Formally) Same Logarithmic accuracy but numerical differences



N.Chanon

no HQ masses

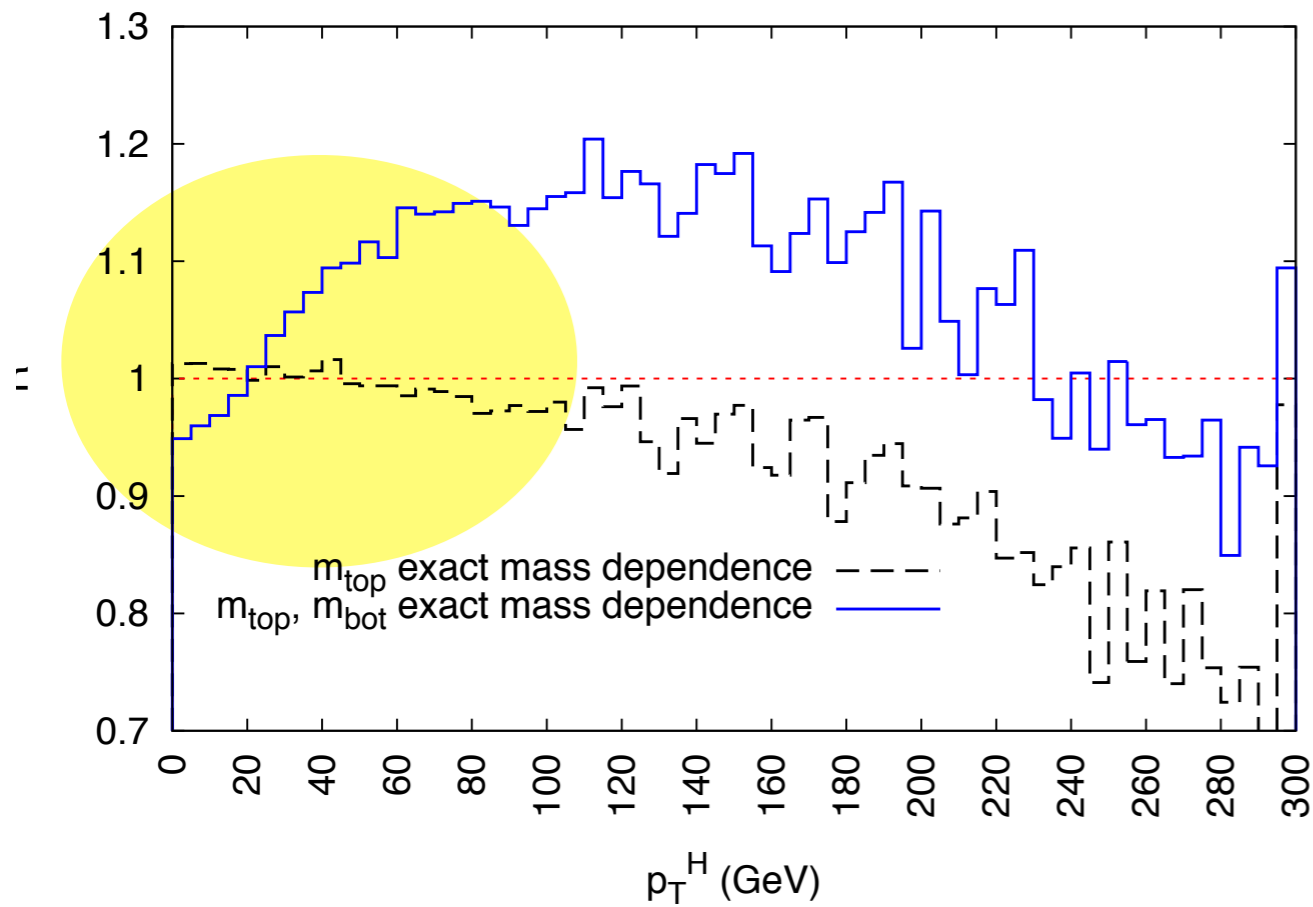
Reasonable agreement, but non-negligible differences in the spectrum

POWHEG with  $hfact=m_H/1.2$  to match Hqt/HRes

# How to include effect of HQ masses?

## POWHEG with HQ (t,b,c) masses

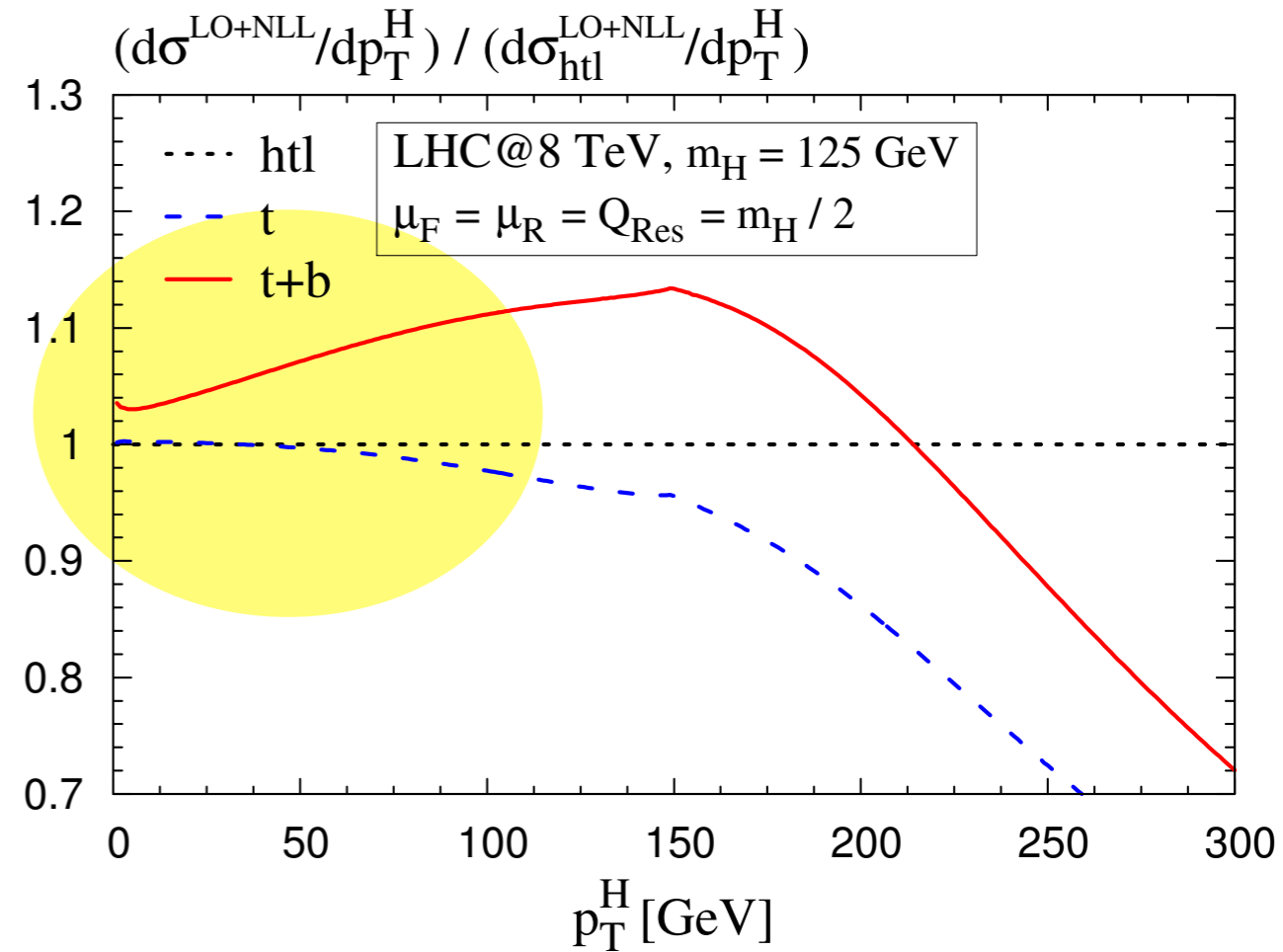
Bagnaschi, Degraasi, Slavich, Vicini



## NLL with HQ (t,b,c) masses

Mantler, Wiesemann

similar MC@NLO  
and Grazzini, Sargsyan



visible effects (depend on implementation) ~ TH uncertainty

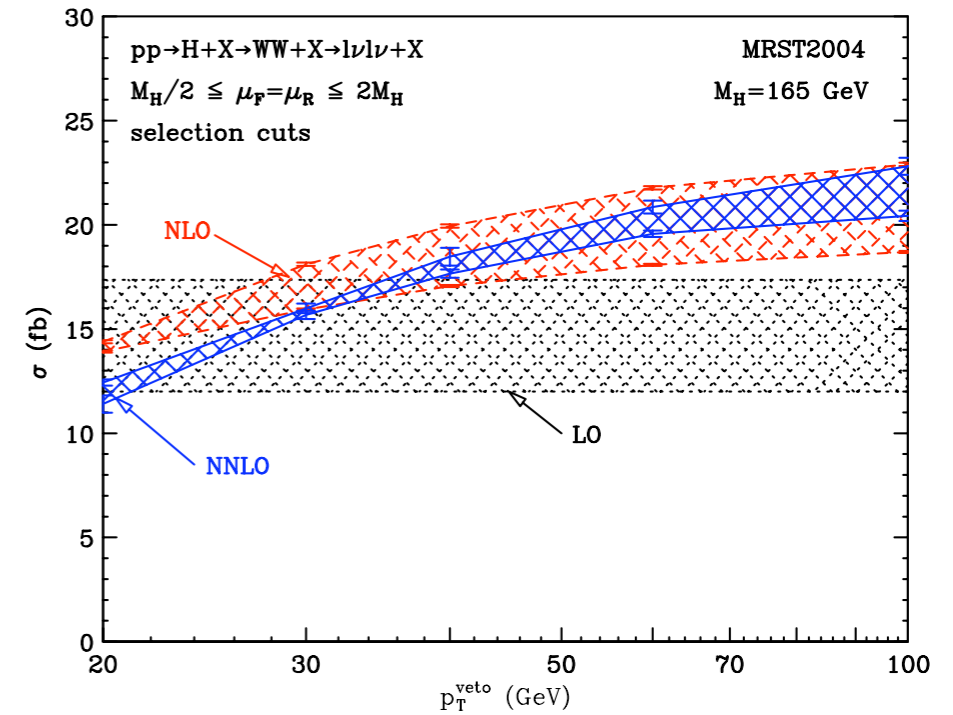
ongoing work within this workshop

# Jet-veto

Use of fixed order calculations  
dangerous for jet-veto cross section

→ underestimate uncertainties

- Better estimate of uncertainties using f.o.  
**Stewart, Tackmann**



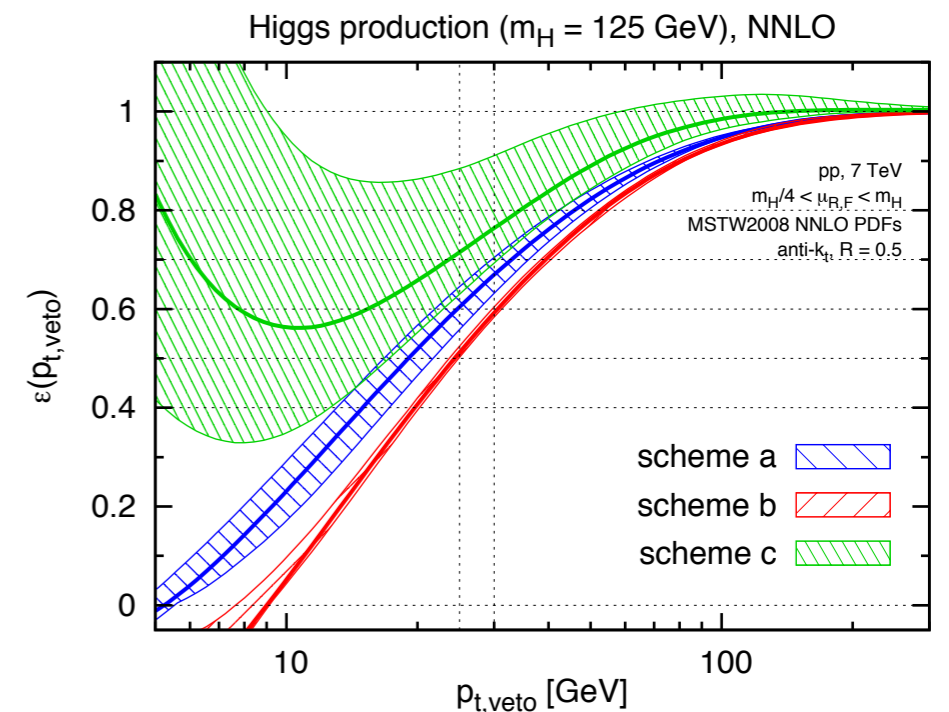
Consider *inclusive* jet cross section uncertainties → Transform to *exclusive* jet cross sections

$$\Delta_0^2 = \Delta_{\text{total}}^2 + \Delta_{\geq 1}^2$$

cut	$\frac{\Delta\sigma_{\text{total}}}{\sigma_{\text{total}}}$	$\frac{\Delta\sigma_{\geq 1}}{\sigma_{\geq 1}}$	$\frac{\Delta\sigma_{\geq 2}}{\sigma_{\geq 2}}$	$\frac{\Delta\sigma_0}{\sigma_0}$	$\frac{\Delta\sigma_1}{\sigma_1}$
$p_T^{\text{cut}} = 30 \text{ GeV}, \eta^{\text{cut}} = 3$	10%	21%	45%	17%	29%

- Alternative: study uncertainties in efficiencies  
**Banfi, Salam, Zanderighi**  $\epsilon(p_{T,\text{veto}}) \equiv \frac{\sigma_0(p_{T,\text{veto}})}{\sigma}$

Different schemes (formally equivalent definitions at NNLO) :  
Envelope from spread in central values agrees with ST

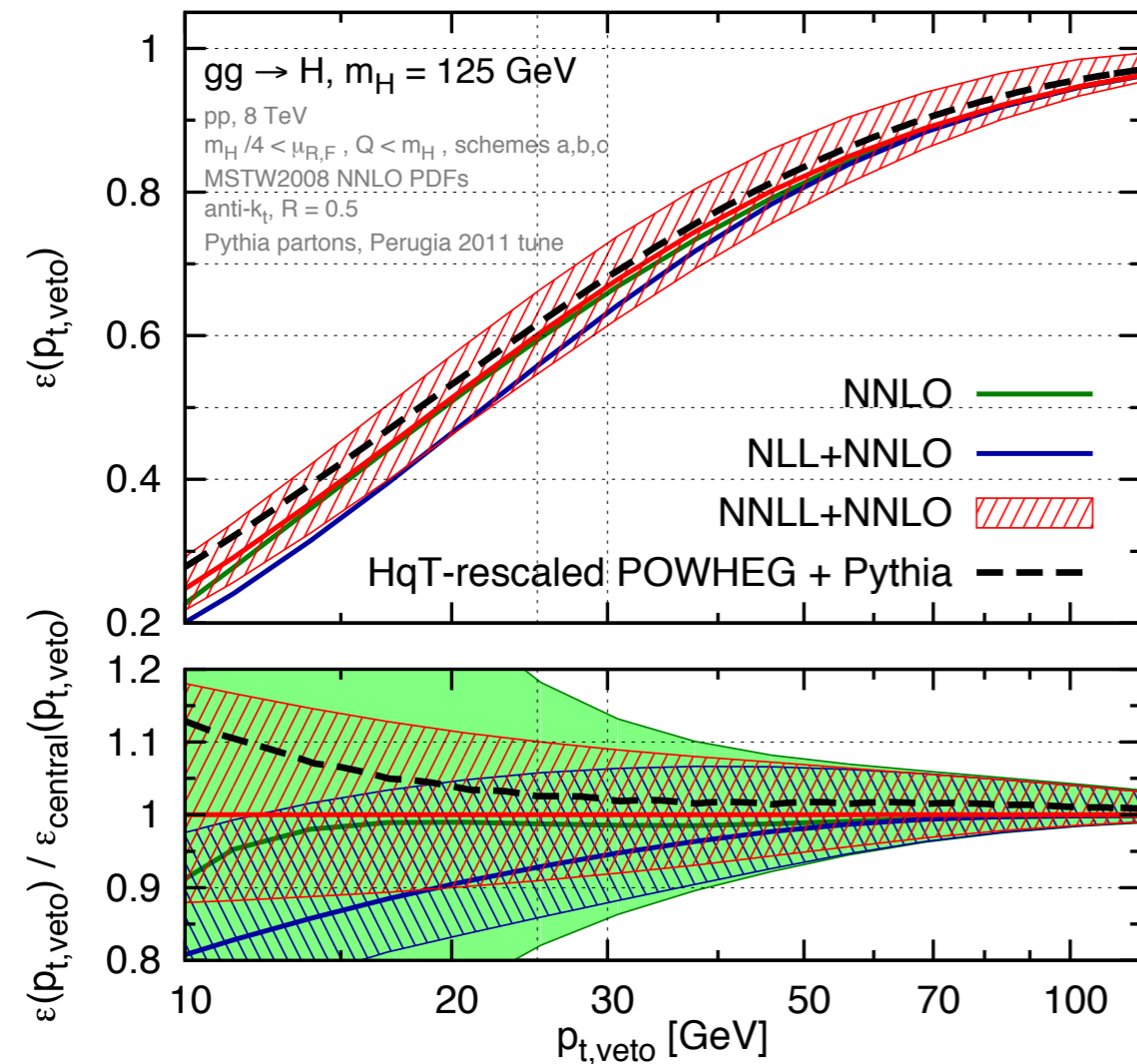


# Recent progress on resummation for jet veto ( $H+0\text{jet}$ , $H+1\text{jet}$ , $H+n\text{ jets}$ )

Berger, Marcantoni, Stewart, Tackmann, Waalewijn  
 Liu, Petriello  
 Becher, Neubert  
 Tackmann, Walsh, Zuberi  
 Bernlochner, Gangal, Gillbert, Tackmann

## NNLL+NNLO jet veto efficiencies

Banfi, Monni, Salam, Zanderighi (2012)

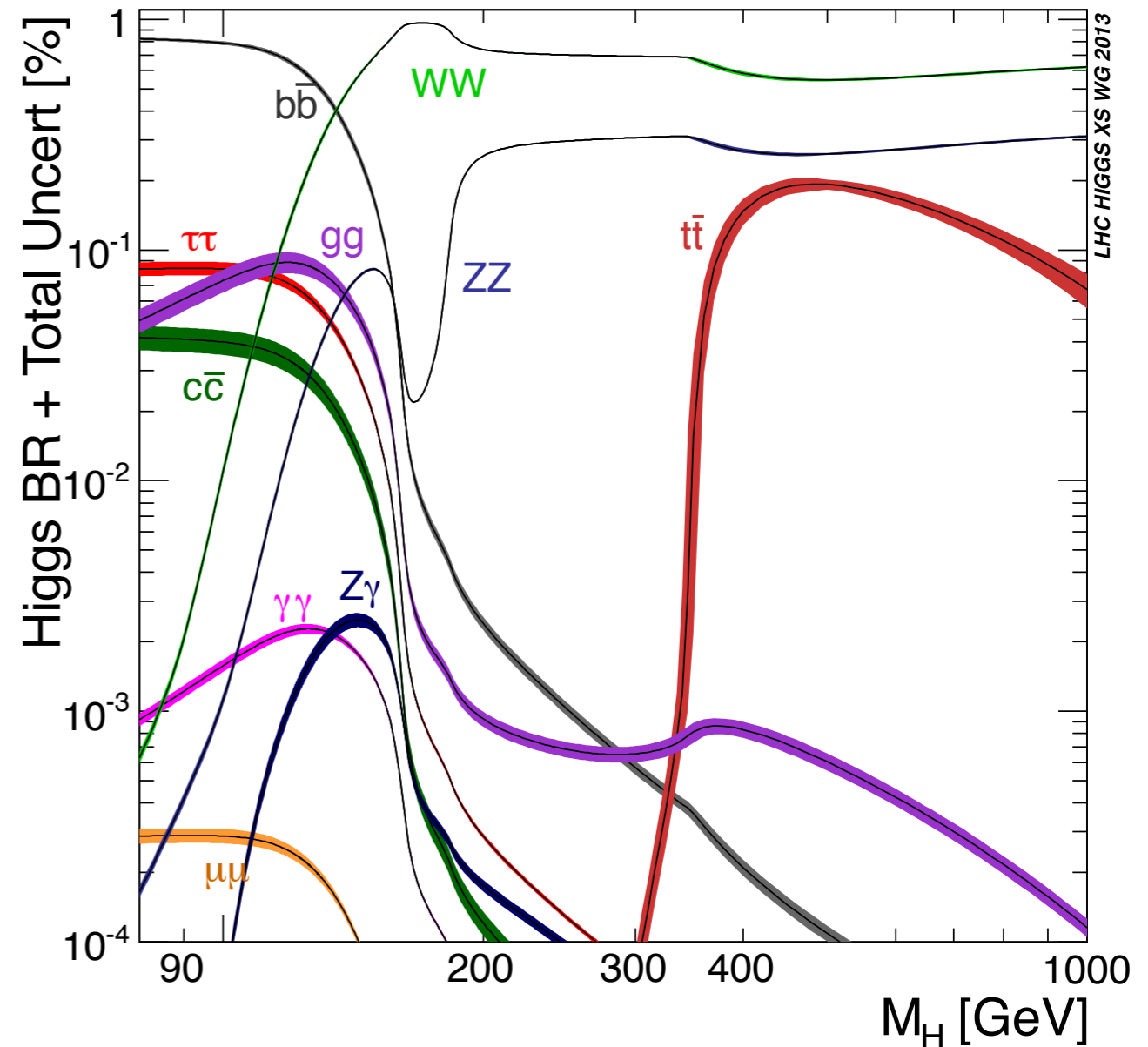
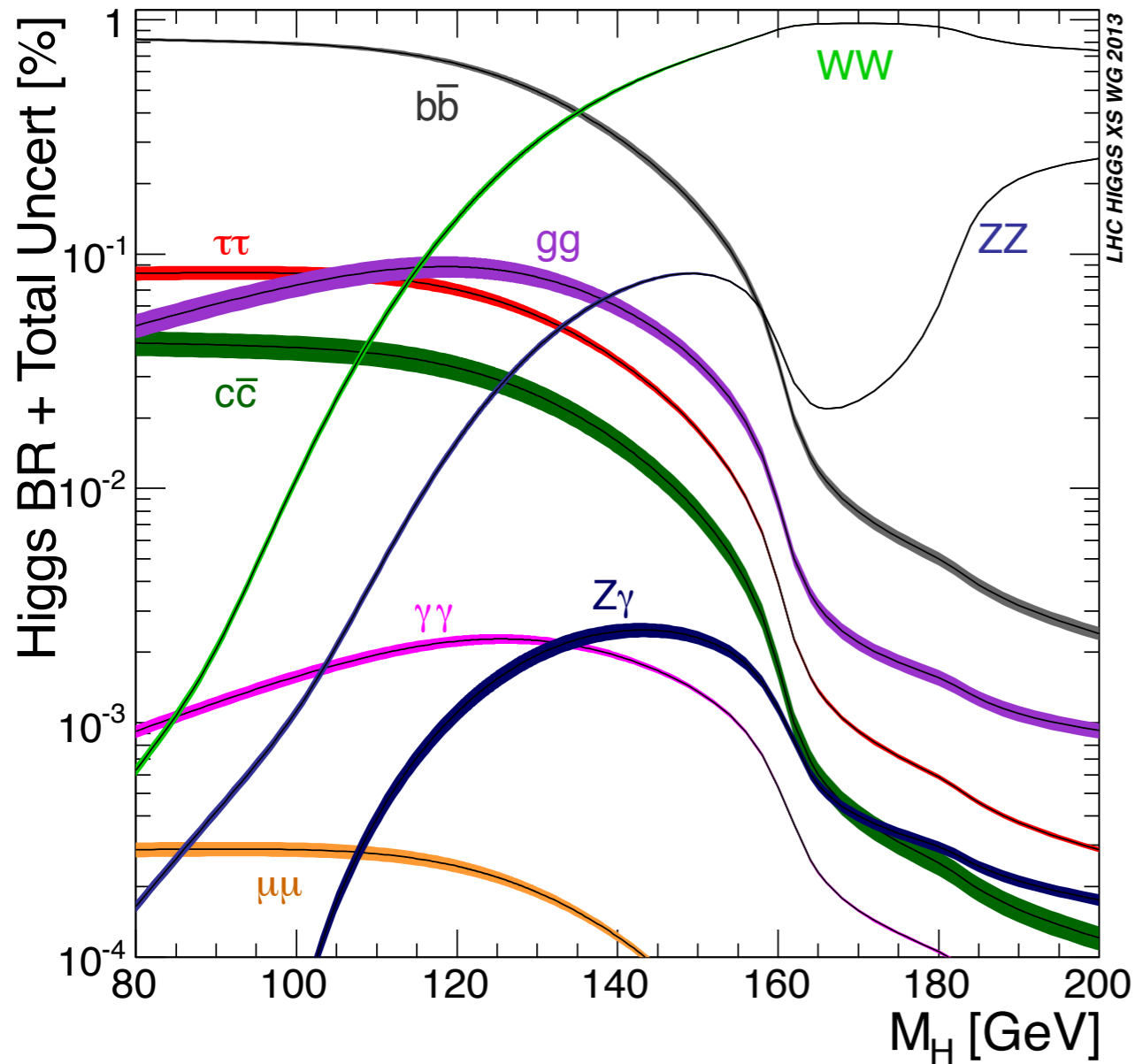


R	$p_{t,\text{veto}}$	$\epsilon^{(7 \text{ TeV})}$	$\sigma_{0\text{-jet}}^{(7 \text{ TeV})}$	$\epsilon^{(8 \text{ TeV})}$	$\sigma_{0\text{-jet}}^{(8 \text{ TeV})}$
0.4	25	$0.63^{+0.07}_{-0.05}$	$9.6^{+1.3}_{-1.1}$	$0.61^{+0.07}_{-0.06}$	$12.0^{+1.6}_{-1.4}$
0.5	30	$0.68^{+0.06}_{-0.05}$	$10.4^{+1.2}_{-1.1}$	$0.67^{+0.06}_{-0.05}$	$13.0^{+1.5}_{-1.5}$
1.0	30	$0.64^{+0.03}_{-0.05}$	$9.8^{+0.8}_{-1.1}$	$0.63^{+0.04}_{-0.05}$	$12.2^{+1.1}_{-1.4}$

**~10-13%**

- reduction in efficiency uncertainty
- **HqT-Reweighted** POWHEG agrees with central value (might not be reliable for uncertainty)

# Decay : Branching ratios (and partial widths)



$$\Gamma_H = \Gamma^{\text{HD}} - \Gamma_{ZZ}^{\text{HD}} - \Gamma_{WW}^{\text{HD}} + \Gamma_{4f}^{\text{Proph.}}$$

HDECAY

Prophecy4F

$$\Gamma_{4f}^{\text{Proph.}} = \Gamma_{H \rightarrow W^* W^* \rightarrow 4f} + \Gamma_{H \rightarrow Z^* Z^* \rightarrow 4f} + \Gamma_{WW/ZZ\text{-int.}}$$

most complicated channel (EW corrections)

$$\mathcal{A}_{ij \rightarrow H \rightarrow X} = \mathcal{A}_{ij \rightarrow H} \frac{-1}{Q^2 - m_H^2 + im_H \Gamma_H} \mathcal{A}_{H \rightarrow X}$$

$$\sigma_{H \rightarrow X}(m_H) = \int dQ^2 \frac{Q \Gamma_{H \rightarrow X}(Q)}{\pi} \frac{\sigma_H(Q)}{(Q^2 - m_H^2)^2 + m_H^2 \Gamma_H^2} \xrightarrow{\Gamma_H \ll m_H} \frac{\pi}{m_H \Gamma_H} \delta(Q^2 - m_H^2)$$

zero (narrow) width approximation

$$\sigma_{H \rightarrow X}(m_H) = \sigma_H(m_H) \frac{\Gamma_{H \rightarrow X}}{\Gamma_H} = \sigma_H(m_H) \times Br(H \rightarrow X)$$

Proper calculation requires

- Implementation of Higgs Boson Lineshape
- Computation of Signal-Background Interferences

complex pole  
Goria, Passarino, Rosco (2011)

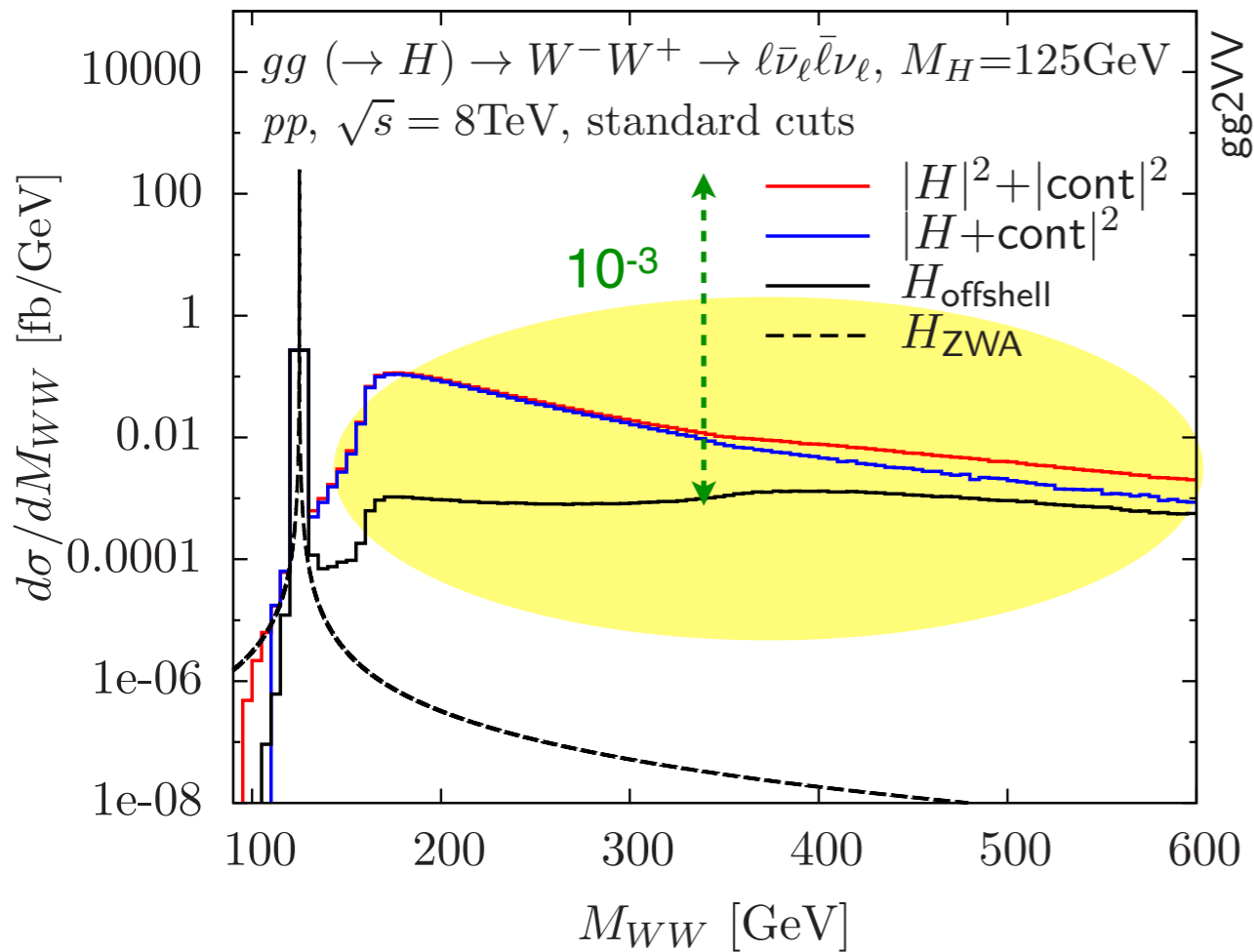
$$\mathcal{A}_{ij \rightarrow X} = \mathcal{A}_{ij \rightarrow H} \frac{-1}{Q^2 - m_H^2 + im_H \Gamma_H} \mathcal{A}_{H \rightarrow X} + \mathcal{A}_{continuum}$$



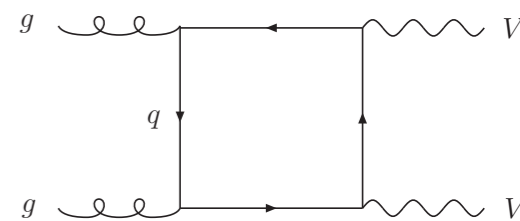
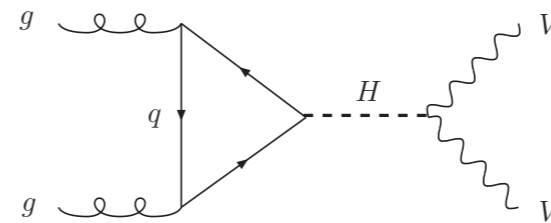
• **Finite width effects** can be sizable in some decay channels even for a light Higgs

e.g., Breit-Wigner lineshape deformed by decay amplitude above threshold

$$|\mathcal{M}_d(H \rightarrow VV)|^2 \sim (q^2)^2 \quad \text{for } \sqrt{q^2} \gtrsim 2 M_V$$



$gg (\rightarrow H) \rightarrow W^-W^+ \rightarrow \ell\bar{\nu}_\ell\ell\nu_\ell, \sigma$ [fb], $pp, \sqrt{s} = 8$ TeV, $M_H = 125$ GeV					
selection cuts	$H_{ZWA}$	$H_{\text{offshell}}$	cont	$ H_{\text{ofs}}+\text{cont} ^2$	$R$
standard cuts	2.707(3)	3.225(3)	10.493(5)	12.241(8)	0.839(2)
Higgs search cuts	1.950(1)	1.980(1)	2.705(2)	4.497(3)	0.9850(7)
$0.75M_H < M_T < M_H$	1.7726(9)	1.779(1)	0.644(1)	2.383(2)	0.9966(8)



Integration over large kinematical range enhances off-shell effects and interference with background

# How to include interference (QCD recommendations)

G.Passarino

Additive

$$\frac{d\sigma_{eff}^{NNLO}}{dx} = \frac{d\sigma^{NNLO}}{dx}(S) + \frac{d\sigma^{LO}}{dx}(I) + \frac{d\sigma^{LO}}{dx}(B)$$

Multiplicative

$$\frac{d\sigma_{eff}^{NNLO}}{dx} = K_D \left[ \frac{d\sigma^{LO}}{dx}(S) + \frac{d\sigma^{LO}}{dx}(I) \right] + \frac{d\sigma^{LO}}{dx}(B), \quad K_D = \frac{\frac{d\sigma^{NNLO}}{dx}(S)}{\frac{d\sigma^{LO}}{dx}(S)},$$

Intermediate

$$\frac{d\sigma_{eff}^{NNLO}}{dx} = K_D \frac{d\sigma^{LO}}{dx}(S) + (K_D^{gg})^{1/2} \frac{d\sigma^{LO}}{dx}(I) + \frac{d\sigma^{LO}}{dx}(B) \quad \text{“Central value”}$$

Signal-background interference effects for  $gg \rightarrow H \rightarrow W^+W^-$  beyond leading order

M.Bonvini, F.Caola, S.Forte, K.Melnikov, G.Ridolfi

Use soft-virtual approximation at NNLO (assuming two-loop Higgs coefficient for background)

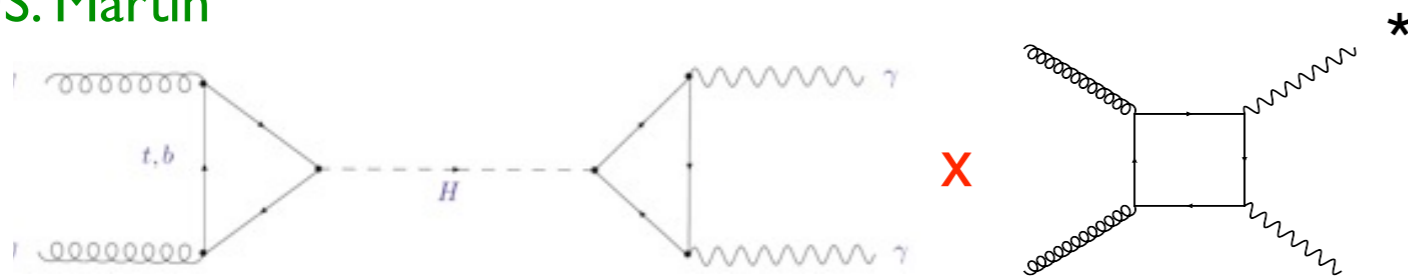
QCD corrections enhance interference, similar to enhancement for signal

$$K_{signal} \sim K_{interf}$$

	$m_h = 600 \text{ GeV}$ , $\sqrt{s} = 8 \text{ TeV}$			$\sqrt{s} = 13 \text{ TeV}$		
	LO	NLO	NNLO	LO	NLO	NNLO
$\sigma_H$	0.379	0.83(2)	1.07(5)	1.55	3.29(8)	4.2(2)
$\sigma_{Hi}$	0.427	0.93(3)	1.20(7)	1.66	3.5(1)	4.5(2)
$\sigma_H/\sigma_H^{LO}$	—	2.19(5)	2.8(1)	—	2.13(5)	2.7(1)
$\sigma_{Hi}/\sigma_{Hi}^{LO}$	—	2.19(7)	2.8(2)	—	2.12(6)	2.7(1)

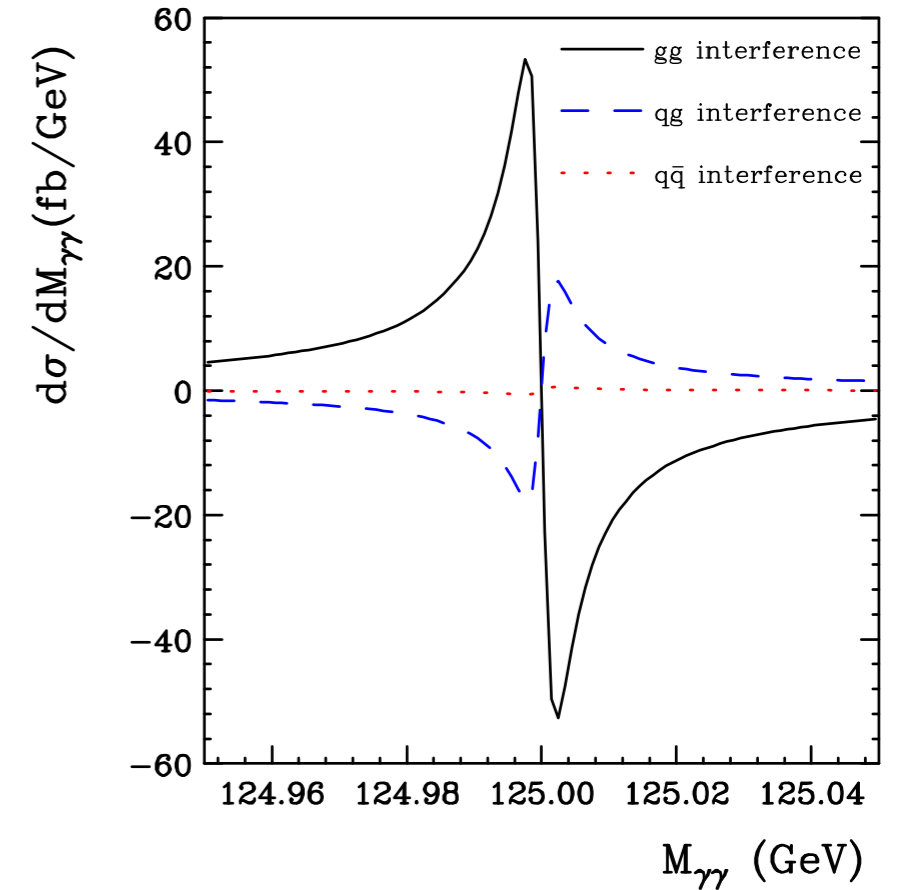
# Interference in diphoton production

• S. Martin



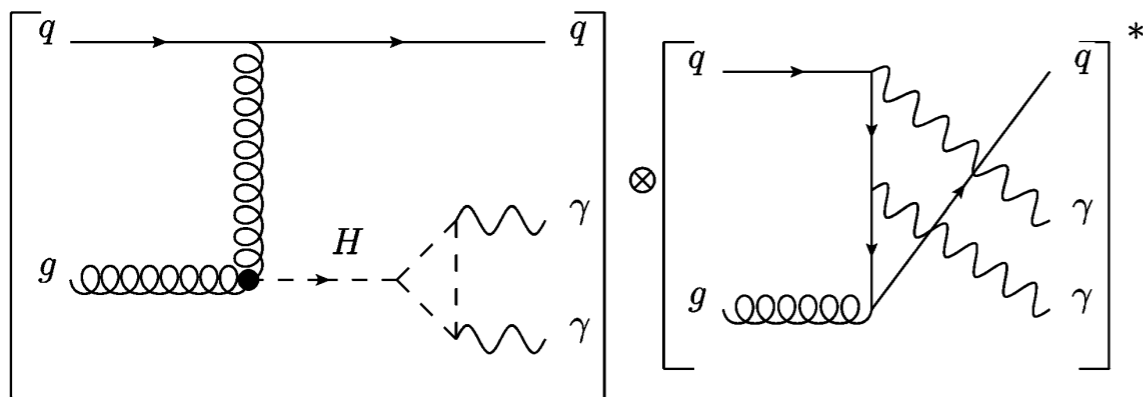
- small asymmetry in the interference
- at this level shift is  $O(\text{MeV})$  as expected

Asymmetry enhanced by detector resolution can reach 100 MeV effect

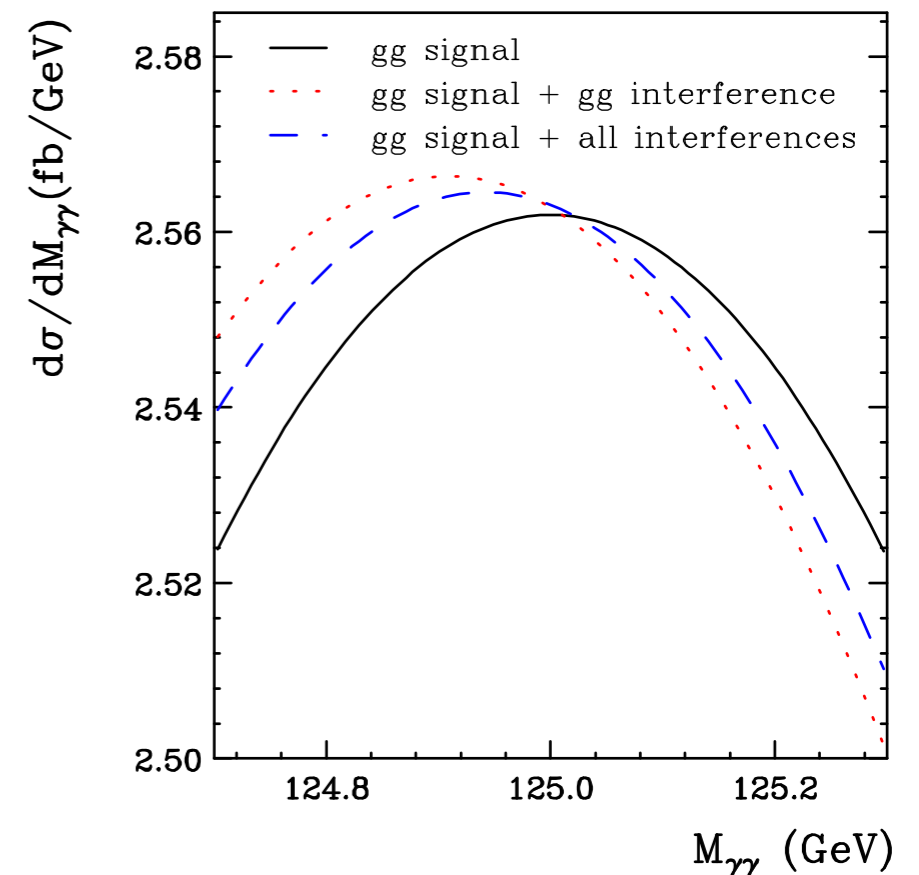


Effects from other channels go in opposite direction

• D.deF., N.Fidanza, R.Hernandez-Pinto, J.Mazzitelli, Y.Rotstein, G.Sborlini

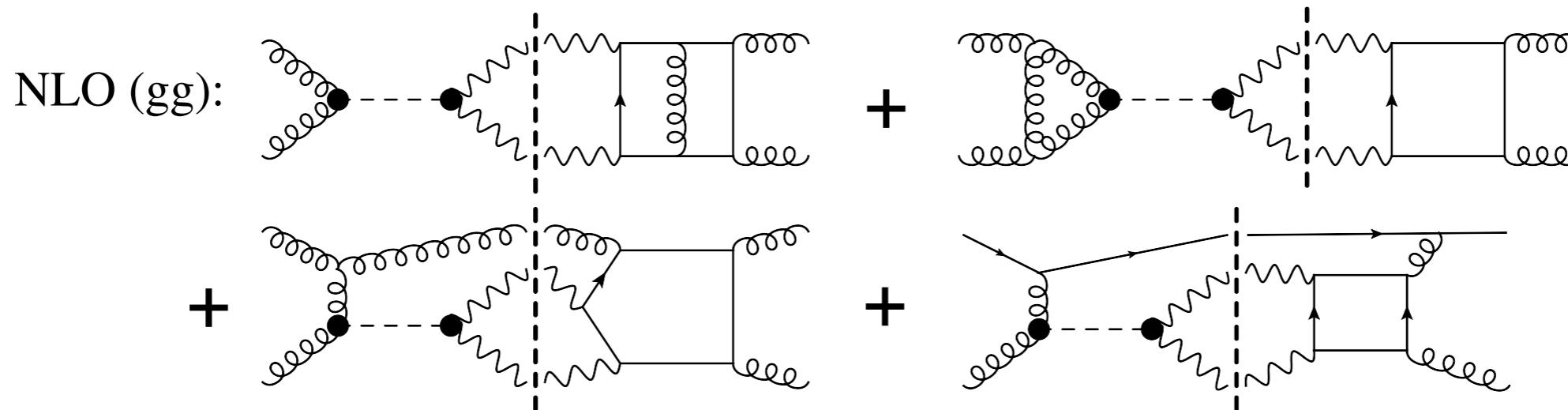


90 MeV  $\longrightarrow$  60 MeV



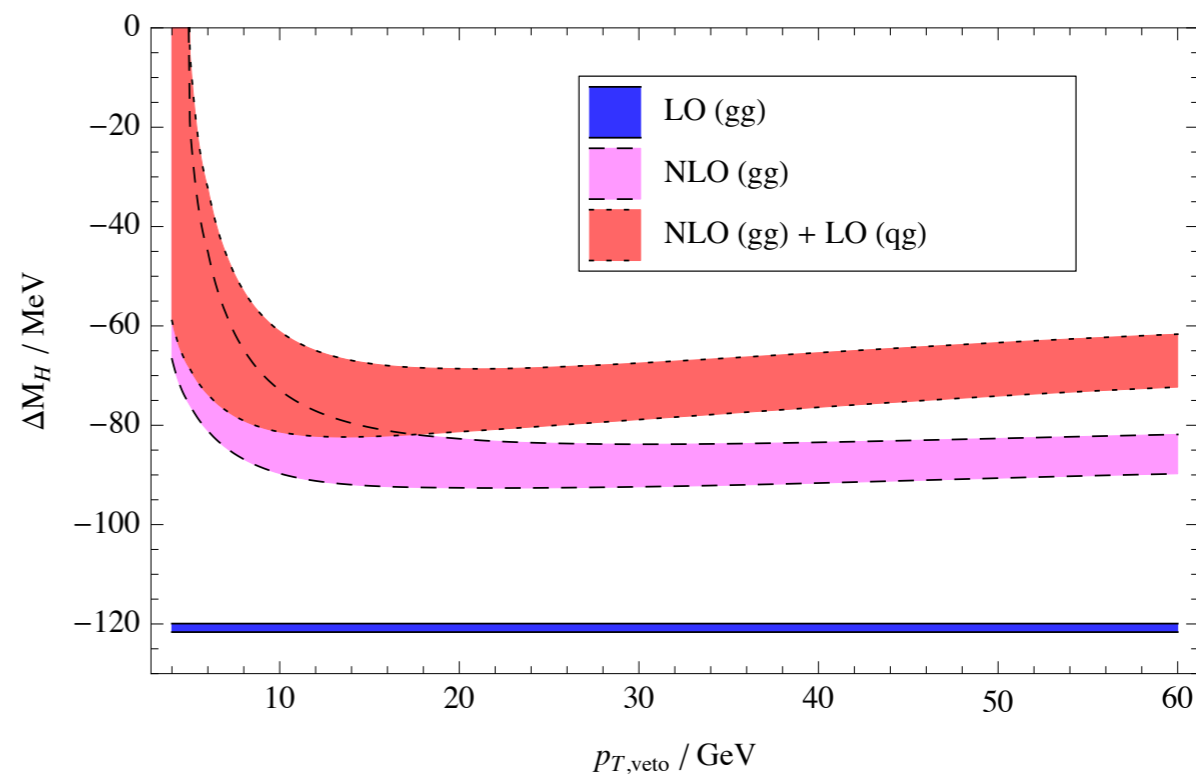
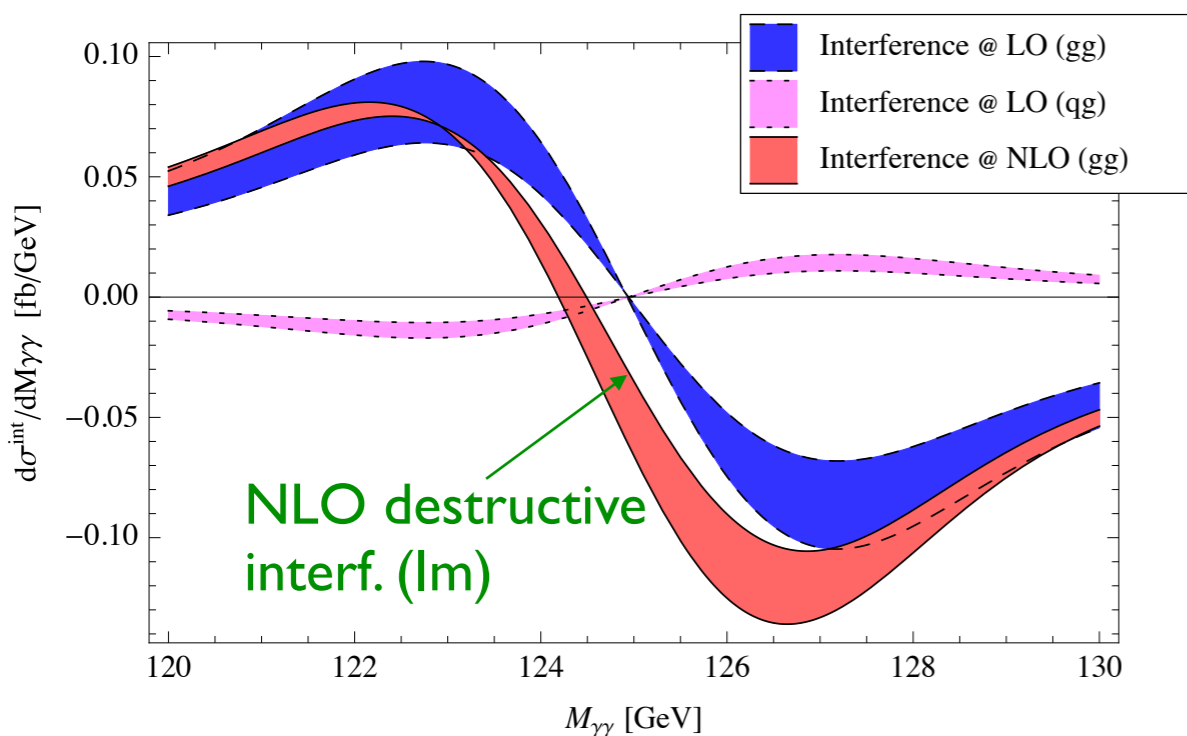
# Interference at NLO

L.Dixon, Y.Li (2013)



## Interferences

## Mass shift

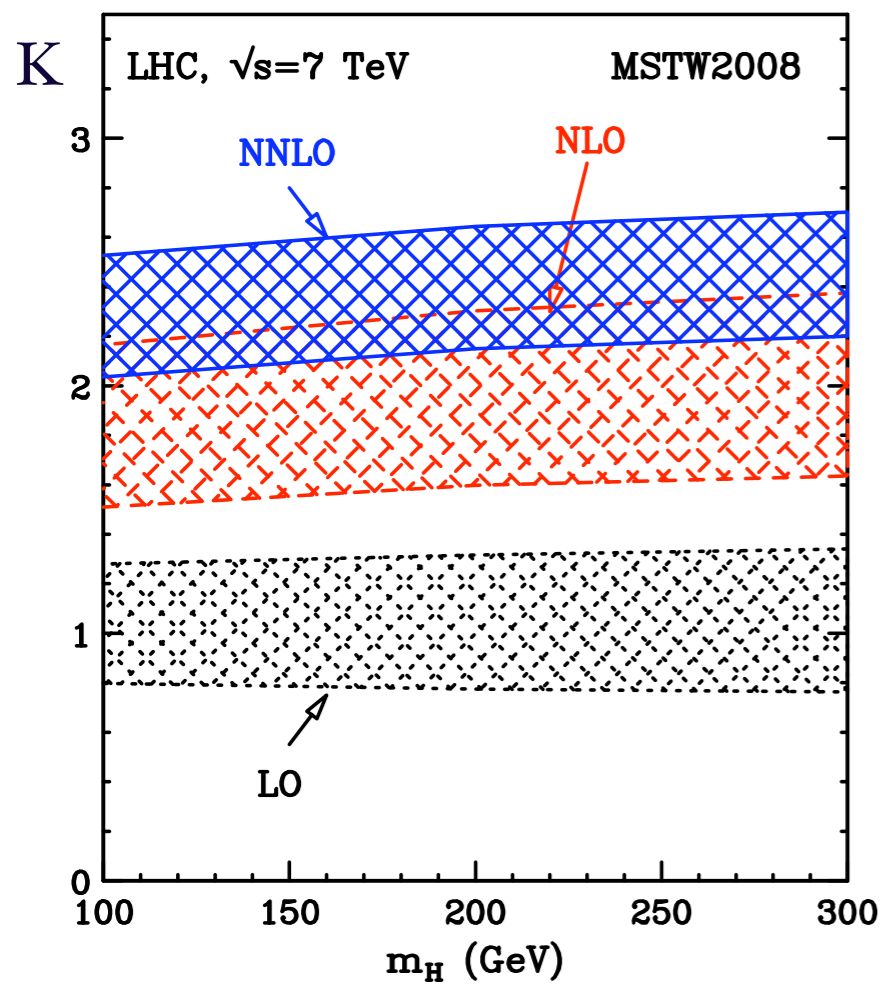


Reduction in mass shift but sensitive to width

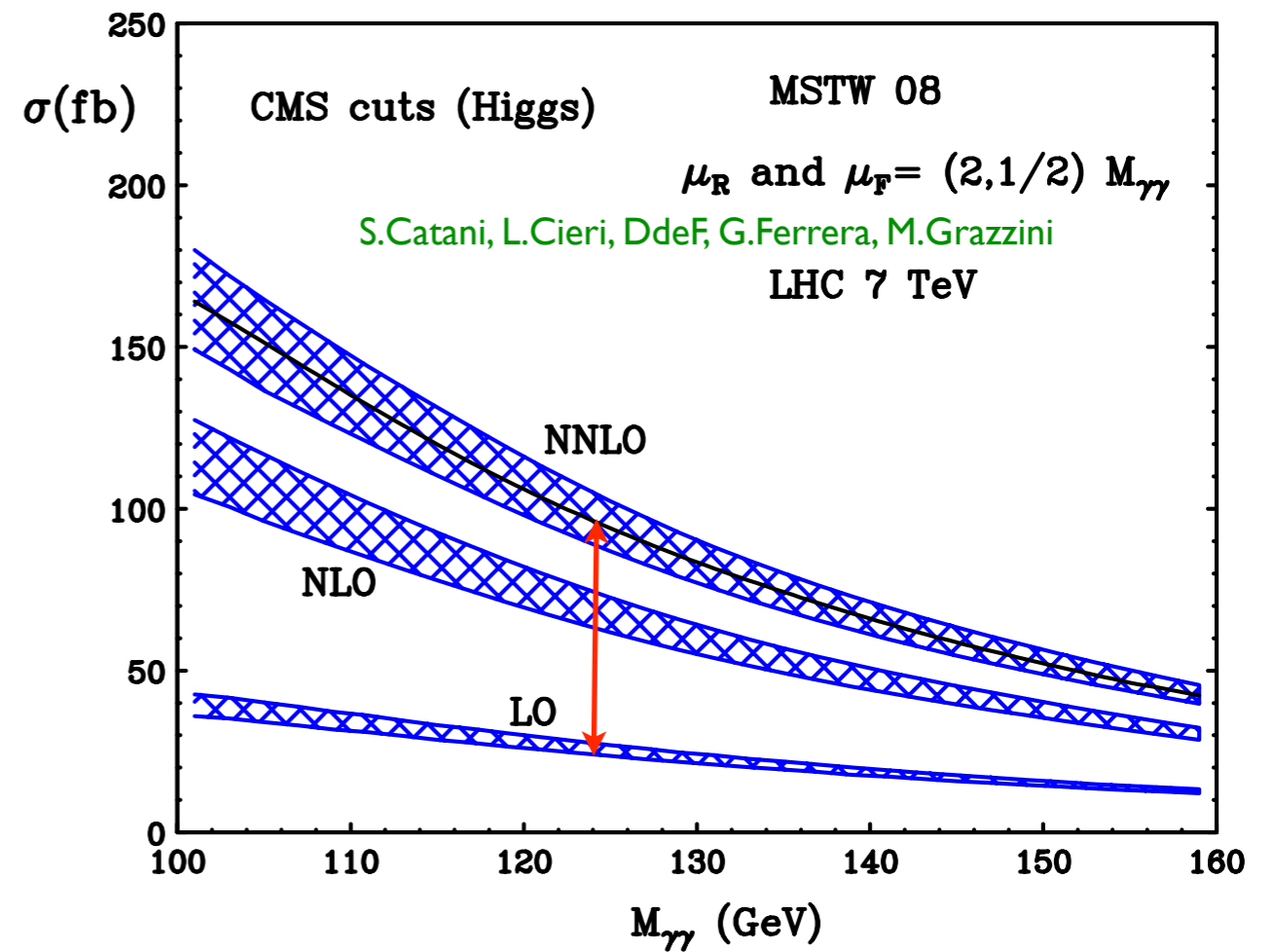
# LH : Accords, Wish-list, Tools, Fondue, Joey Huston, Photons !

Signal NNLO

$$\mathcal{O}(\alpha_s^4)$$



Background NNLO



$$K^{NNLO} \sim 3.5$$